

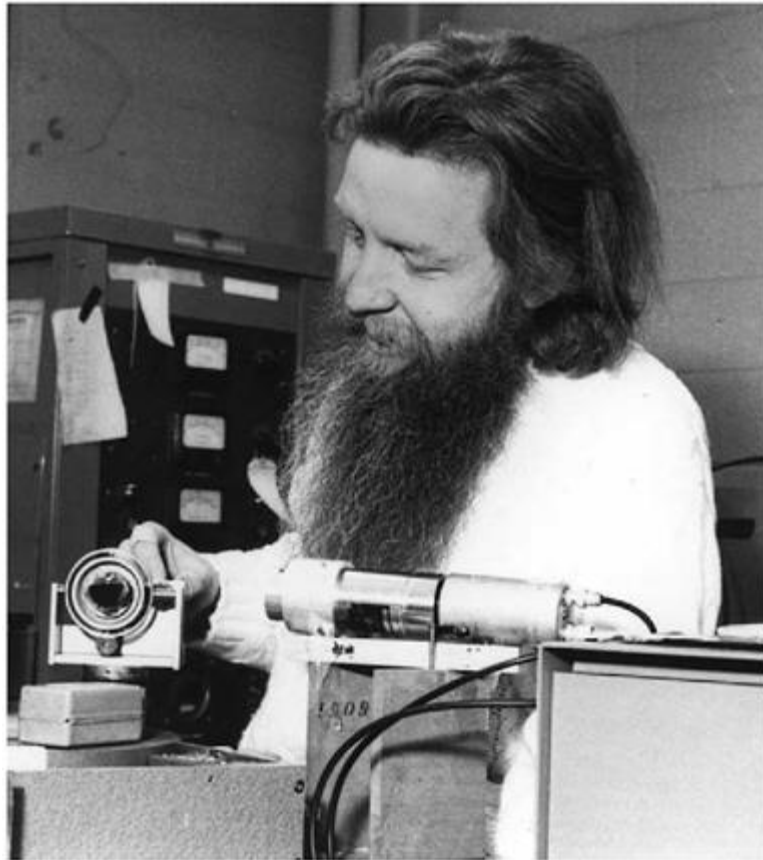
Making Carbon Magnetic

Aaron Sharpe

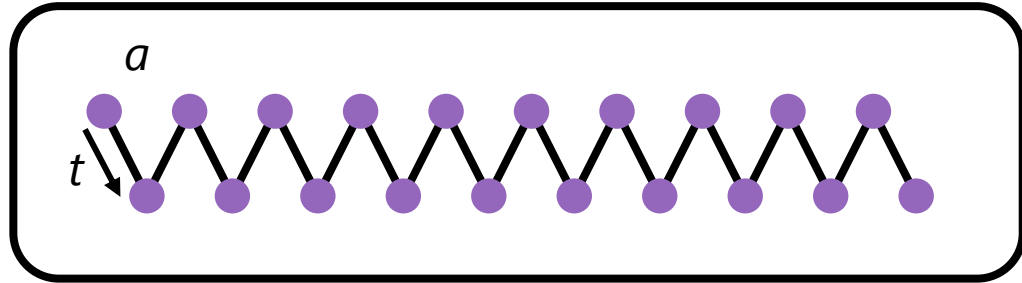
Bill McMillan Colloquium

October 2nd, 2024

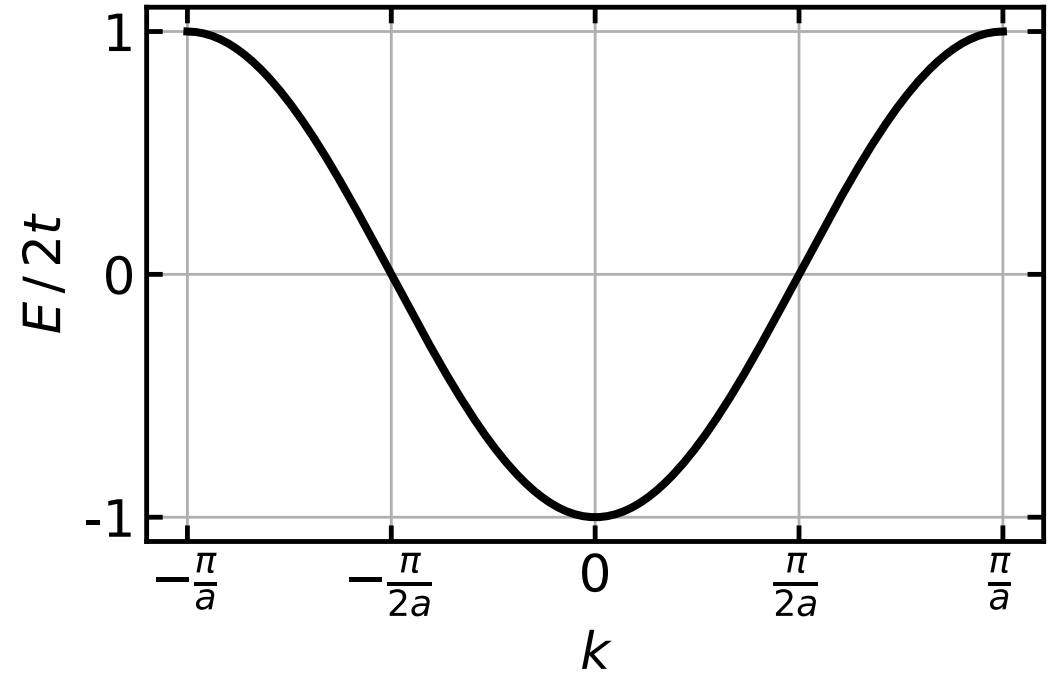
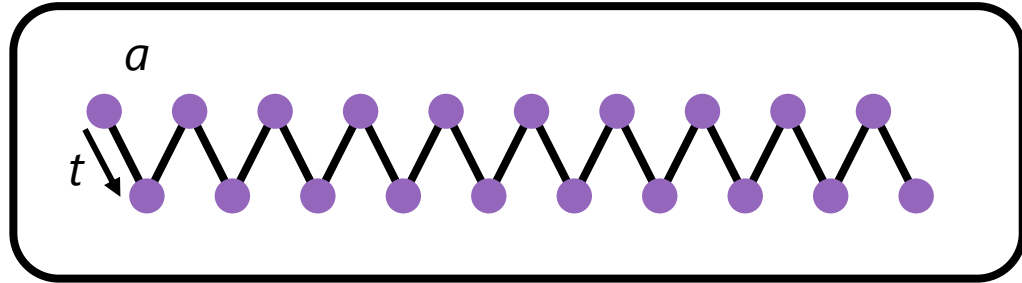
Slides available @ aaronsharpe.science



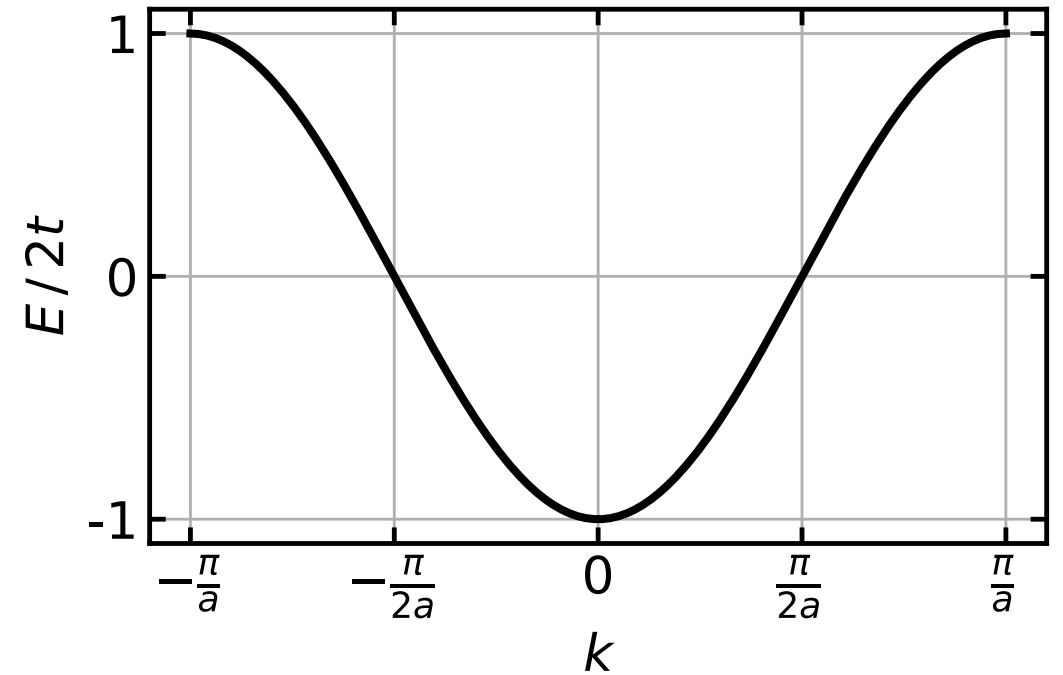
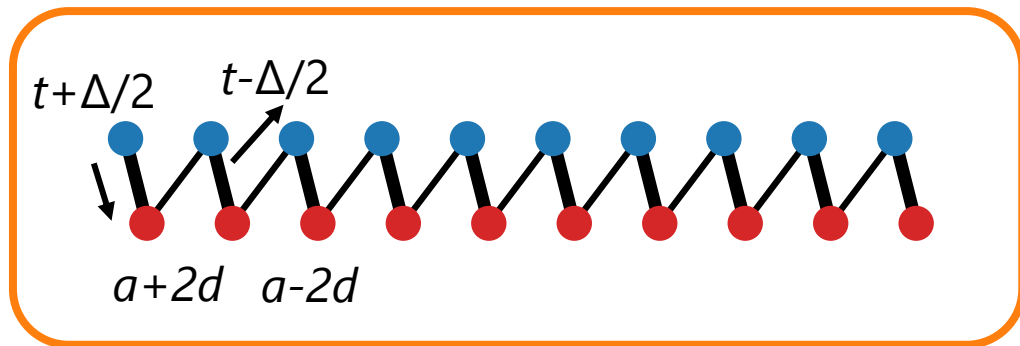
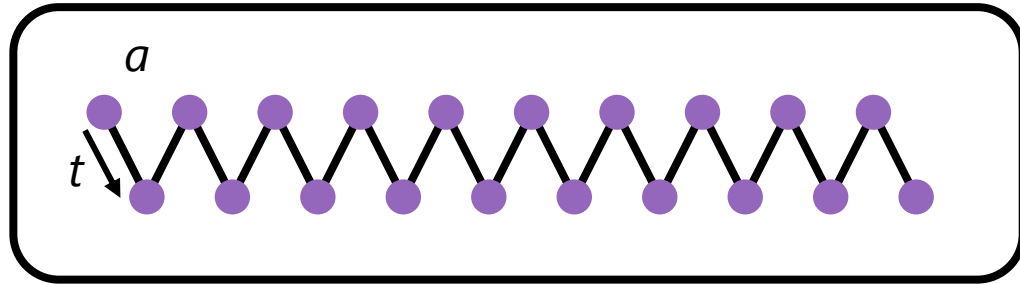
Zig-Zag Chain



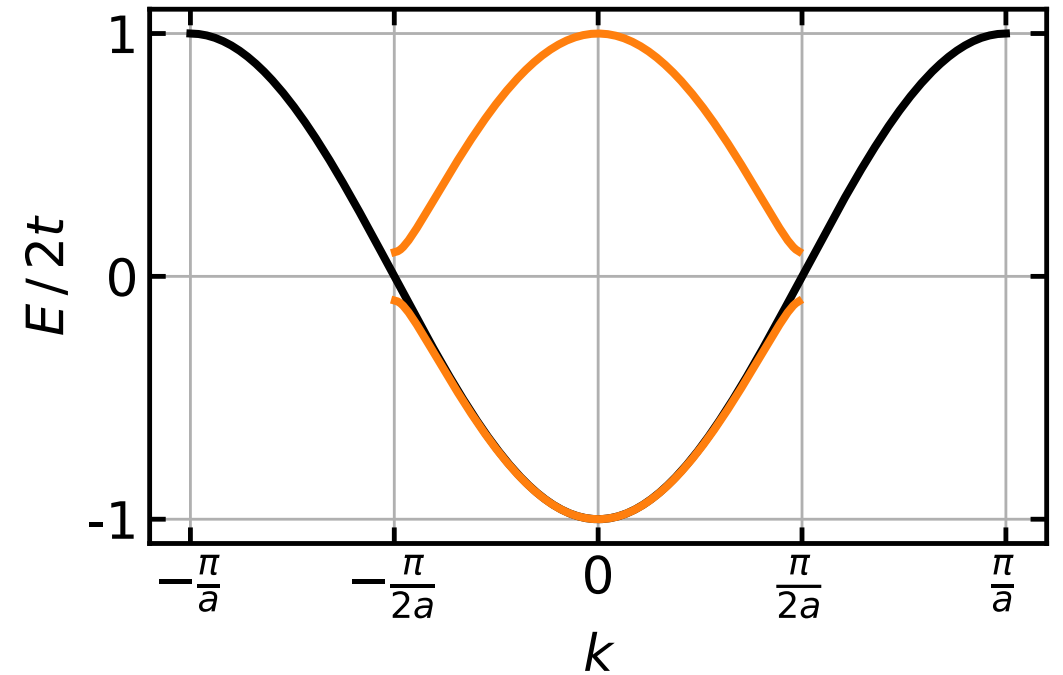
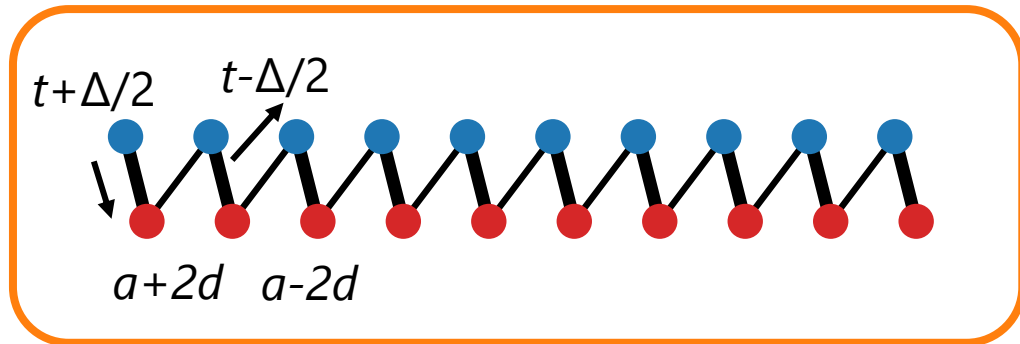
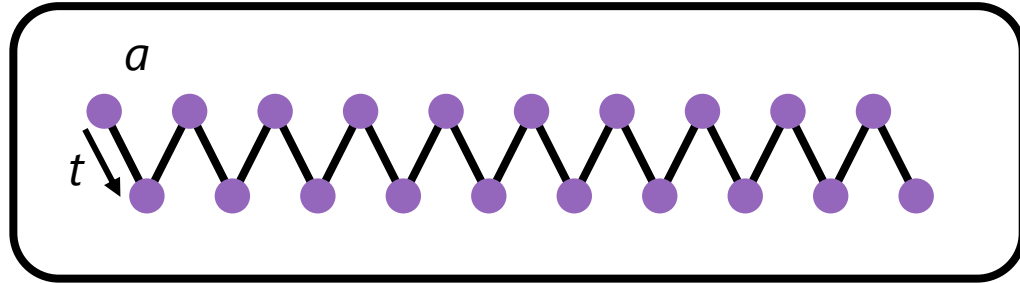
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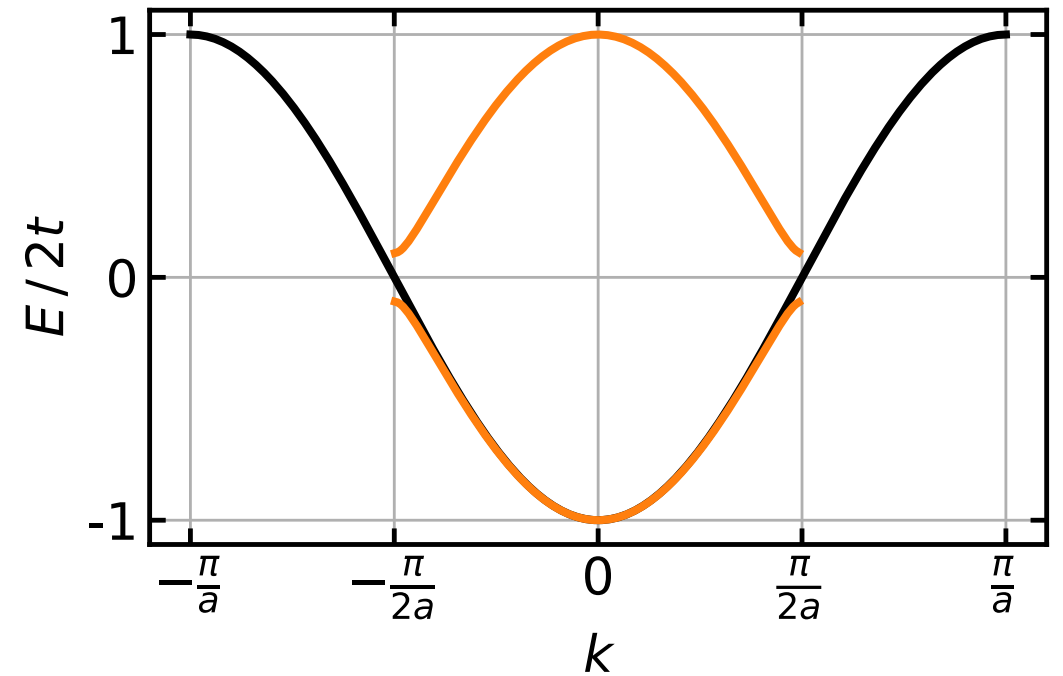
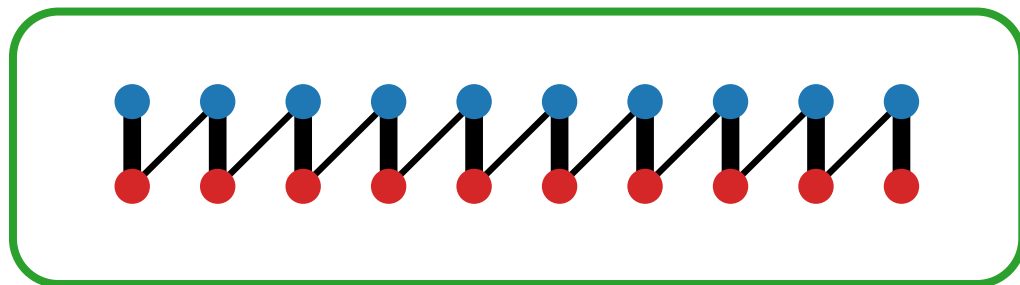
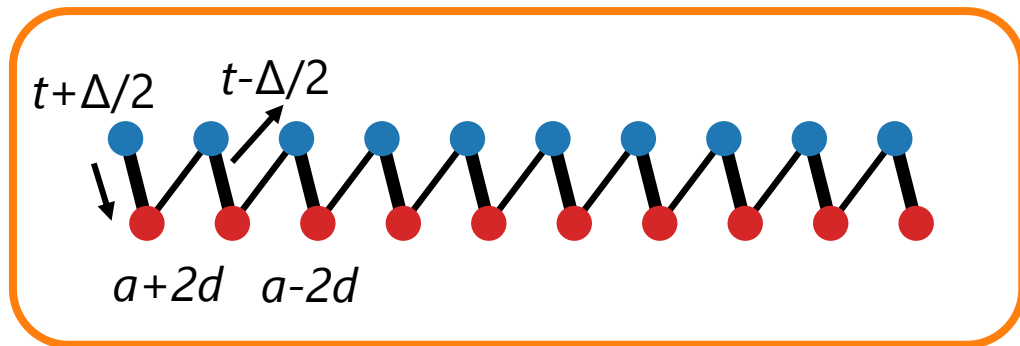
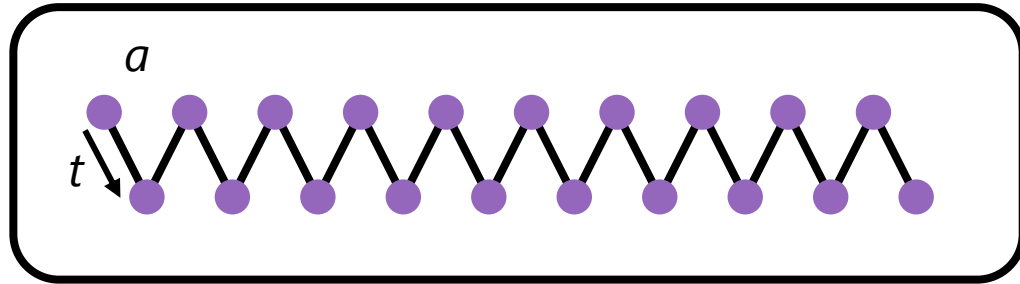
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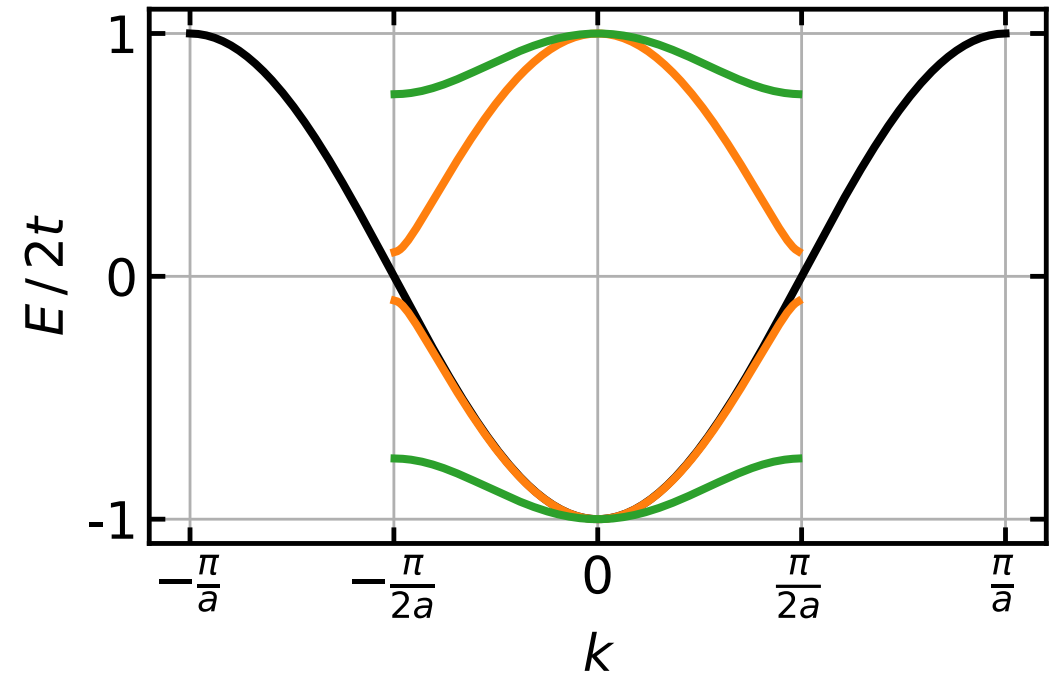
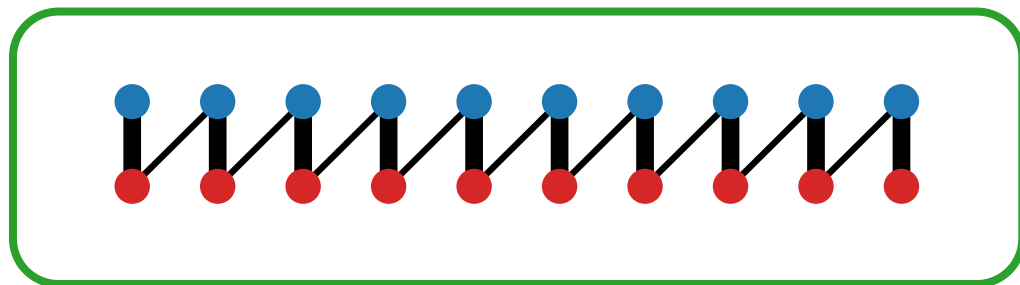
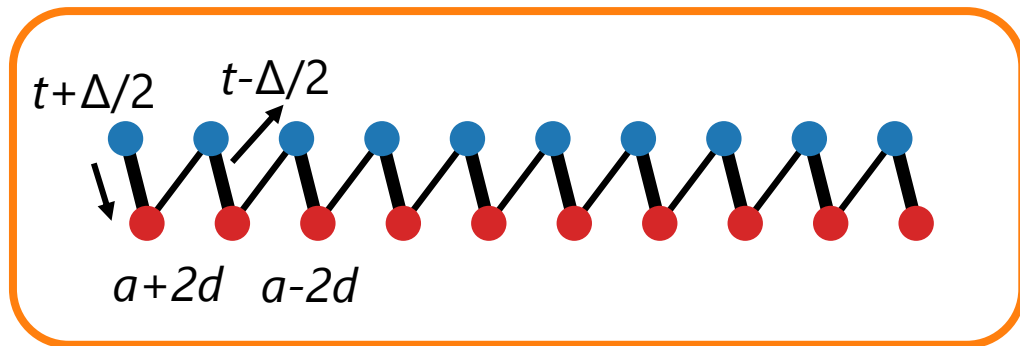
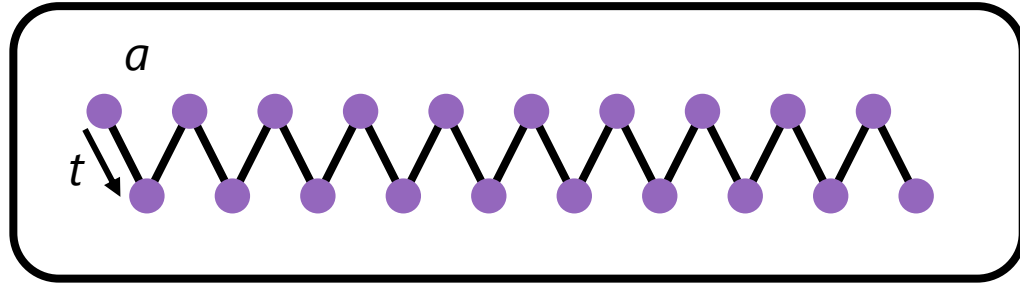
Zig-Zag Chain



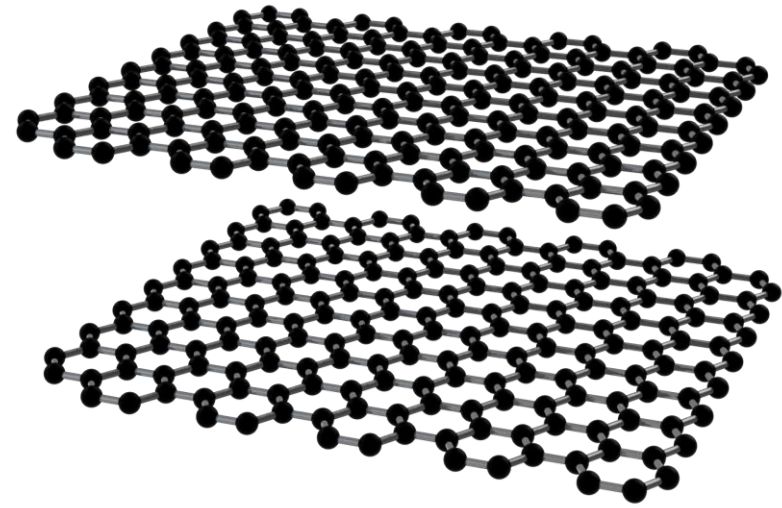
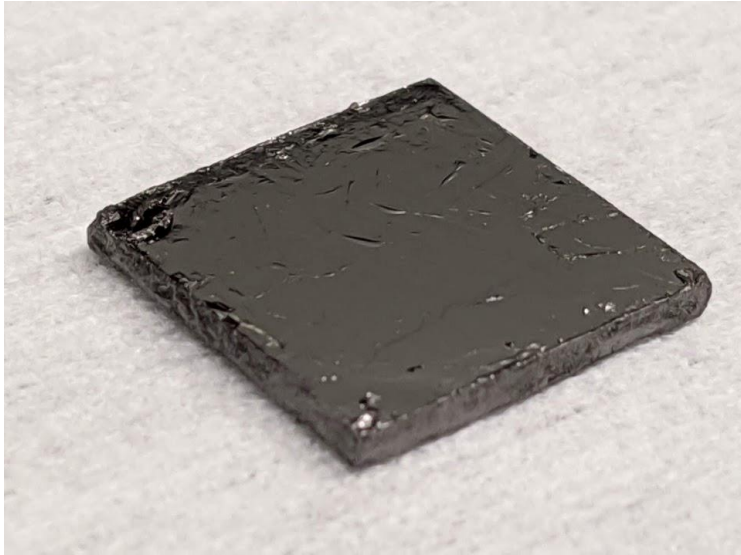
Zig-Zag Chain



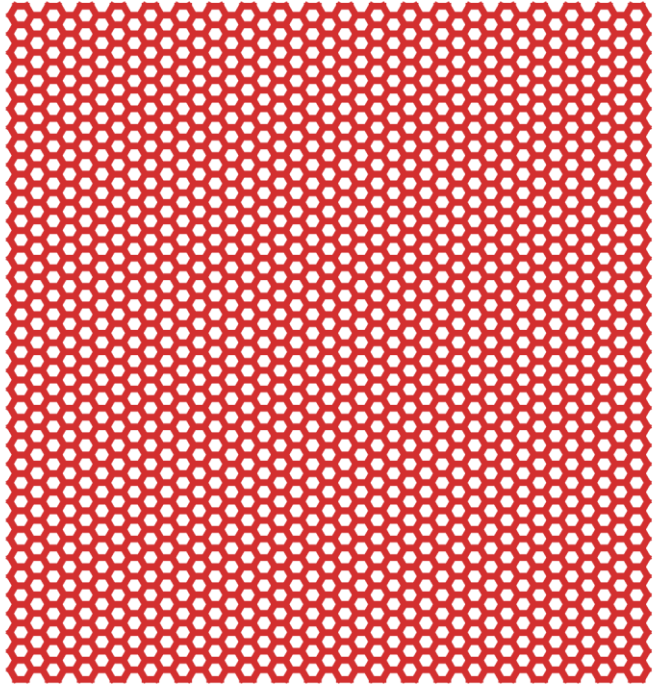
Zig-Zag Chain



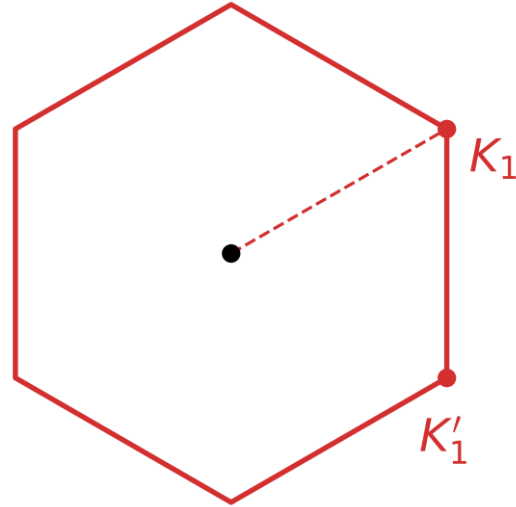
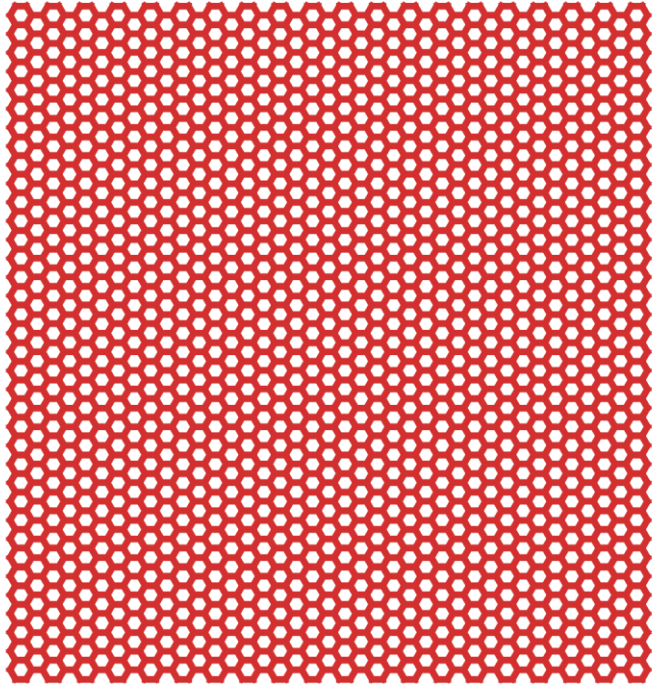
Graphene



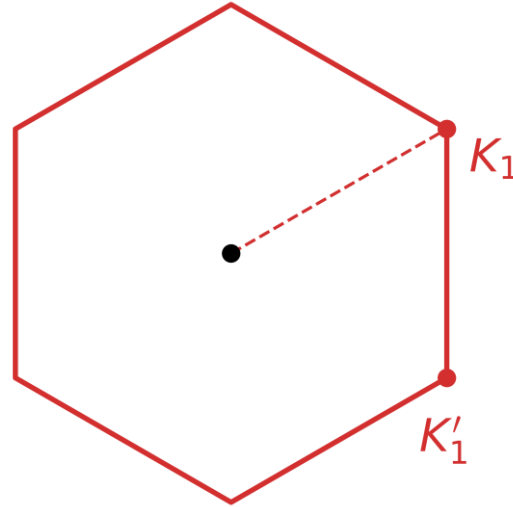
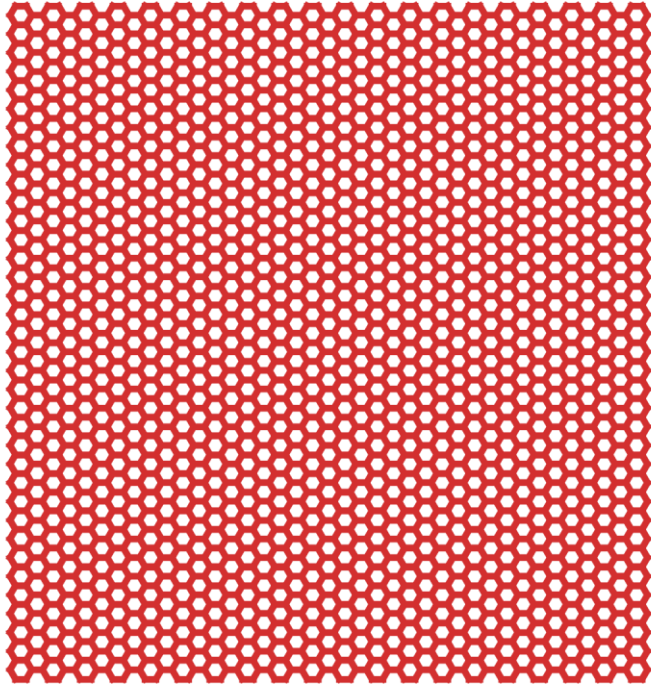
Bandstructure engineering with moirés



Bandstructure engineering with moirés

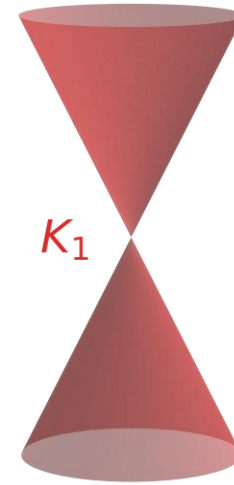
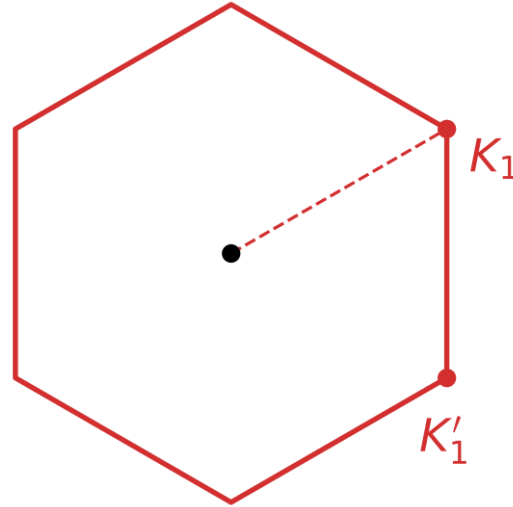
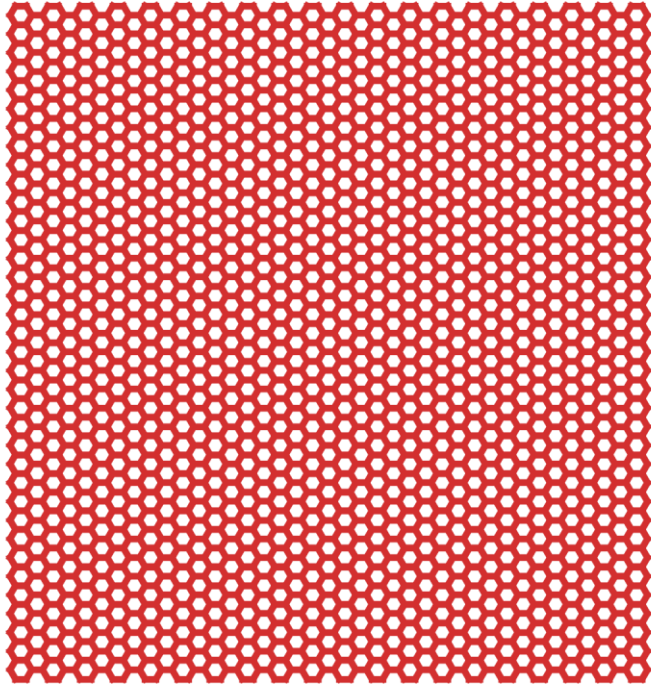


Bandstructure engineering with moirés



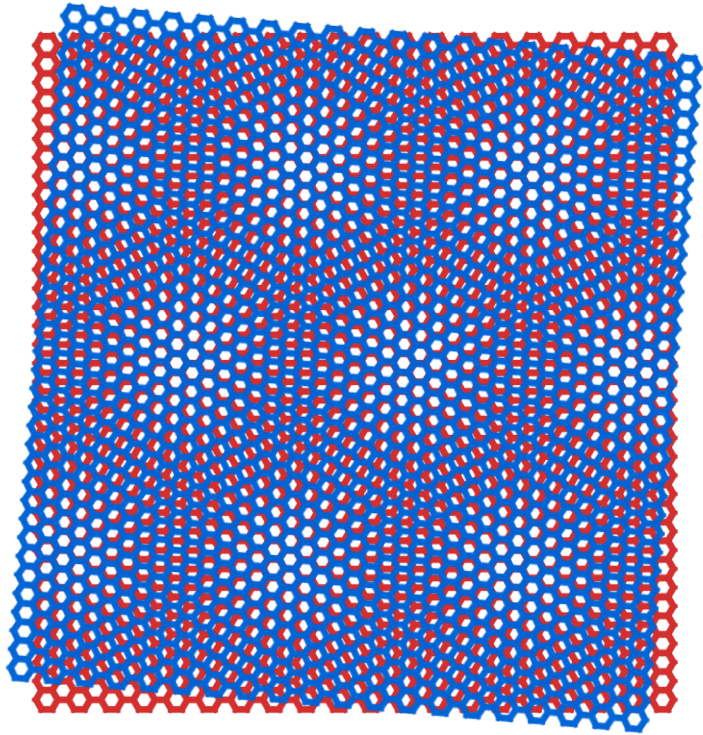
4-fold degenerate
spin x valley

Bandstructure engineering with moirés

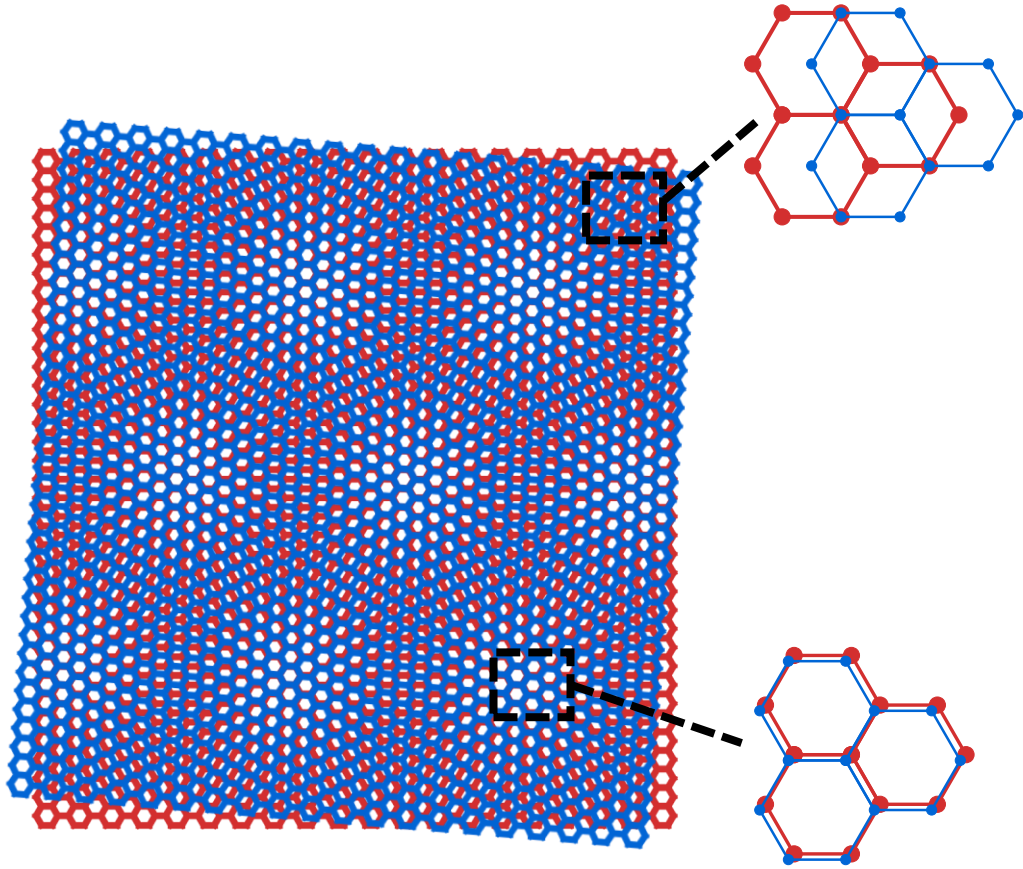


4-fold degenerate
spin x valley

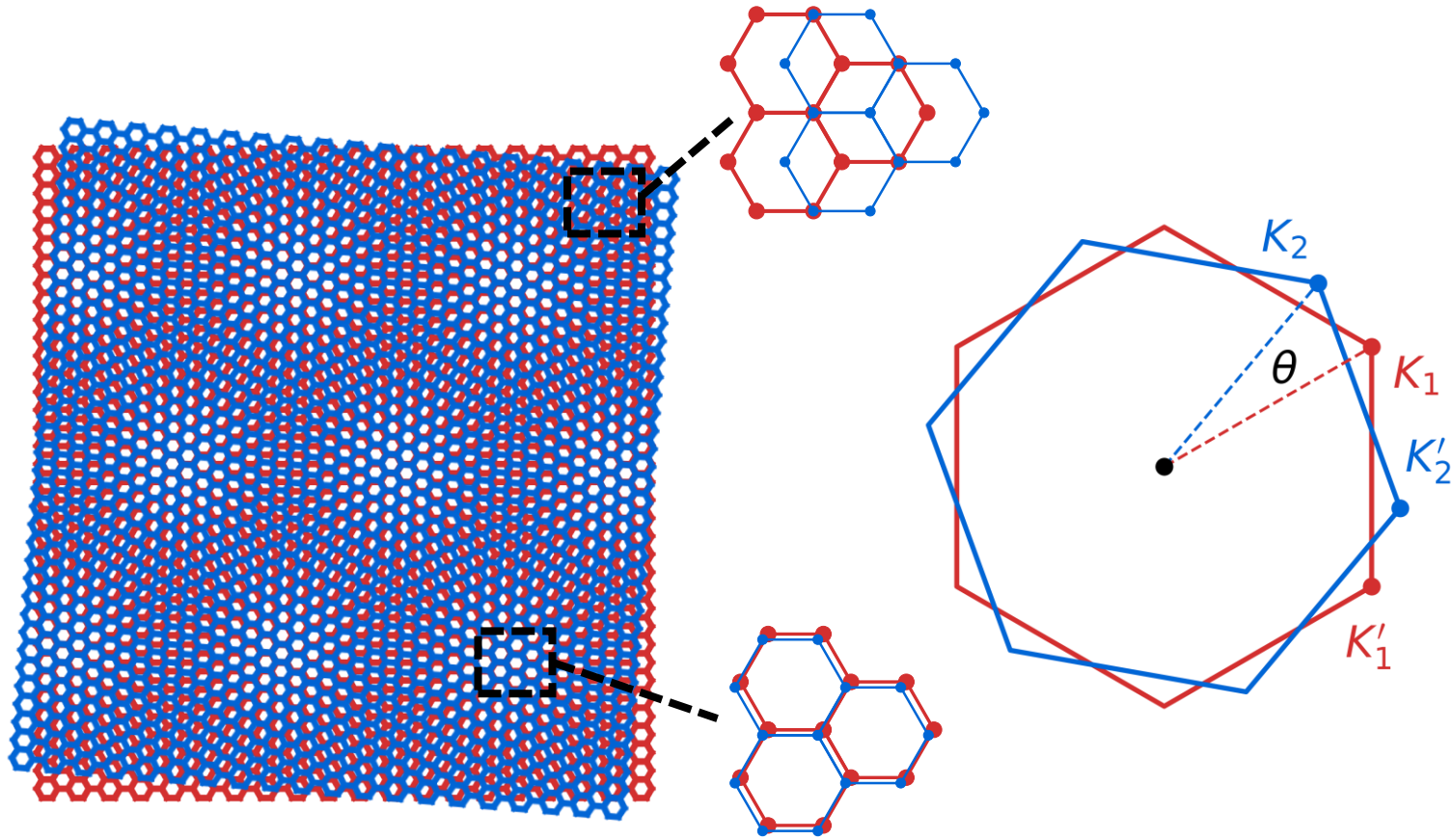
Bandstructure engineering with moirés



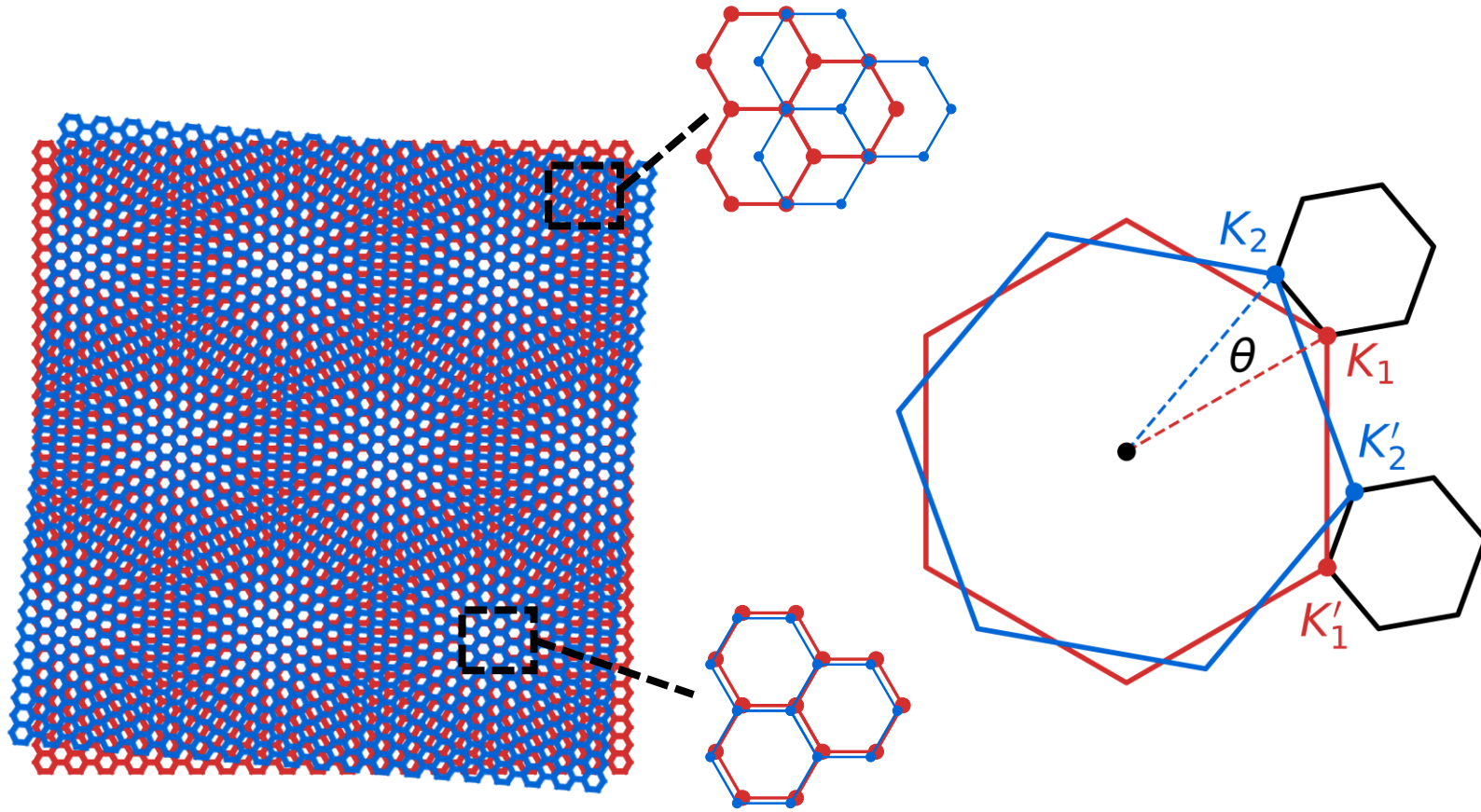
Bandstructure engineering with moirés



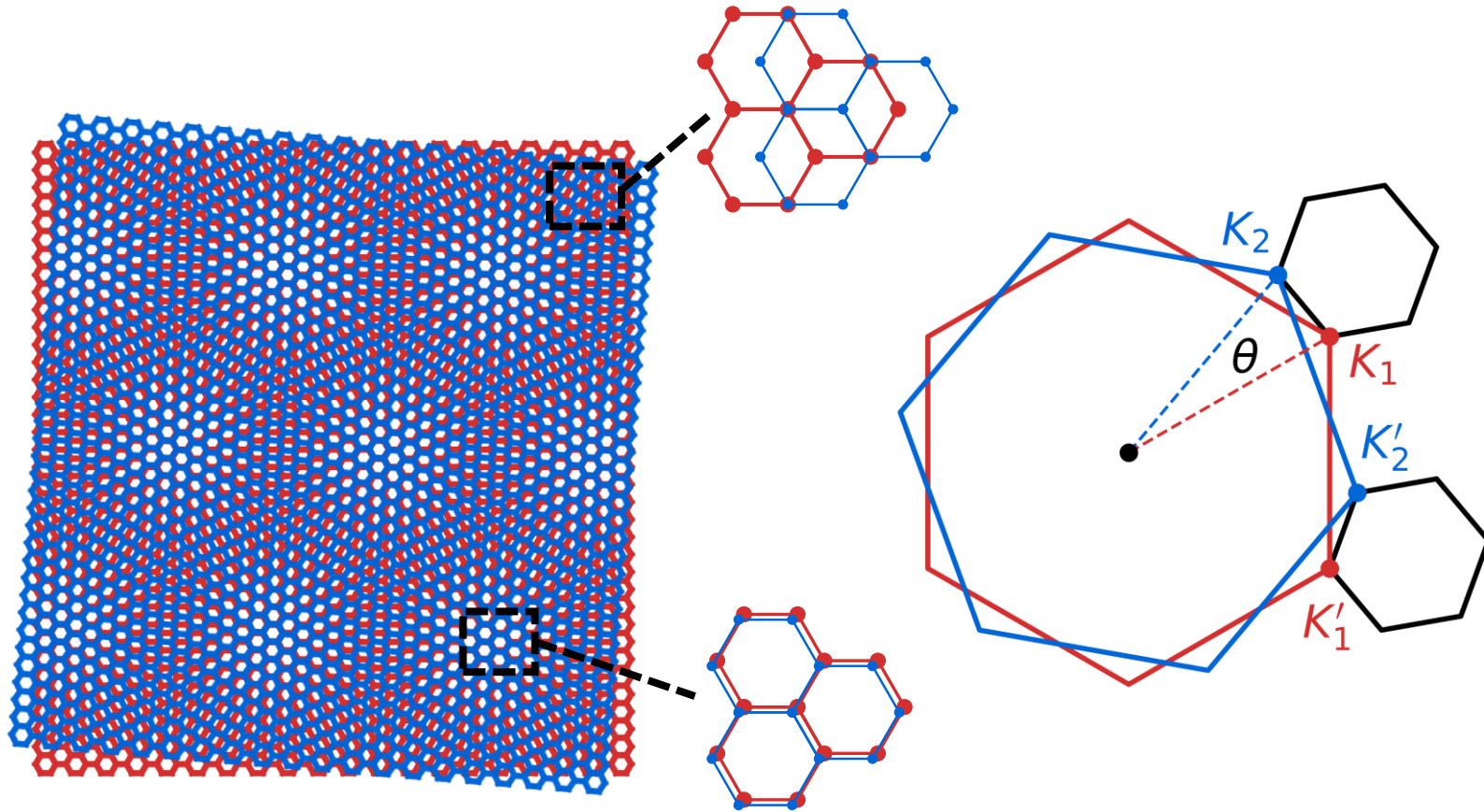
Bandstructure engineering with moirés



Bandstructure engineering with moirés

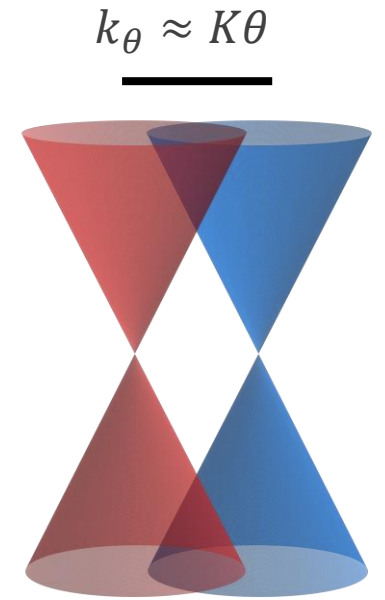
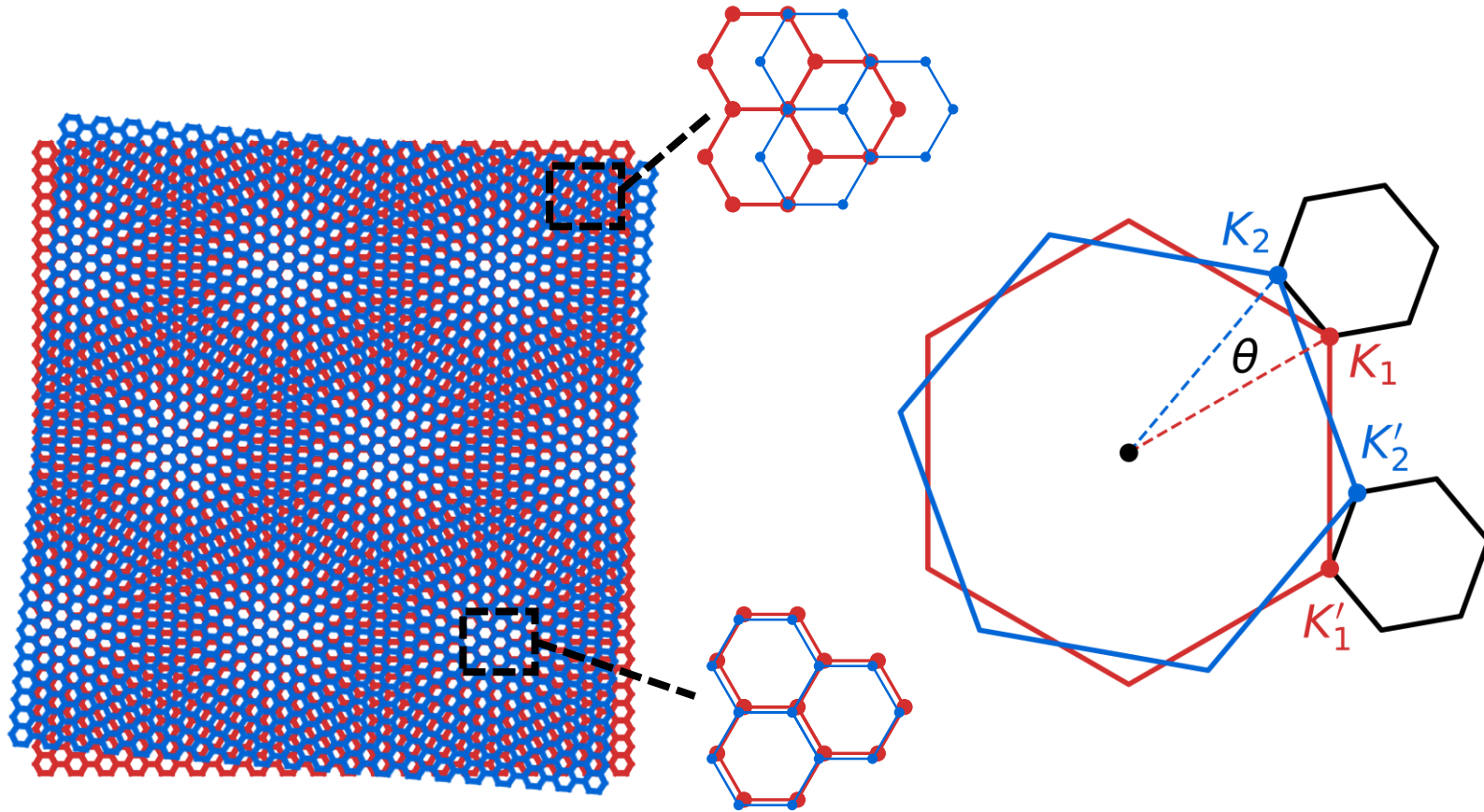


Bandstructure engineering with moirés



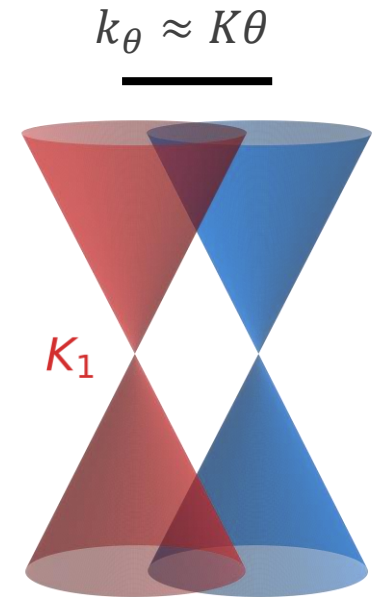
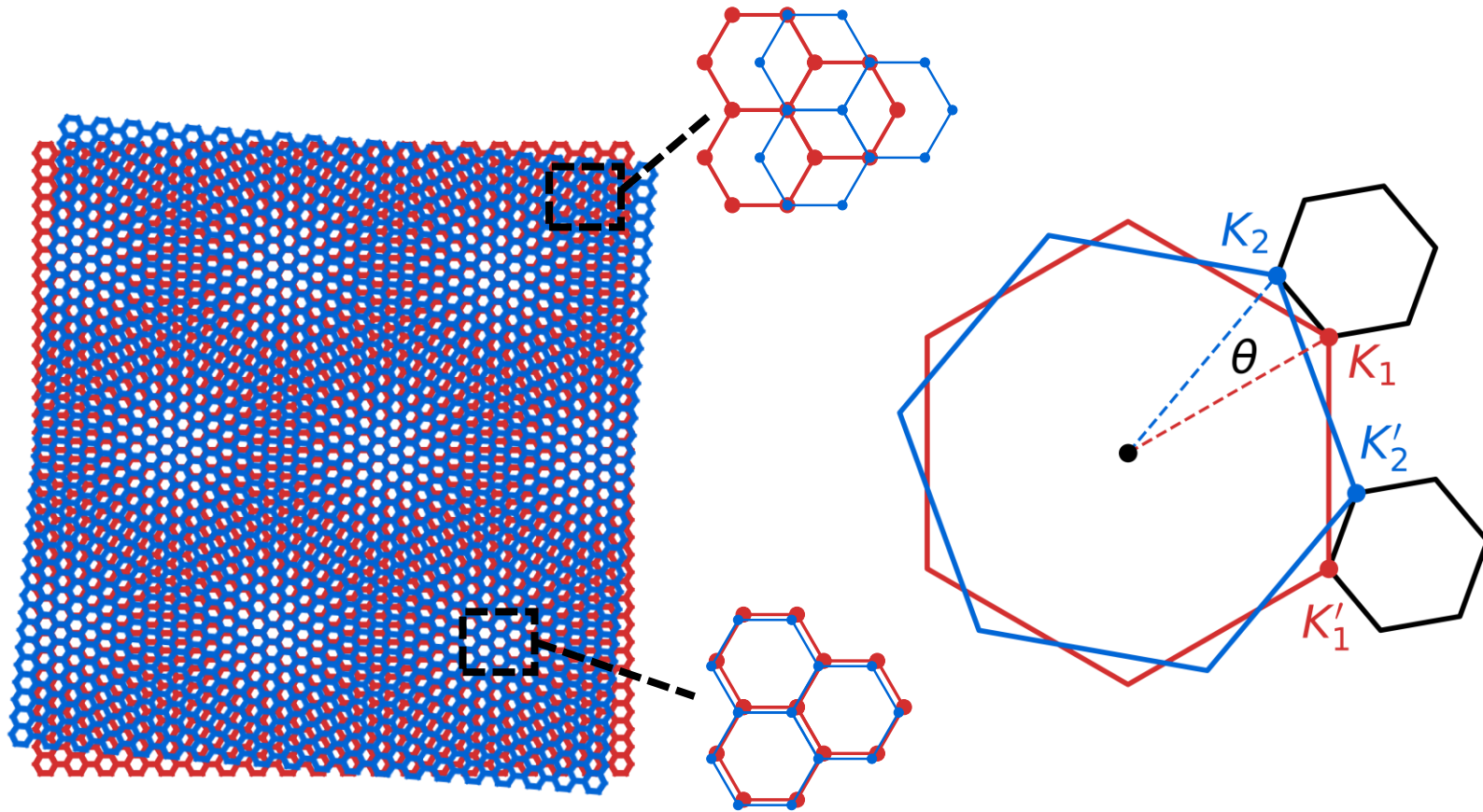
4-fold degenerate
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Bandstructure engineering with moirés



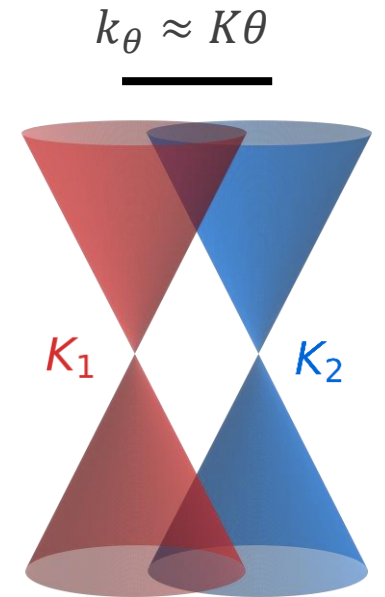
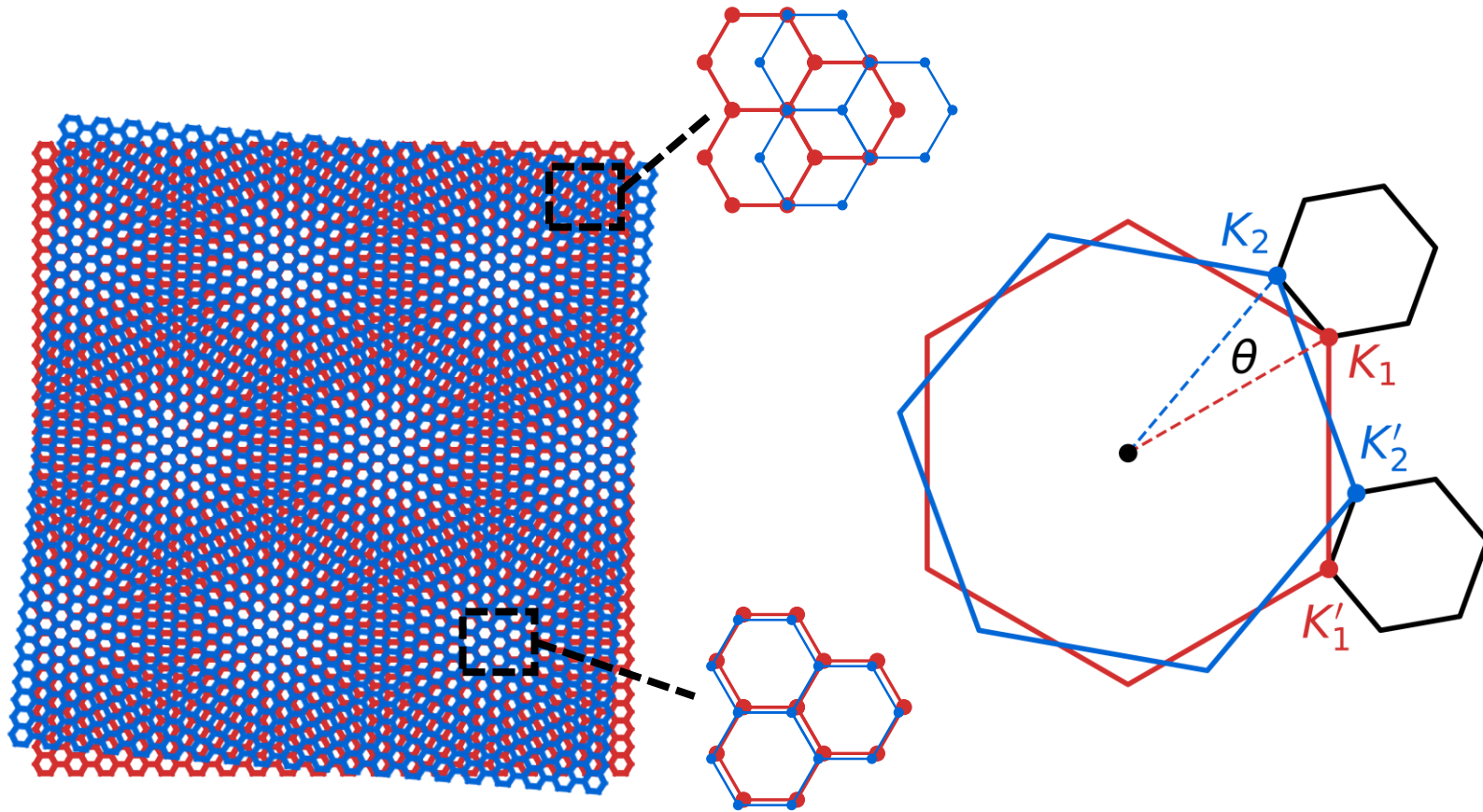
4-fold degenerate
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Bandstructure engineering with moirés



4-fold degenerate
spin x valley

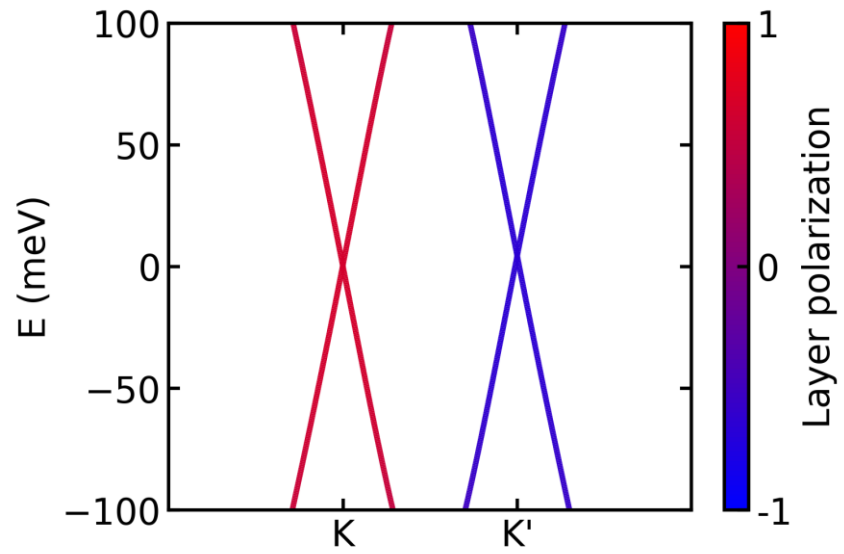
Bandstructure engineering with moirés



4-fold degenerate
spin x valley

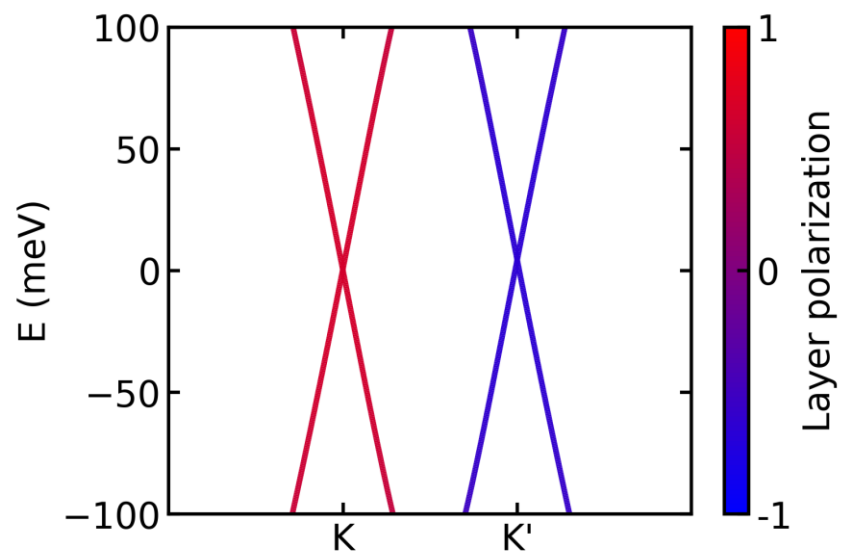
Bandstructure engineering with moirés

3.0°



Bandstructure engineering with moirés

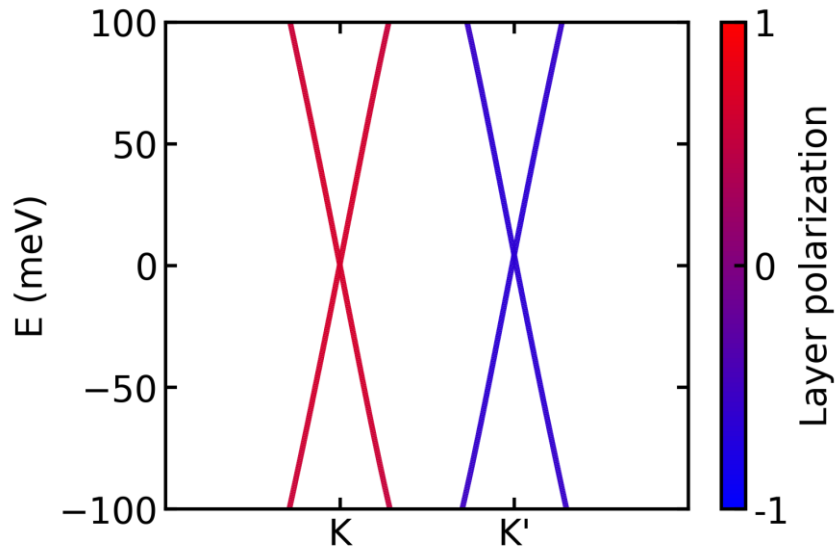
3.0°



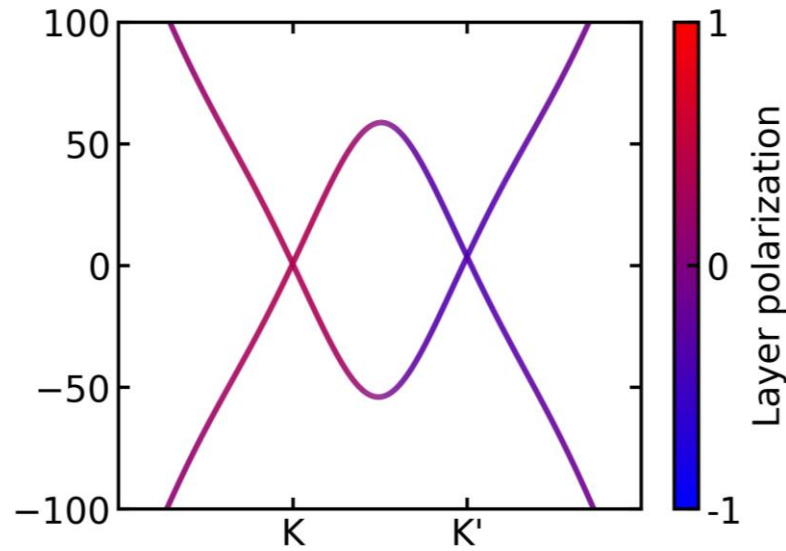
Decreasing twist angle

Bandstructure engineering with moirés

3.0°



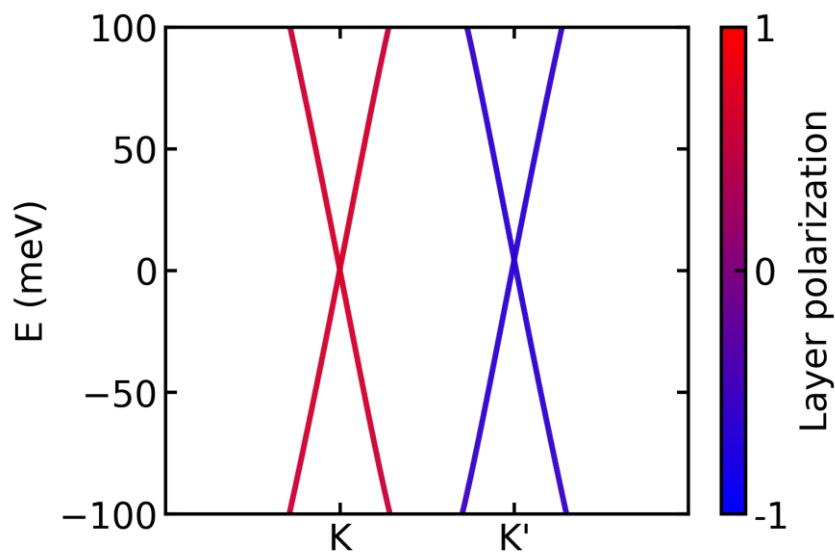
2.0°



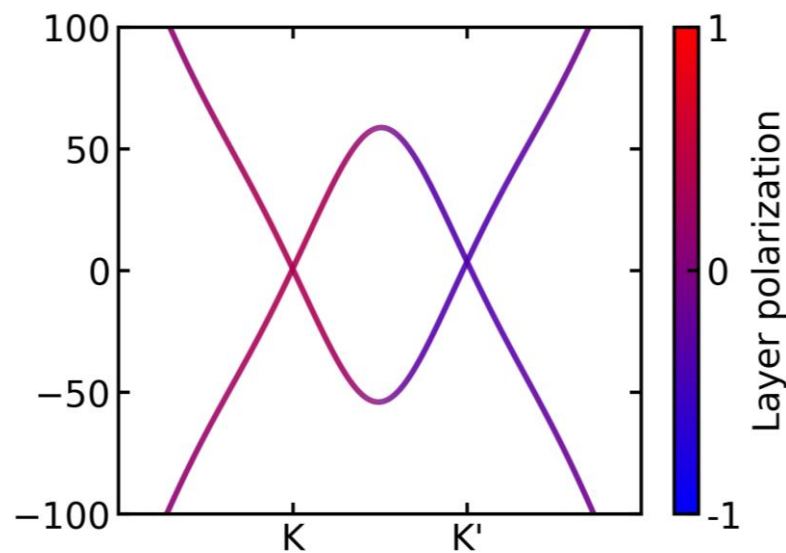
Decreasing twist angle

Bandstructure engineering with moirés

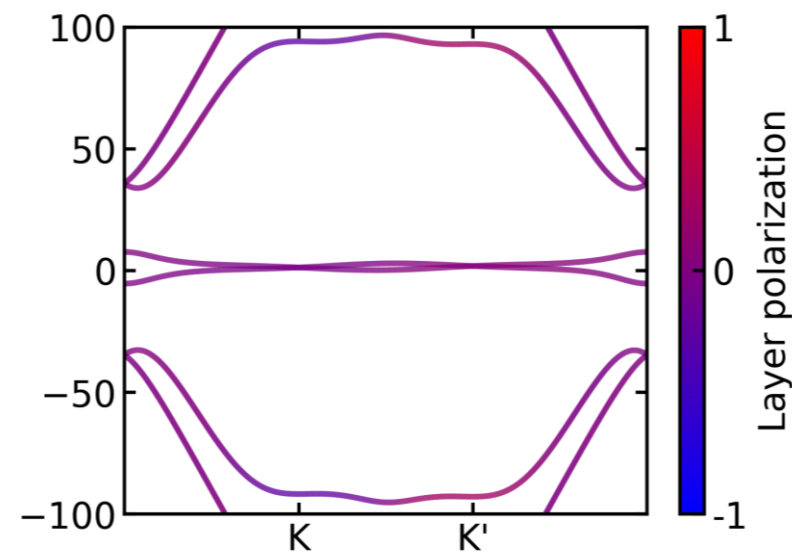
3.0°



2.0°

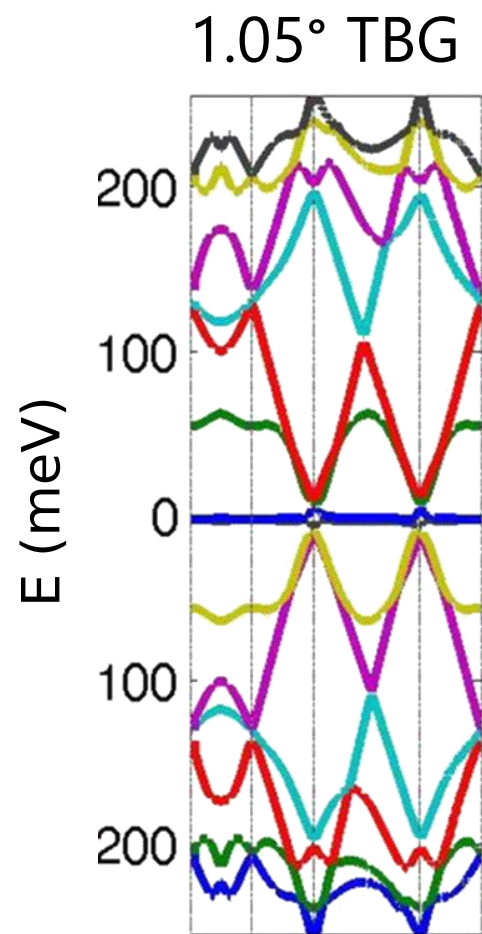


1.1°

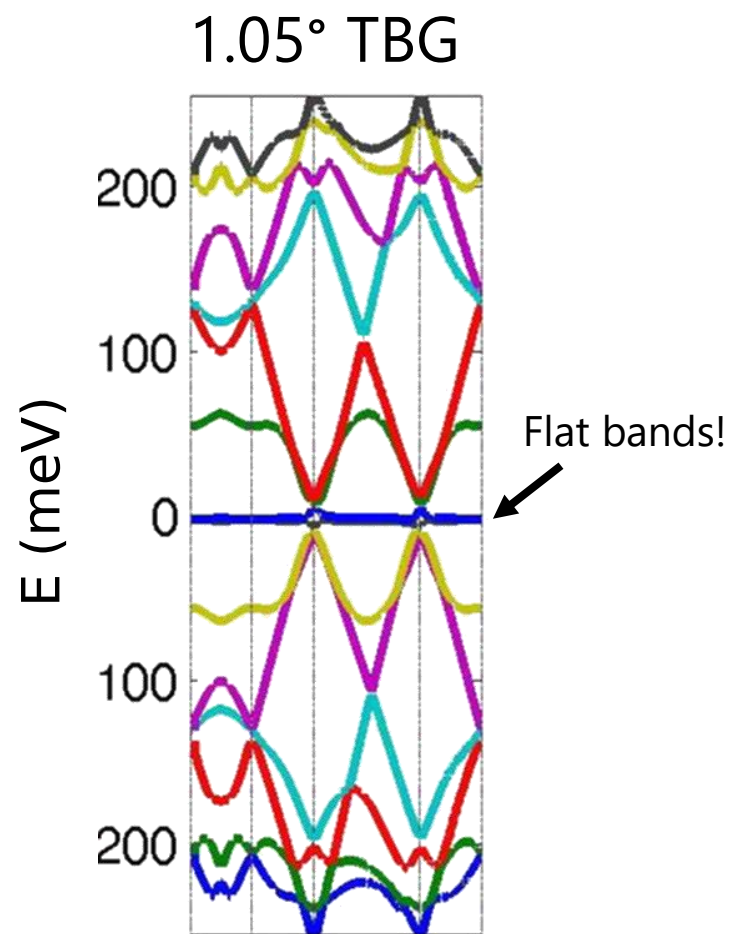


Decreasing twist angle

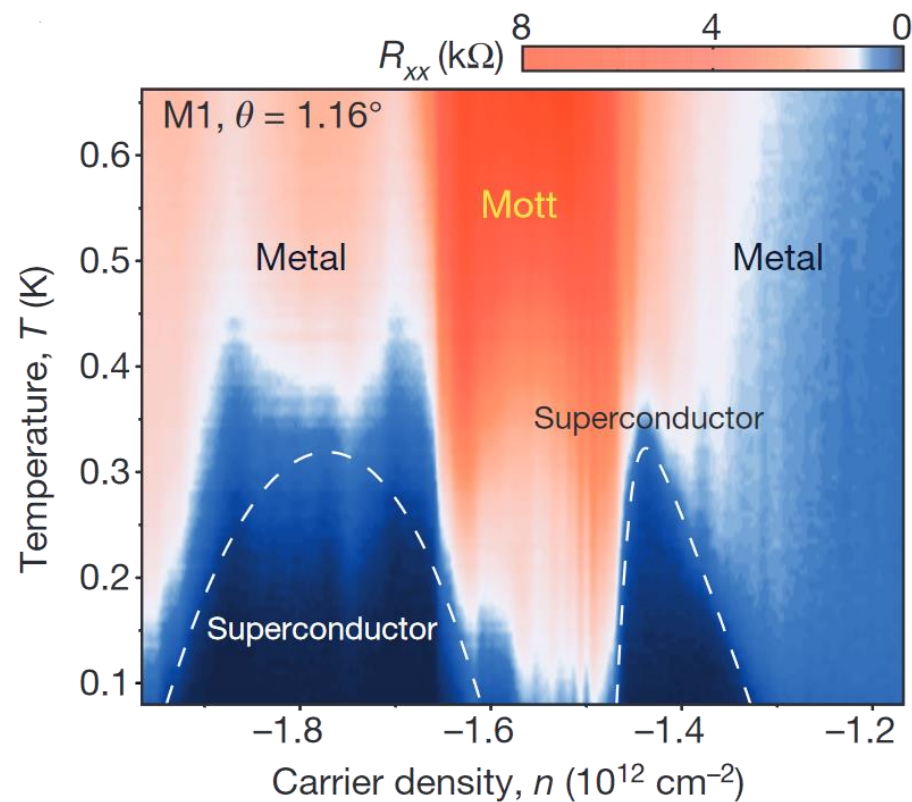
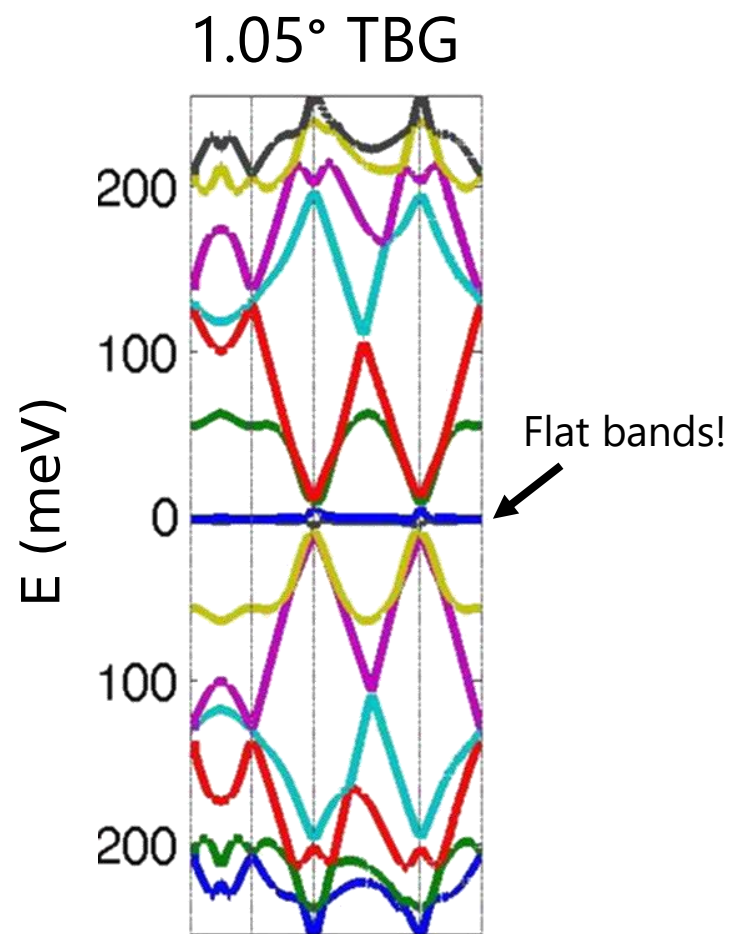
First experimental realization of TBG



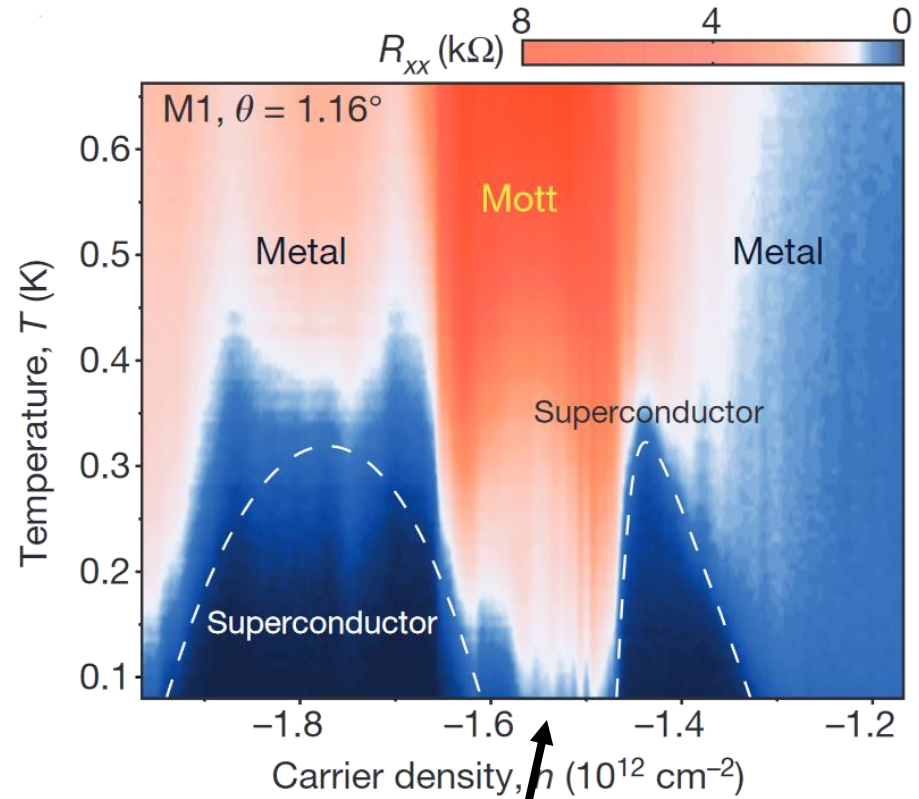
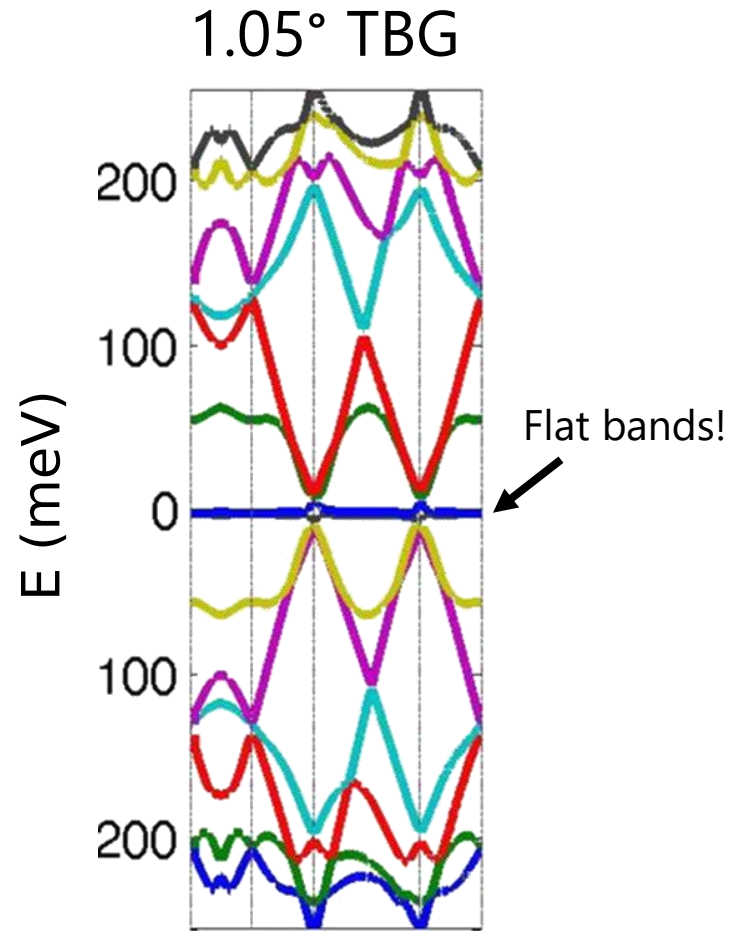
First experimental realization of TBG



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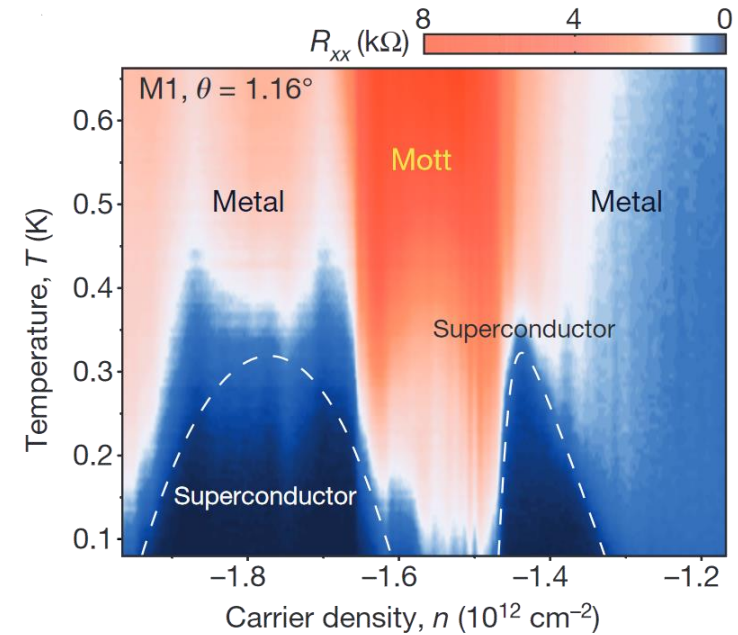
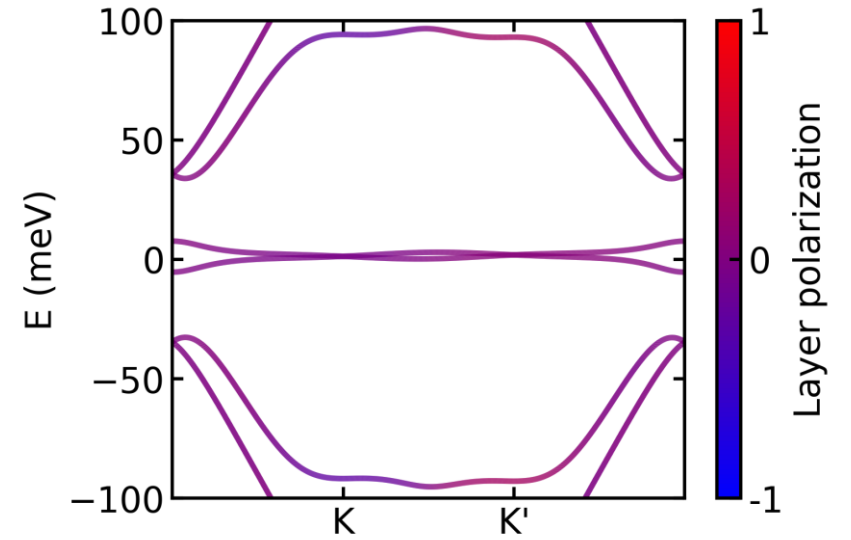


Half filled band – symmetry broken phase
Think Hund's rules

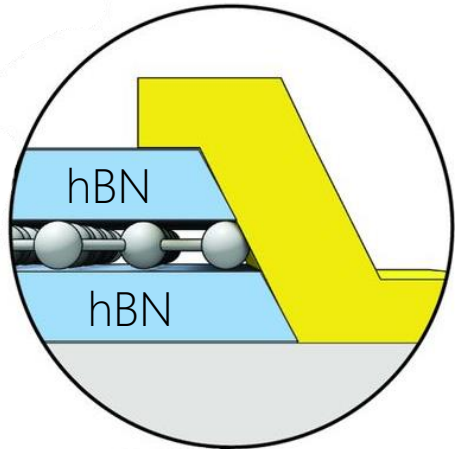
Summary

By controlling twist angle, graphene multilayers can become strongly correlated!

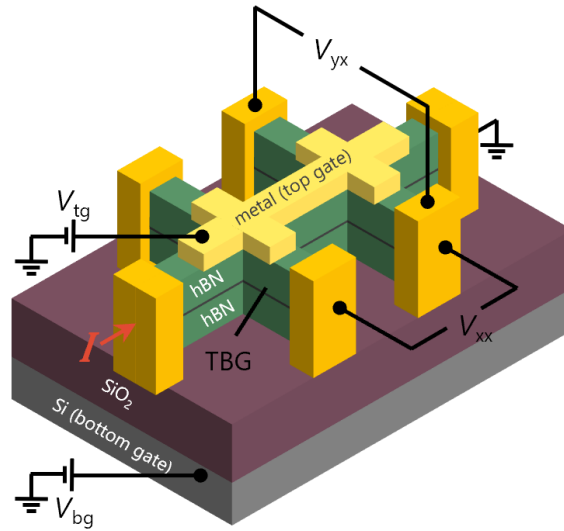
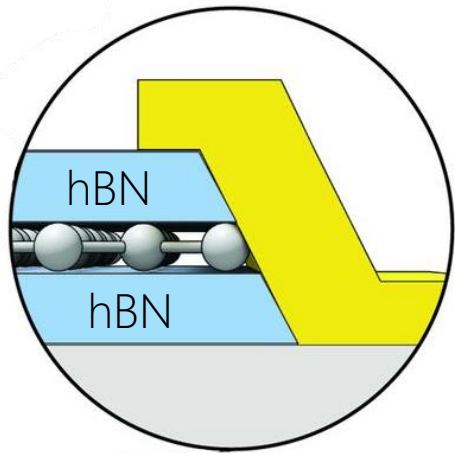
Let's make some samples!



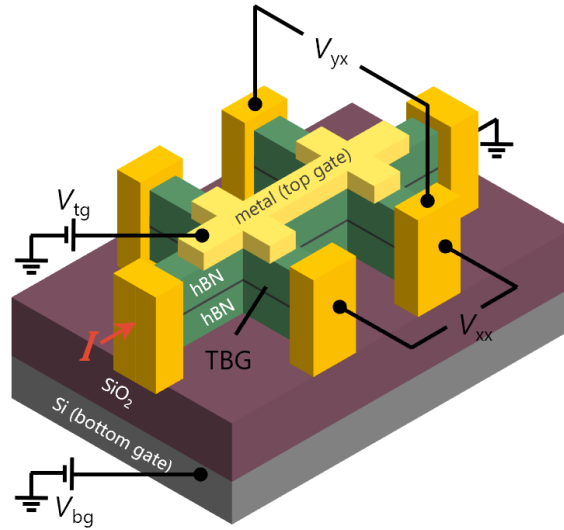
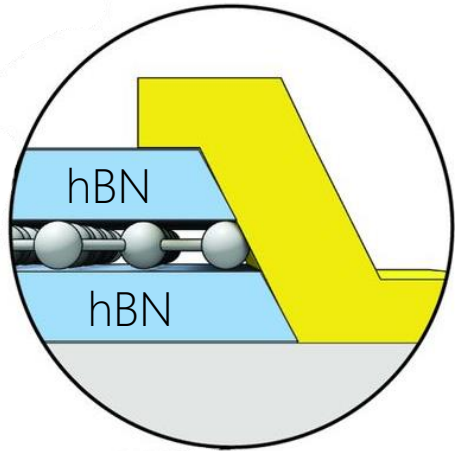
Typical twisted bilayer graphene (TBG)



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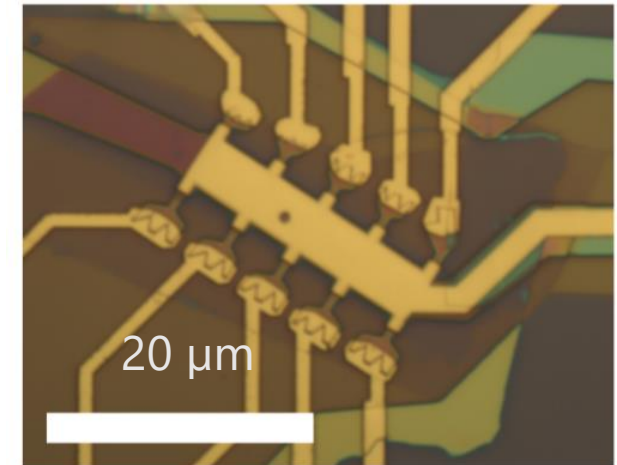
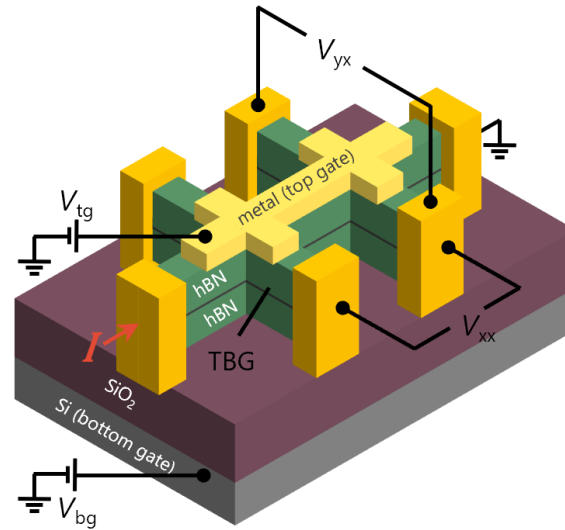
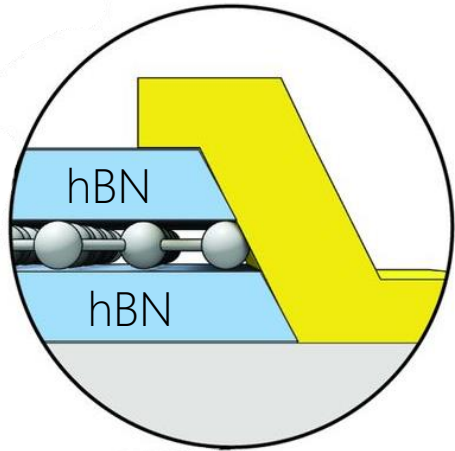


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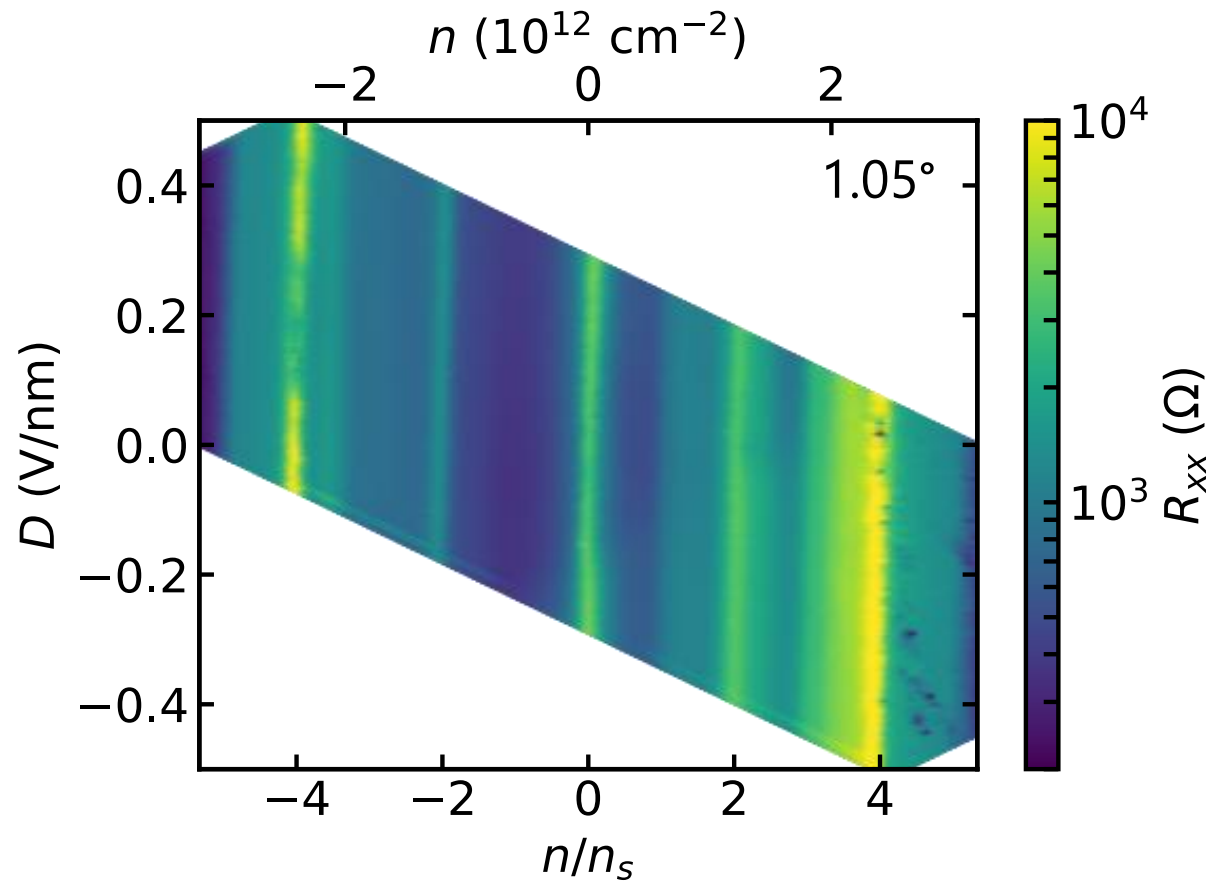
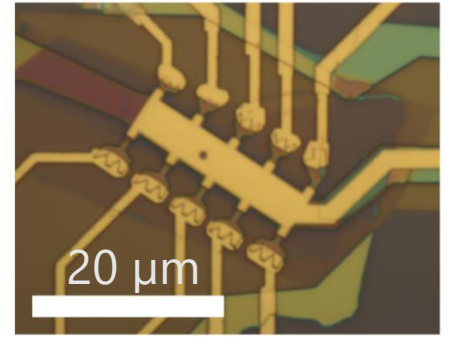
$$n \propto V_{tg}/d_{tg} + V_{bg}/d_{bg}$$
$$D \propto V_{tg}/d_{tg} - V_{bg}/d_{bg}$$

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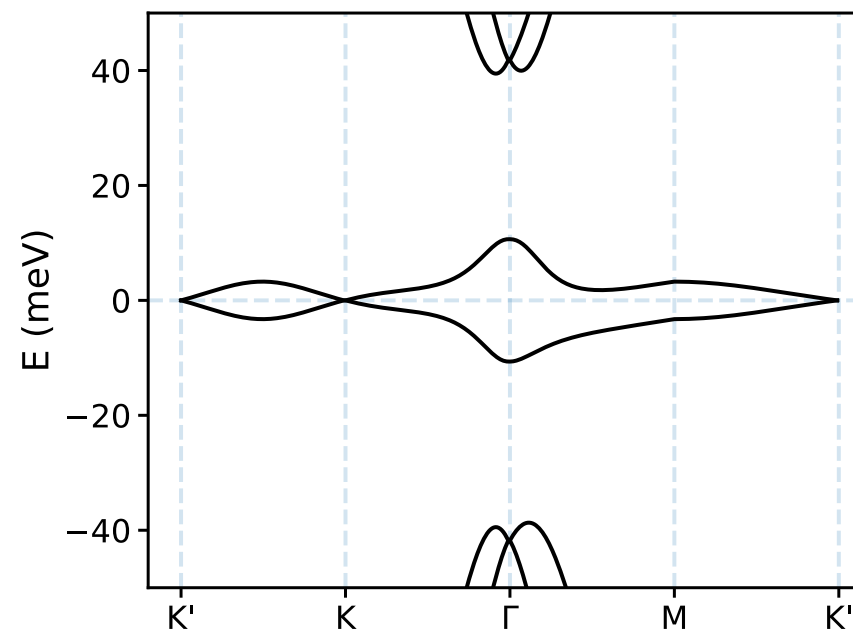
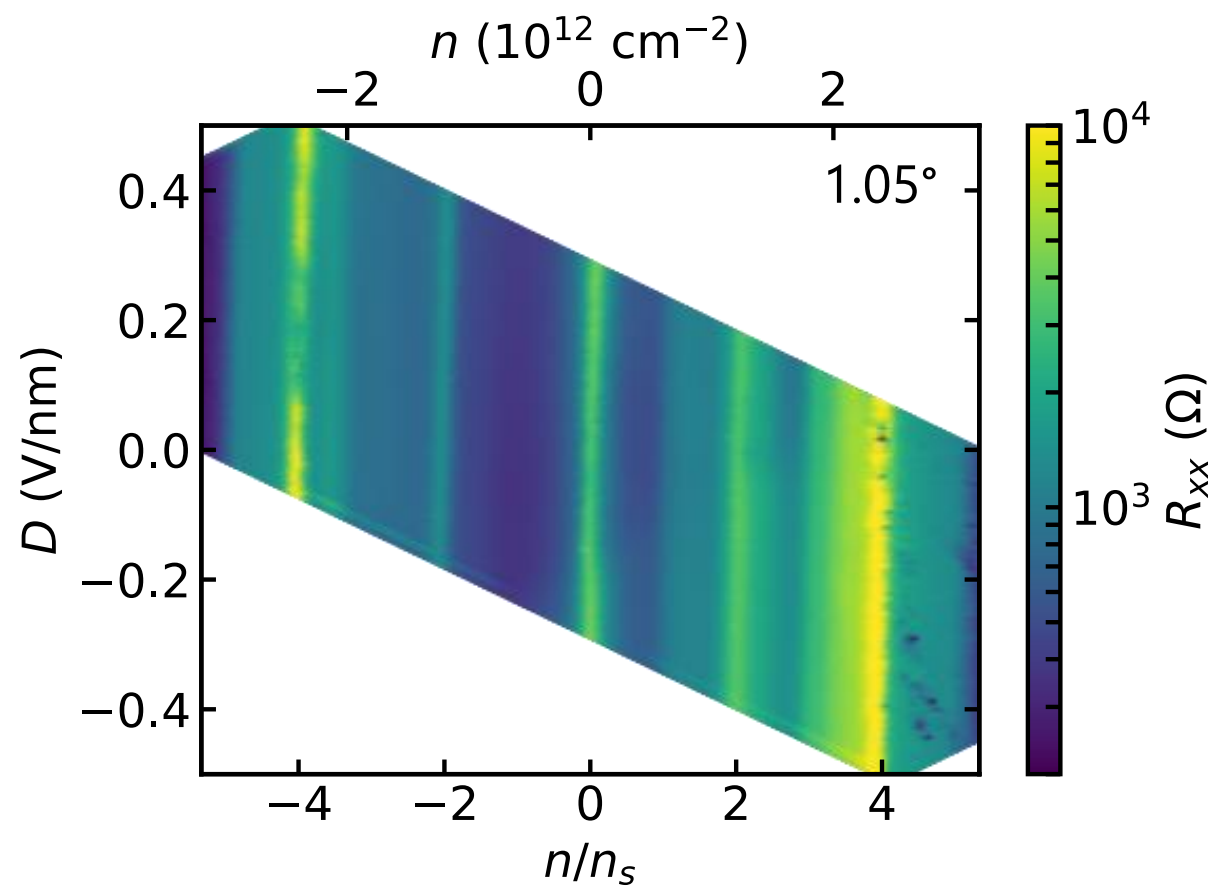
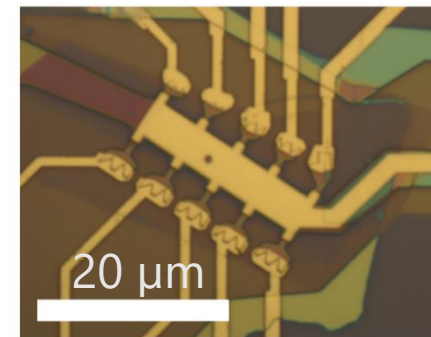


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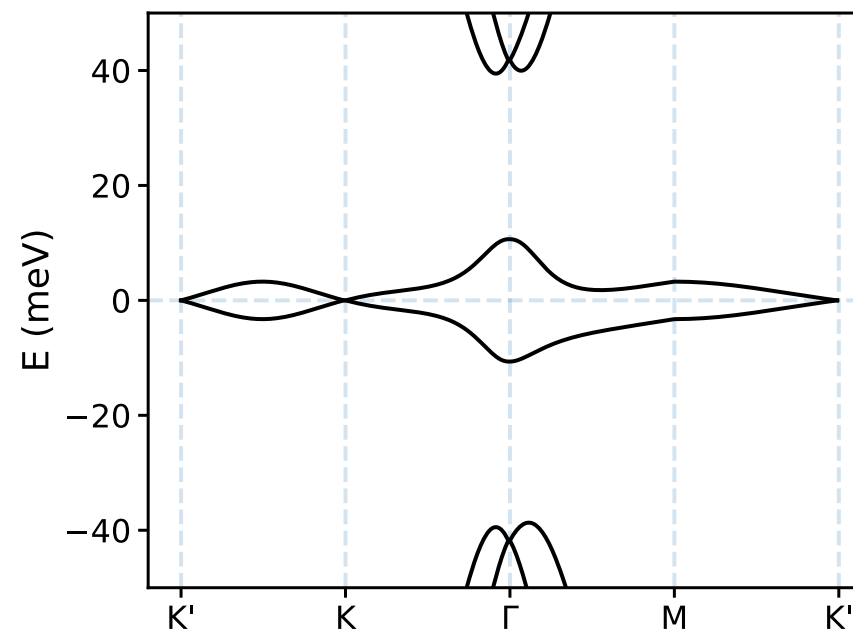
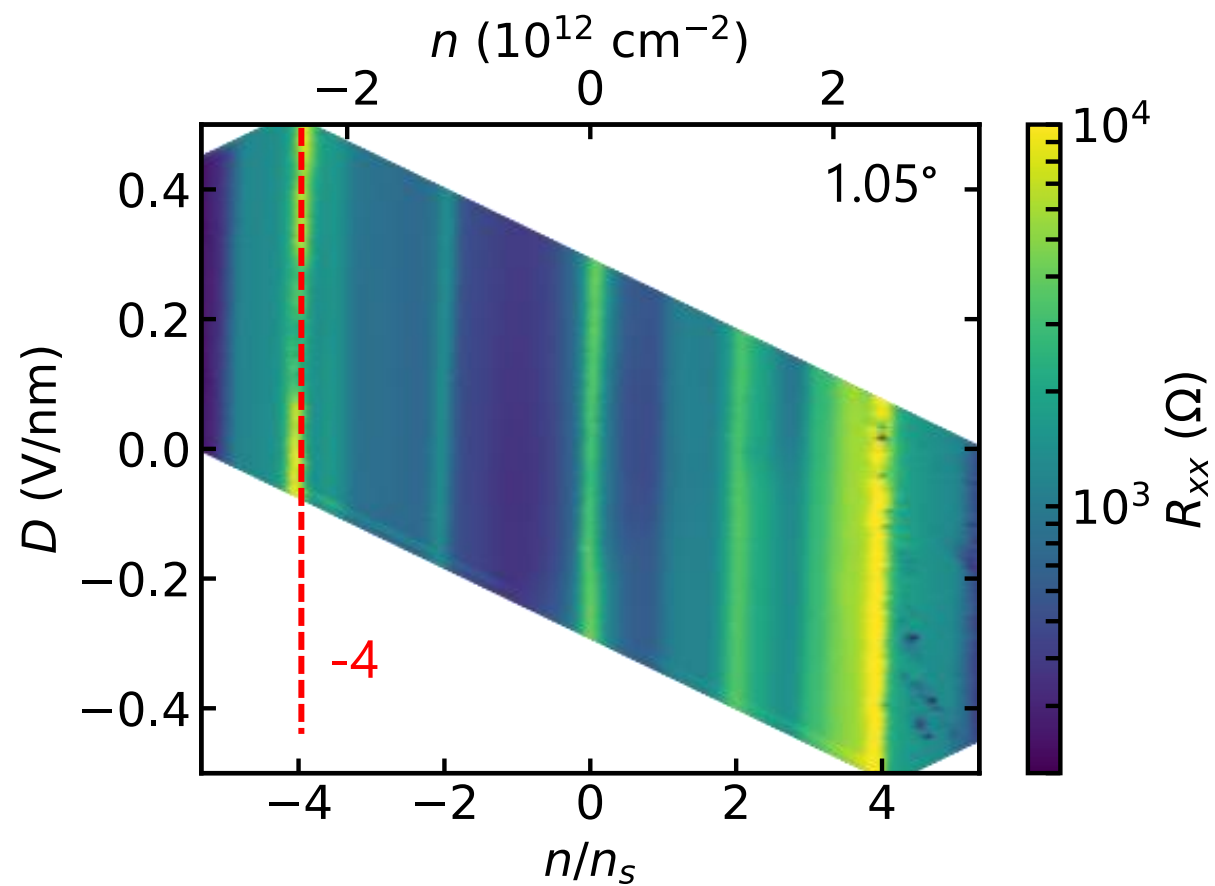
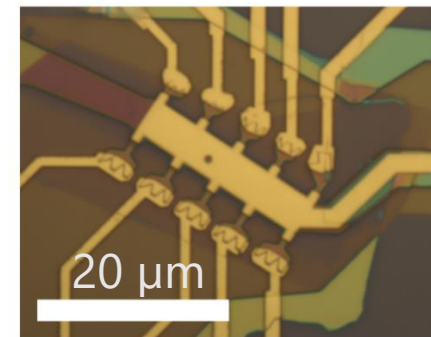
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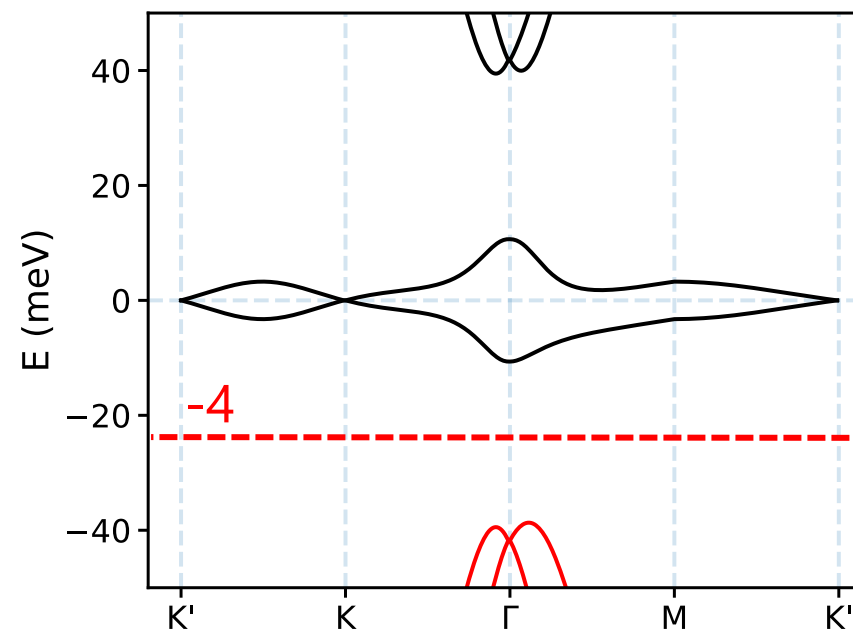
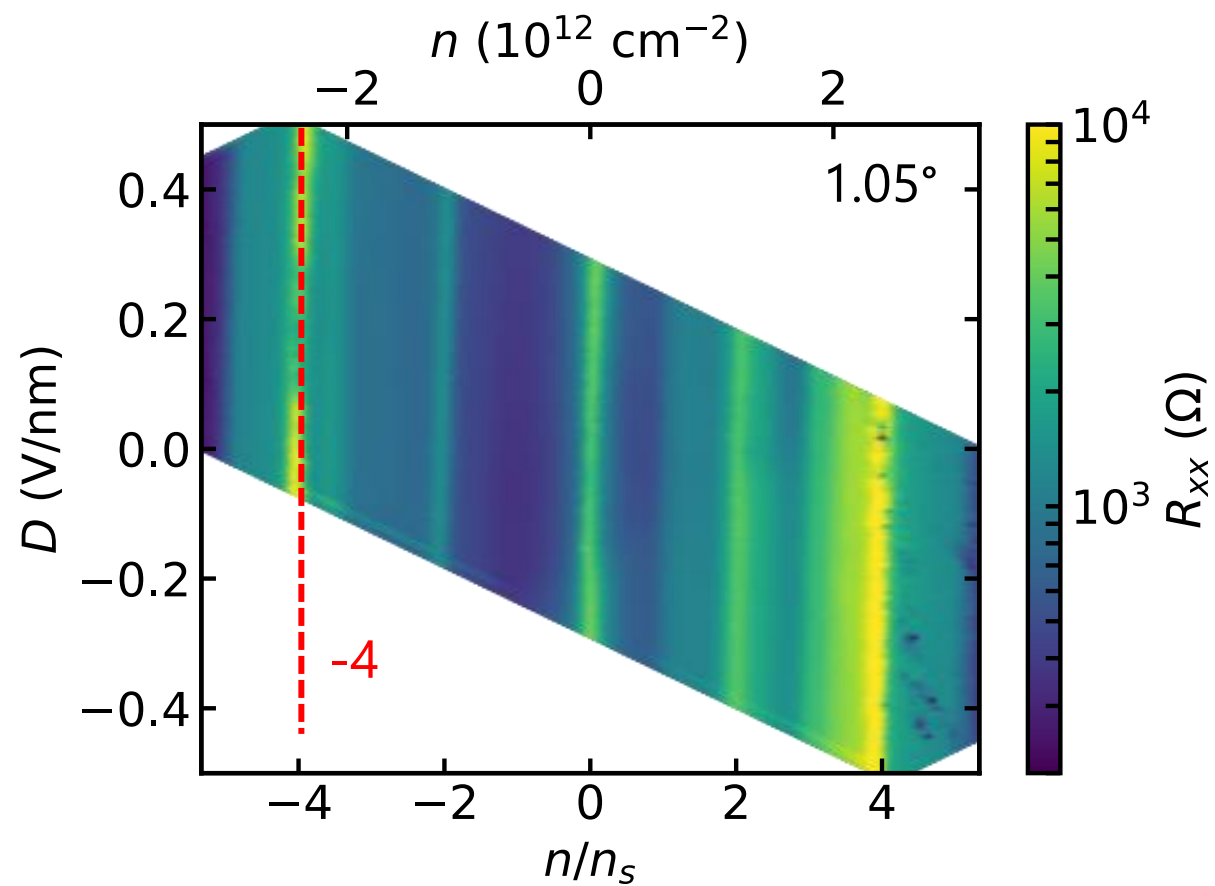
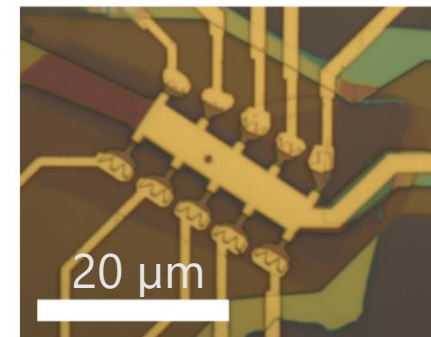
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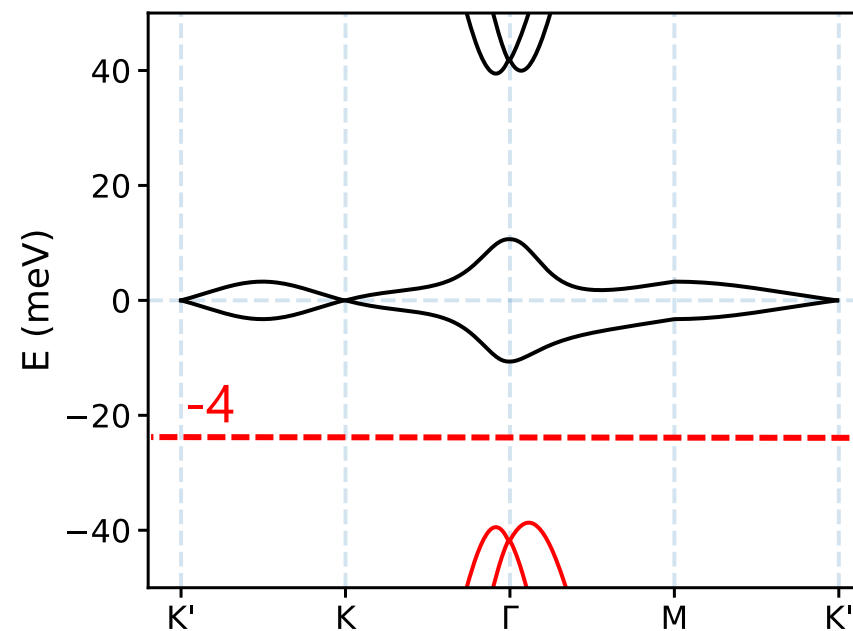
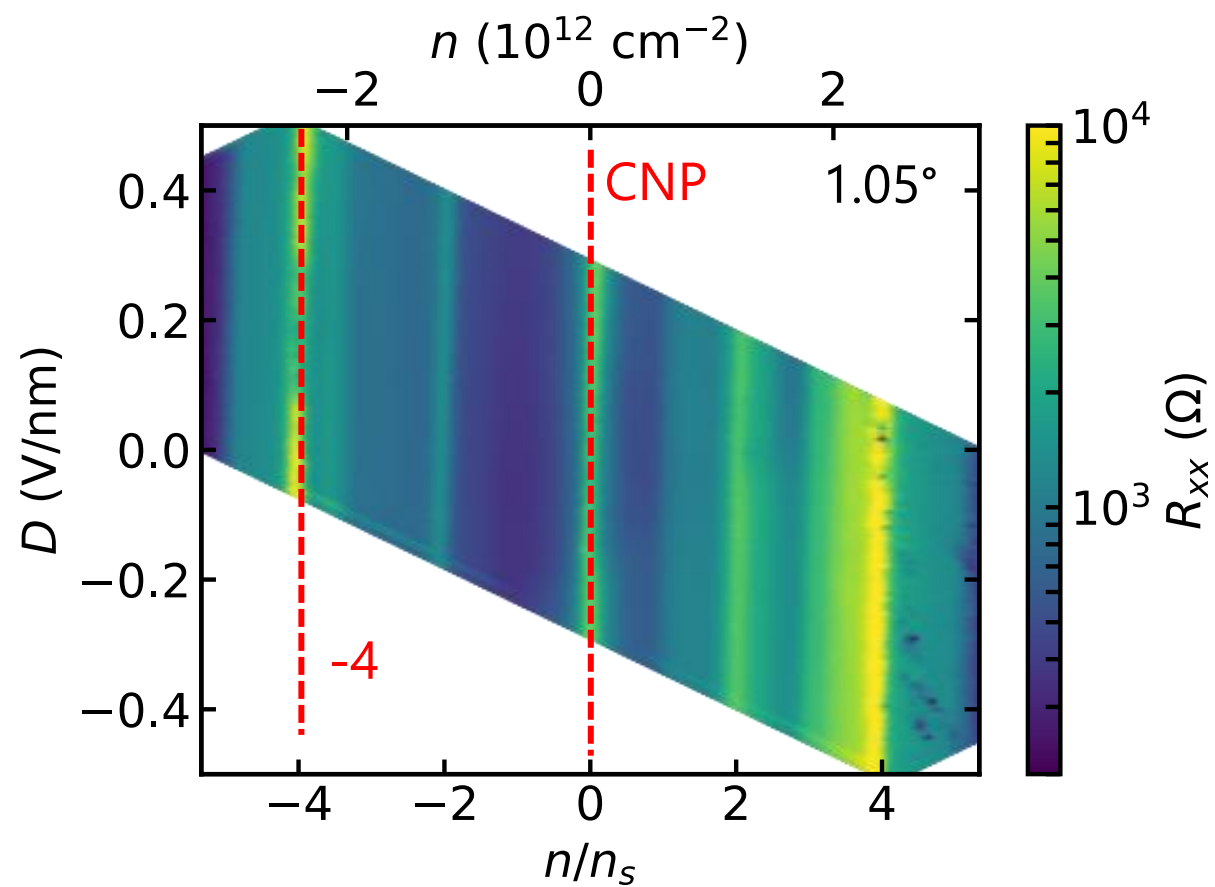
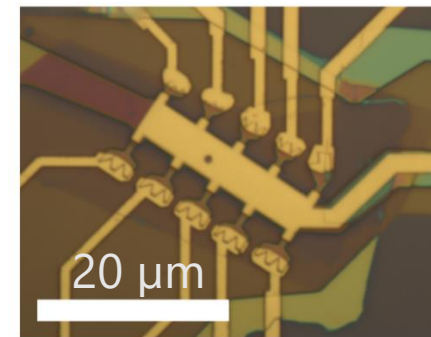
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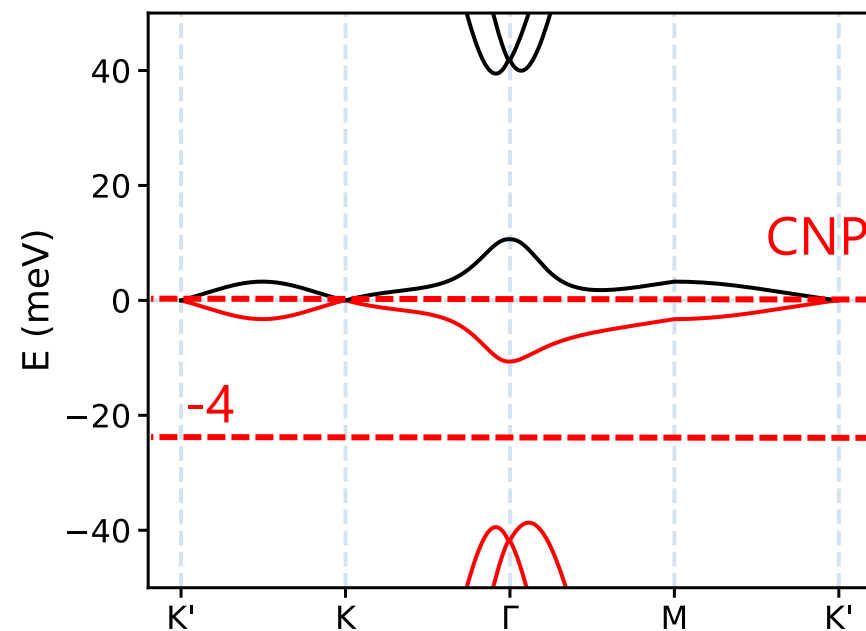
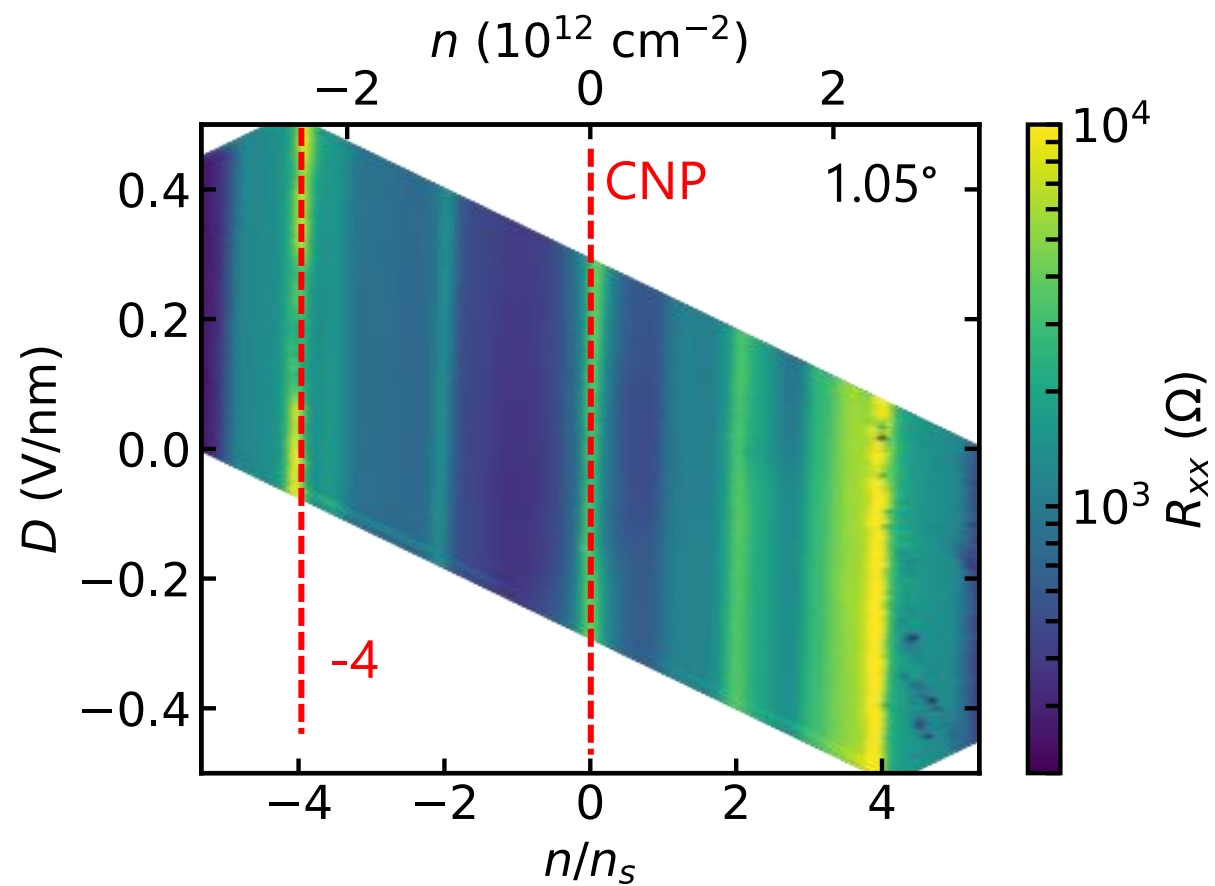
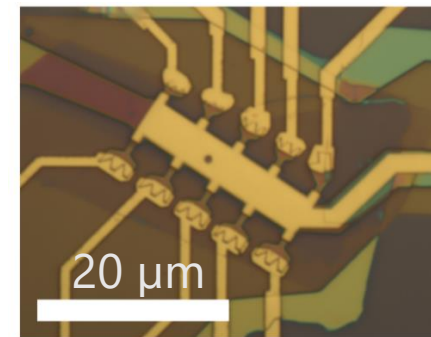
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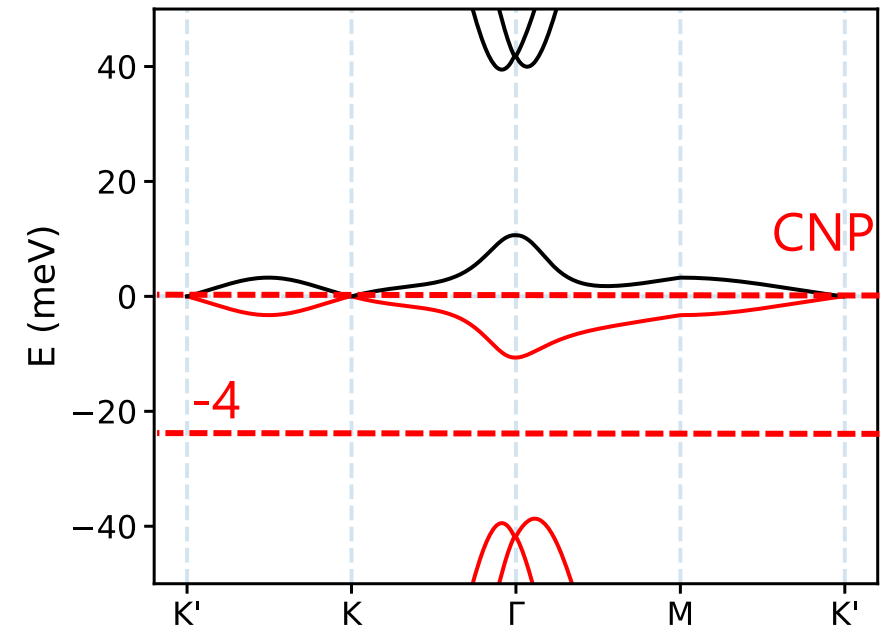
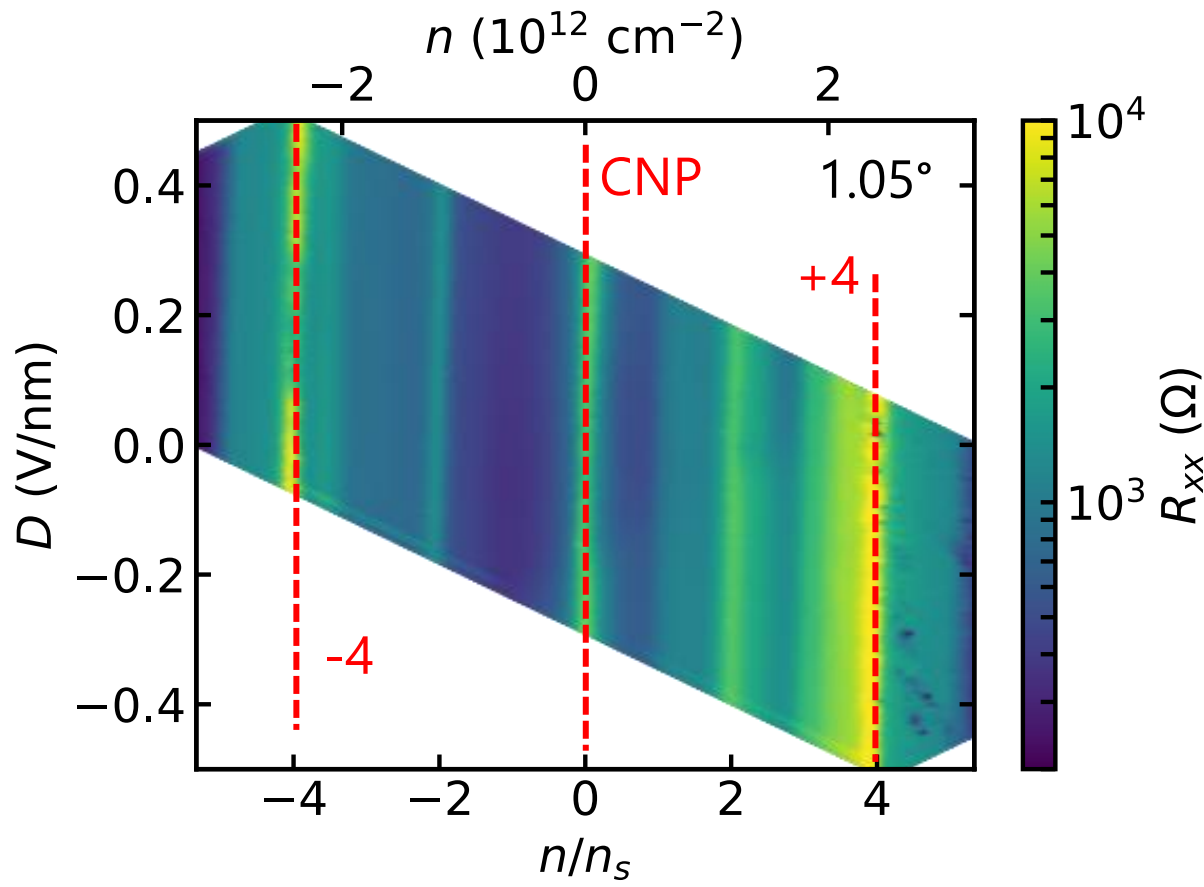
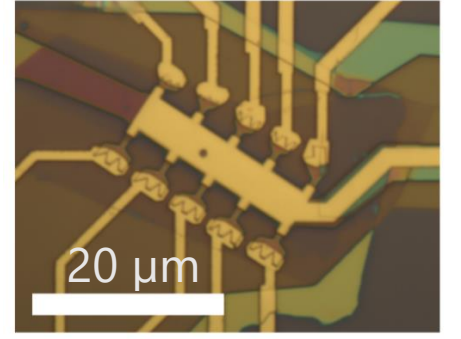
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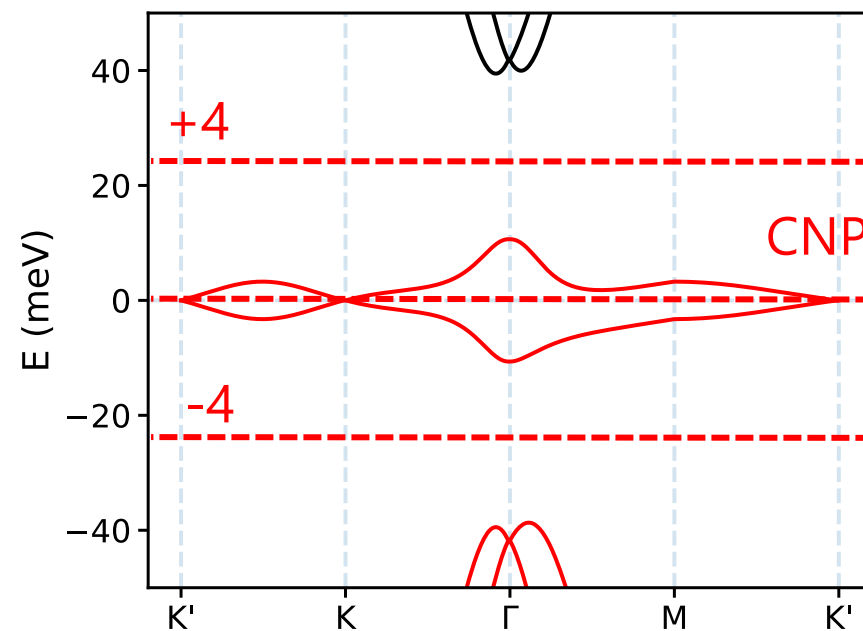
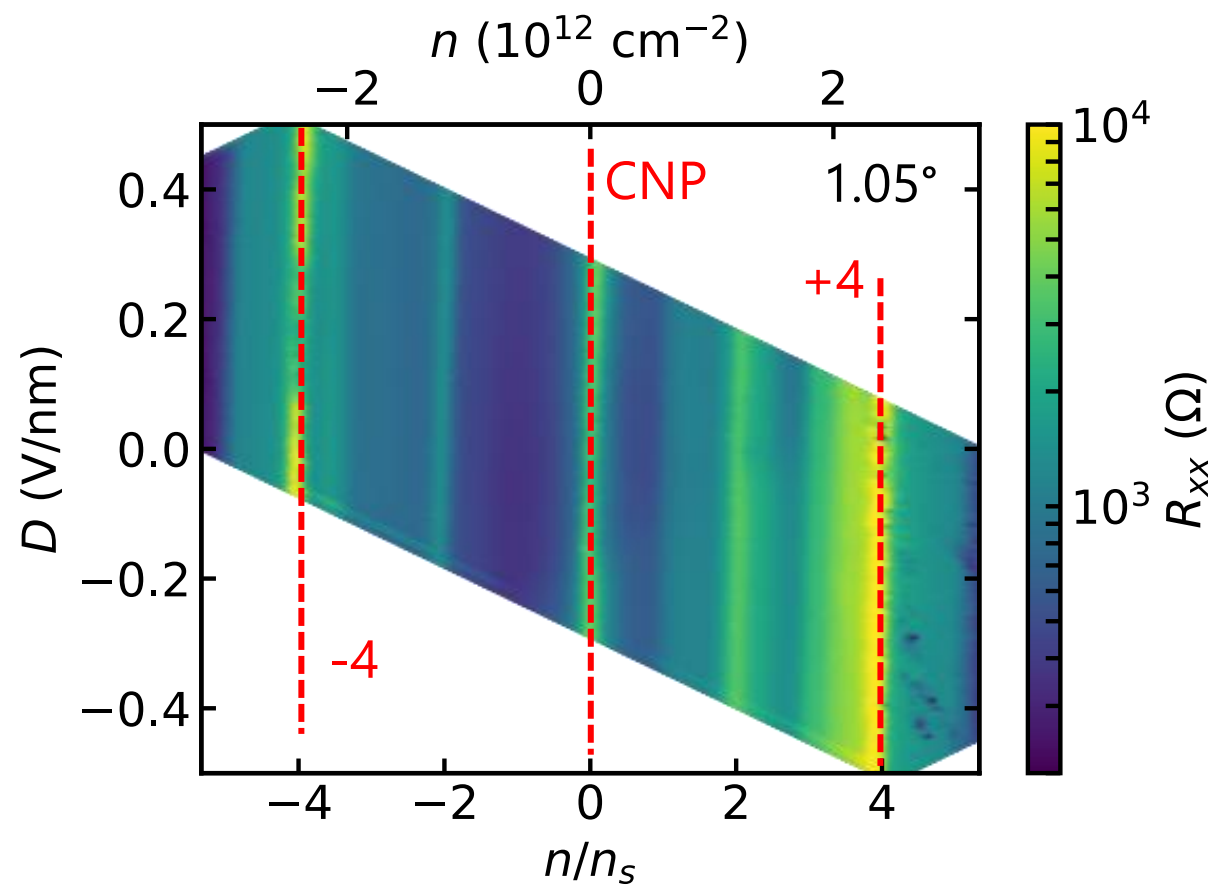
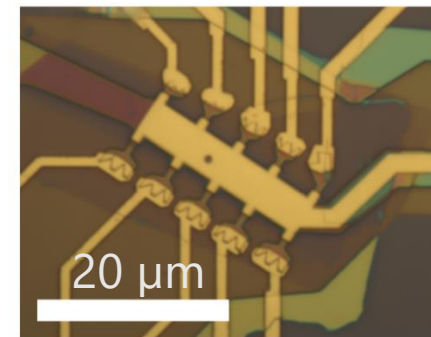
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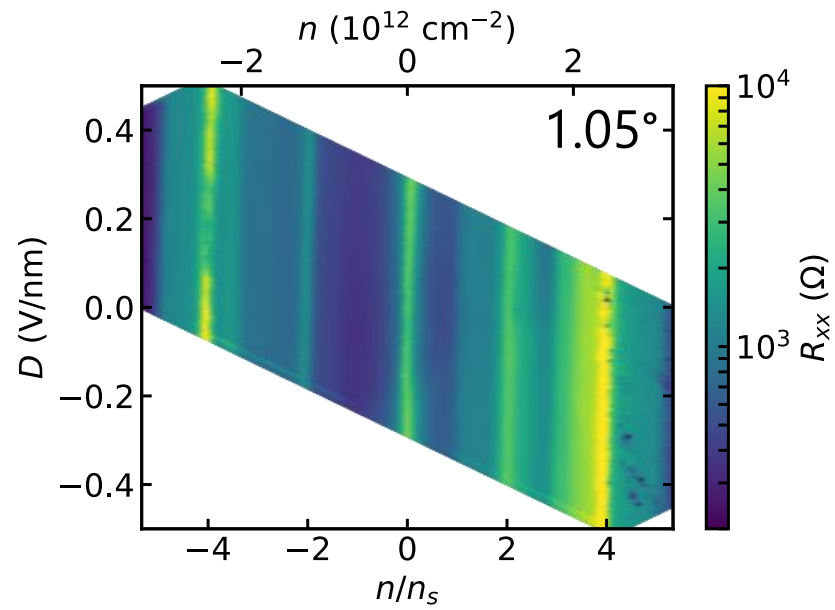
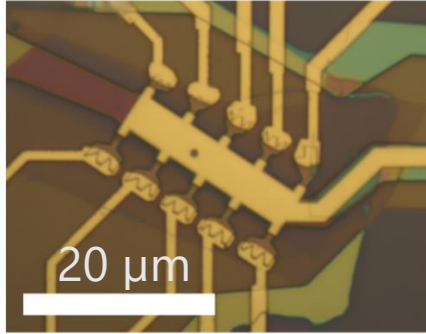
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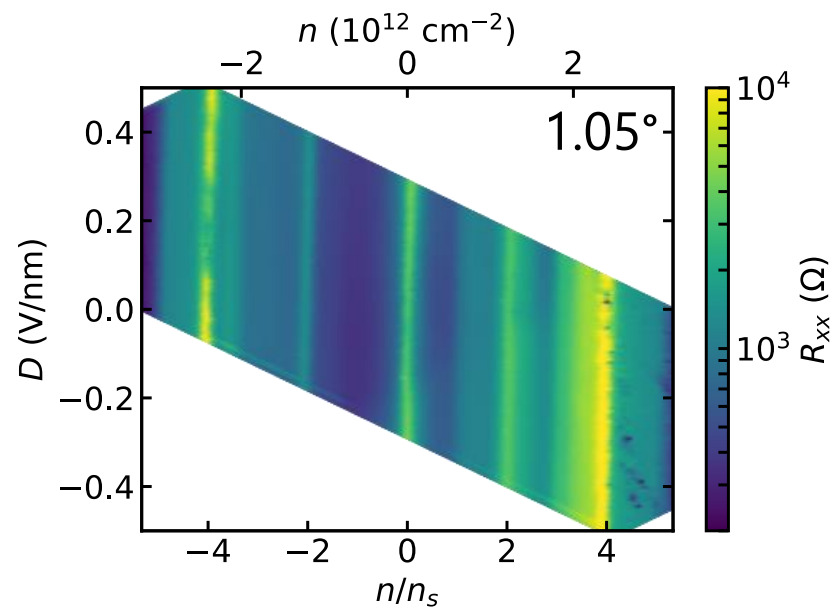
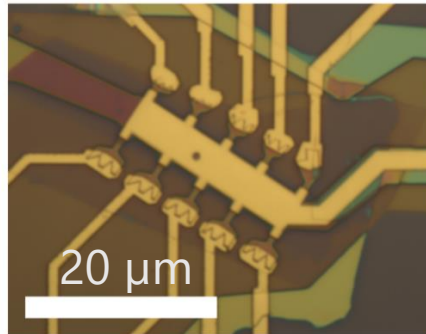


Typical TBG

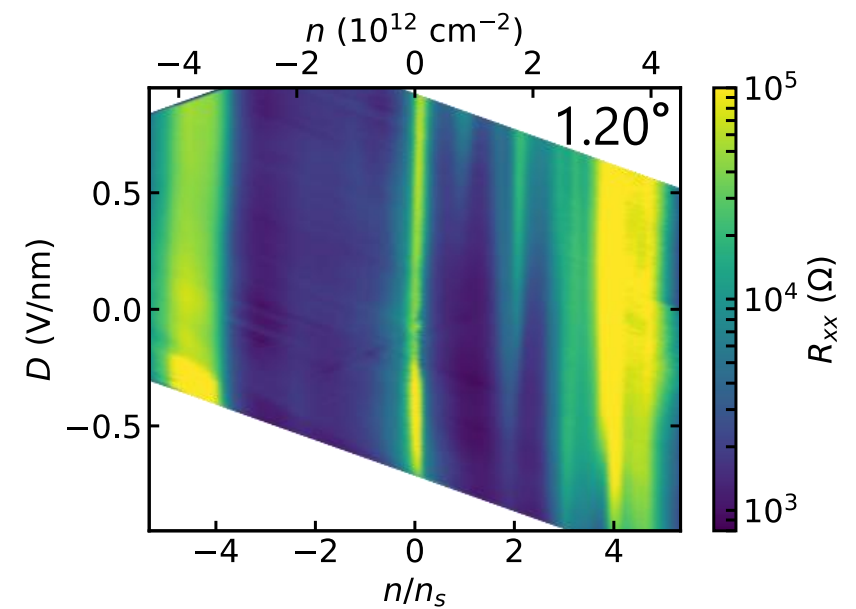
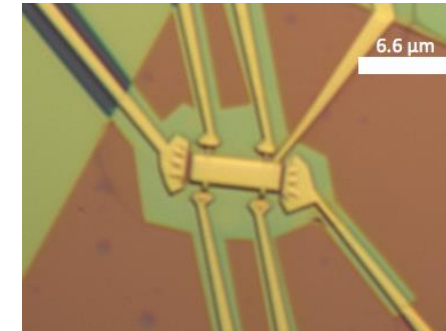


Atypical TBG

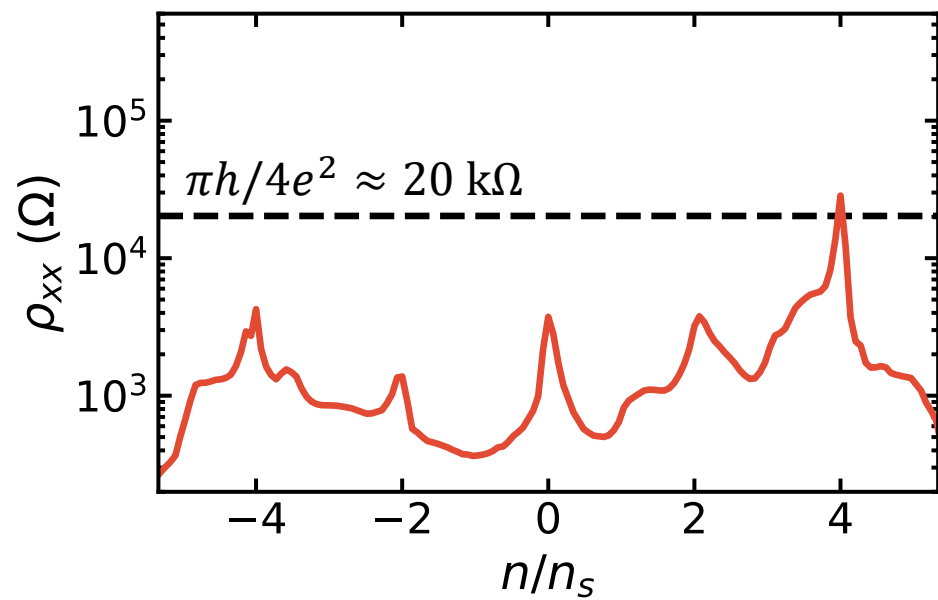
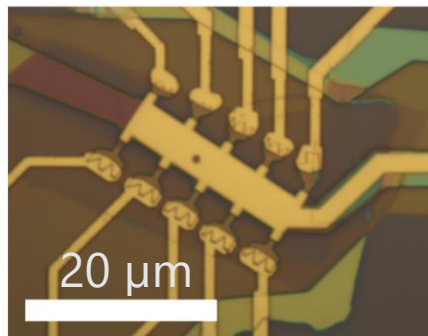
Typical TBG



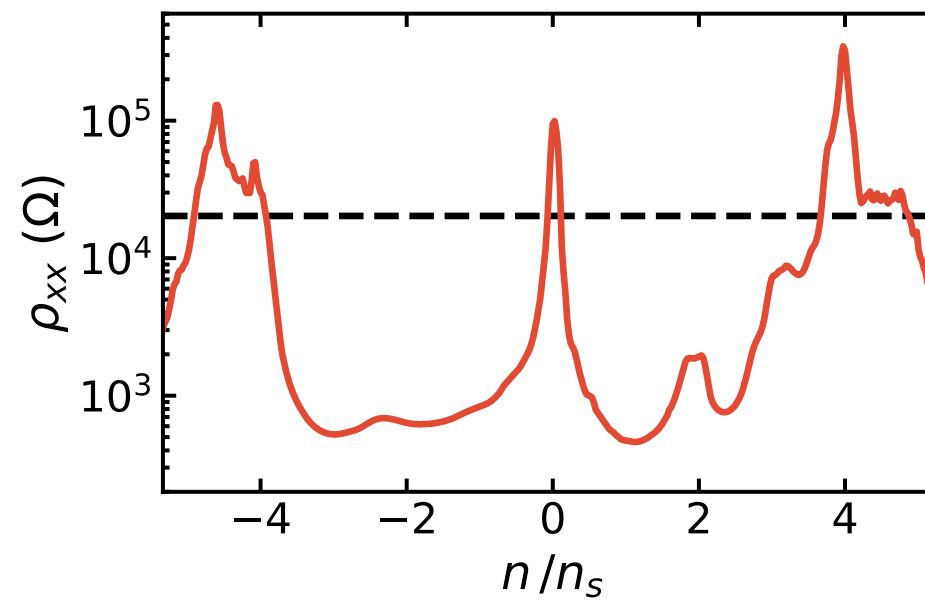
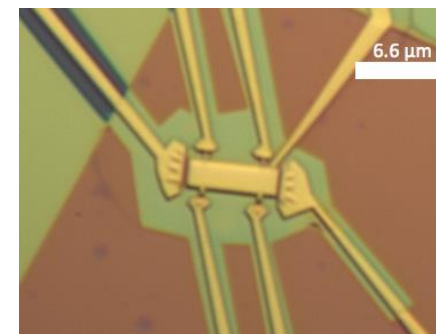
Atypical TBG



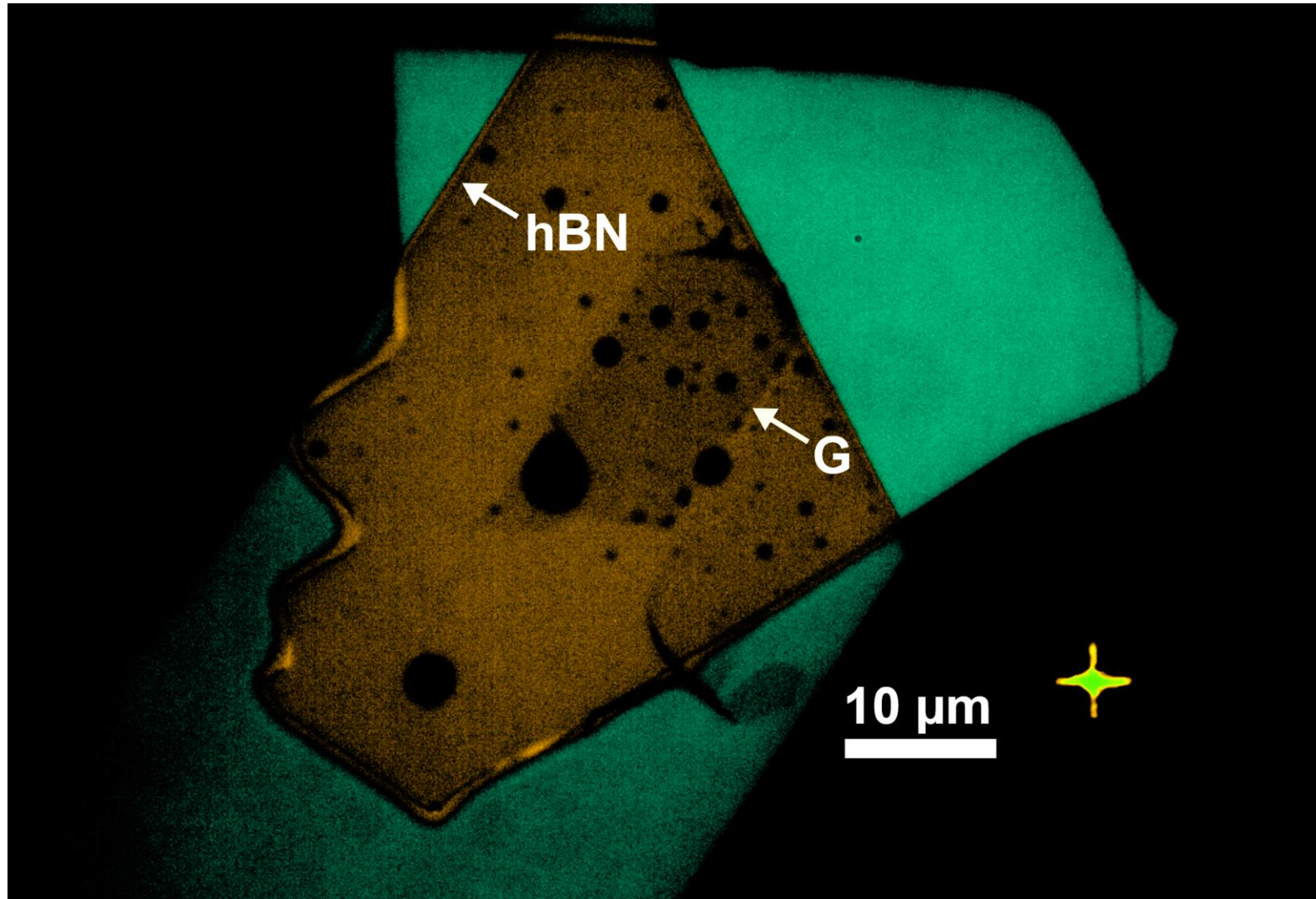
Typical TBG



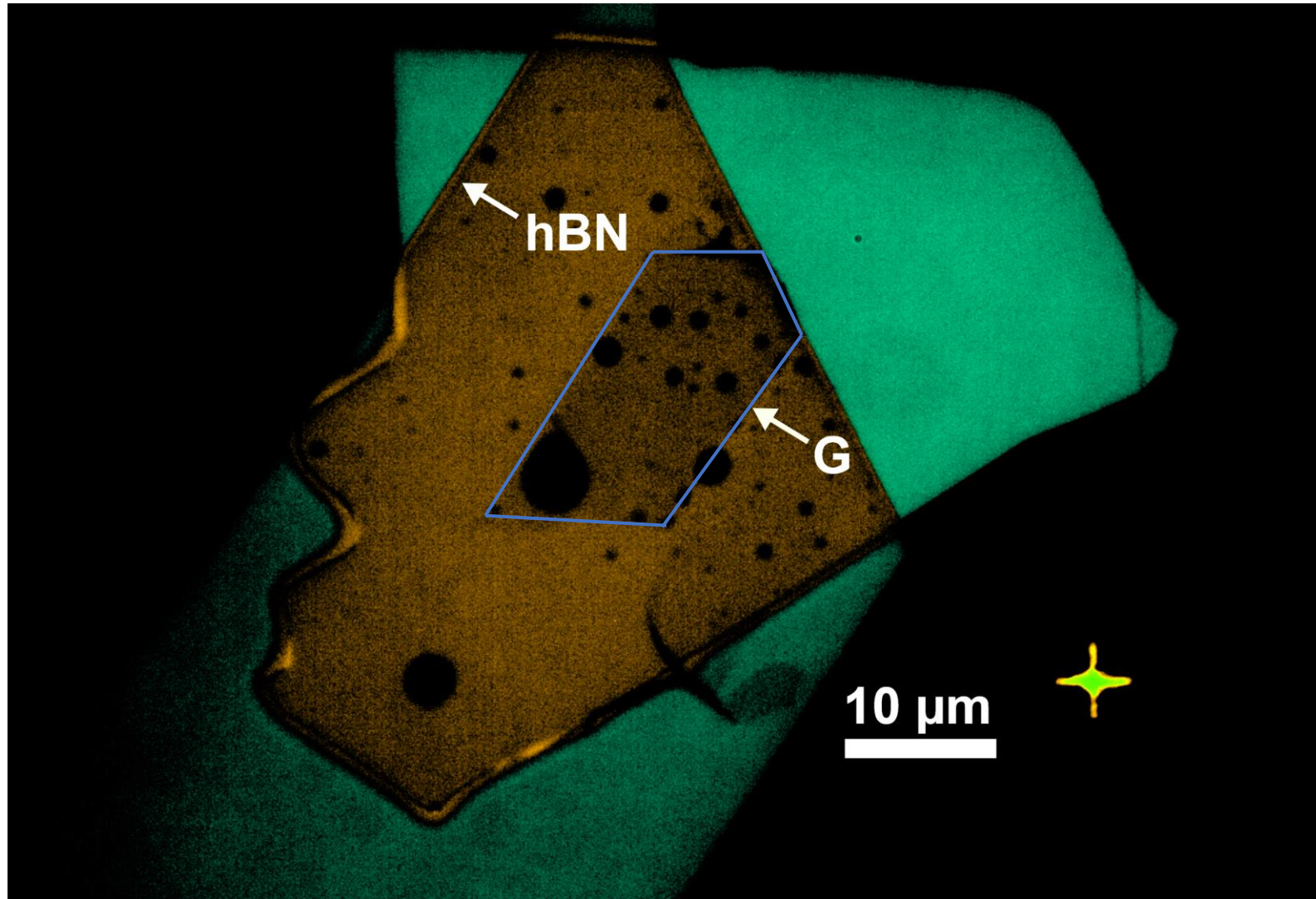
Atypical TBG



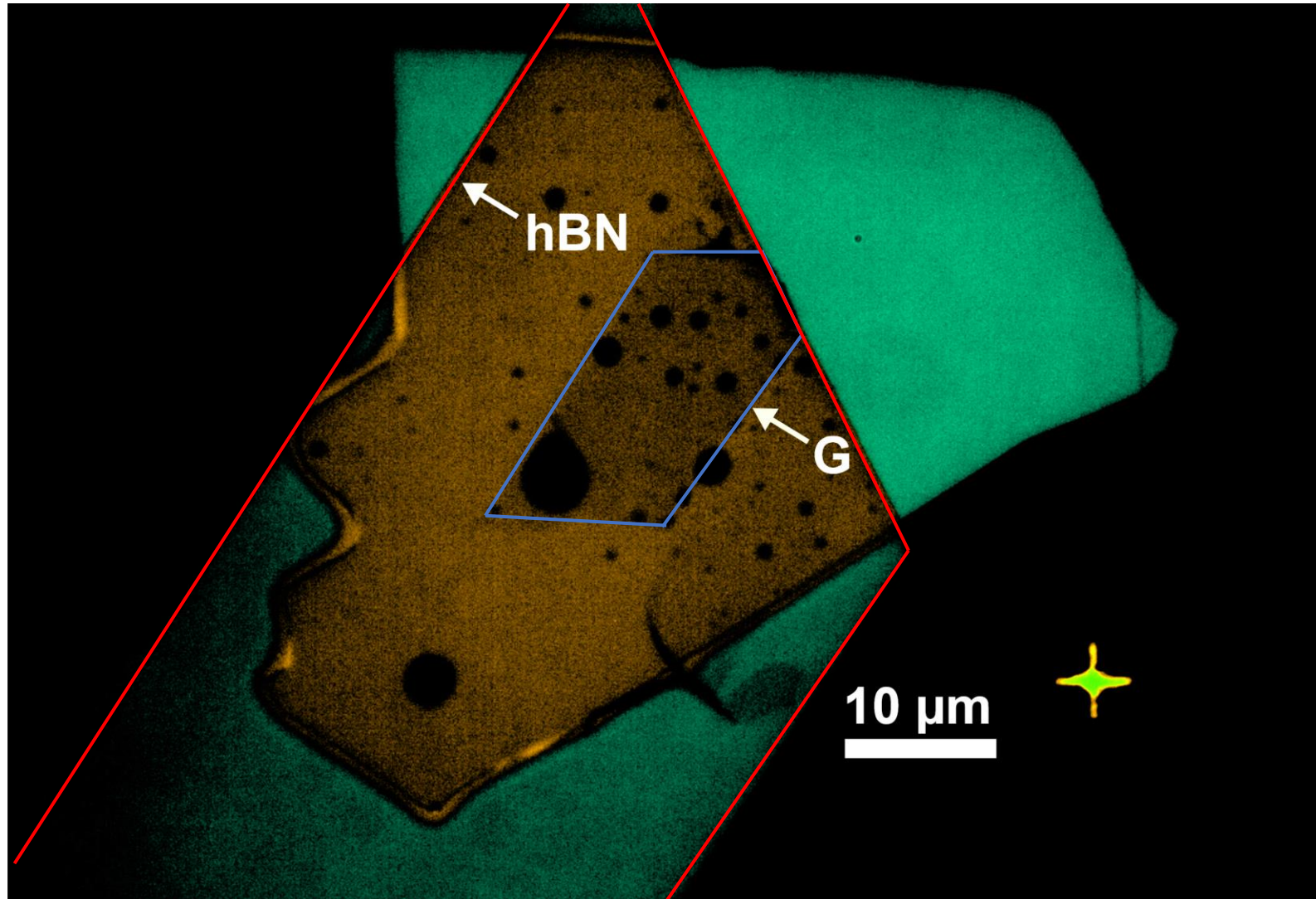
Visual hBN alignment



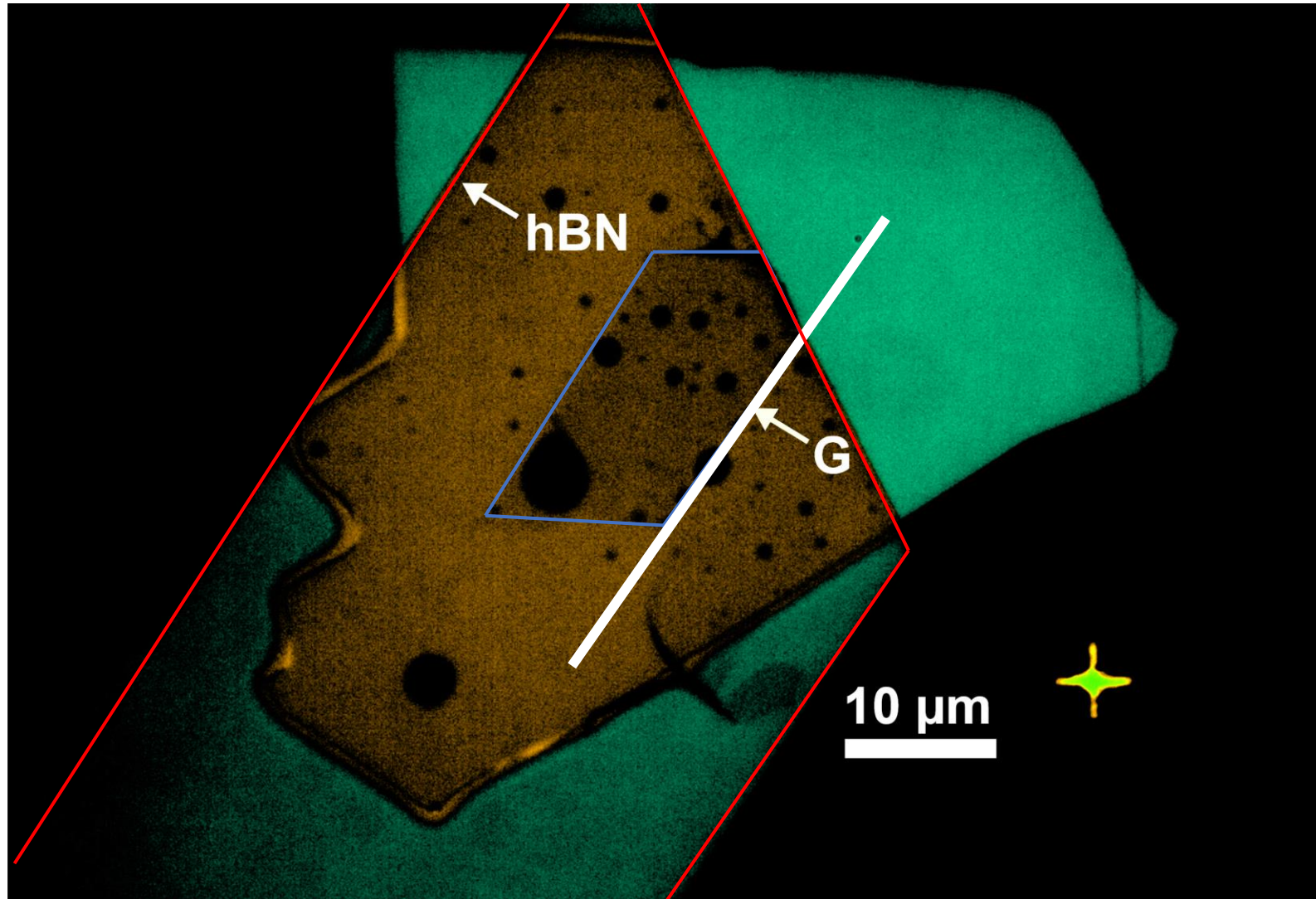
Visual hBN alignment



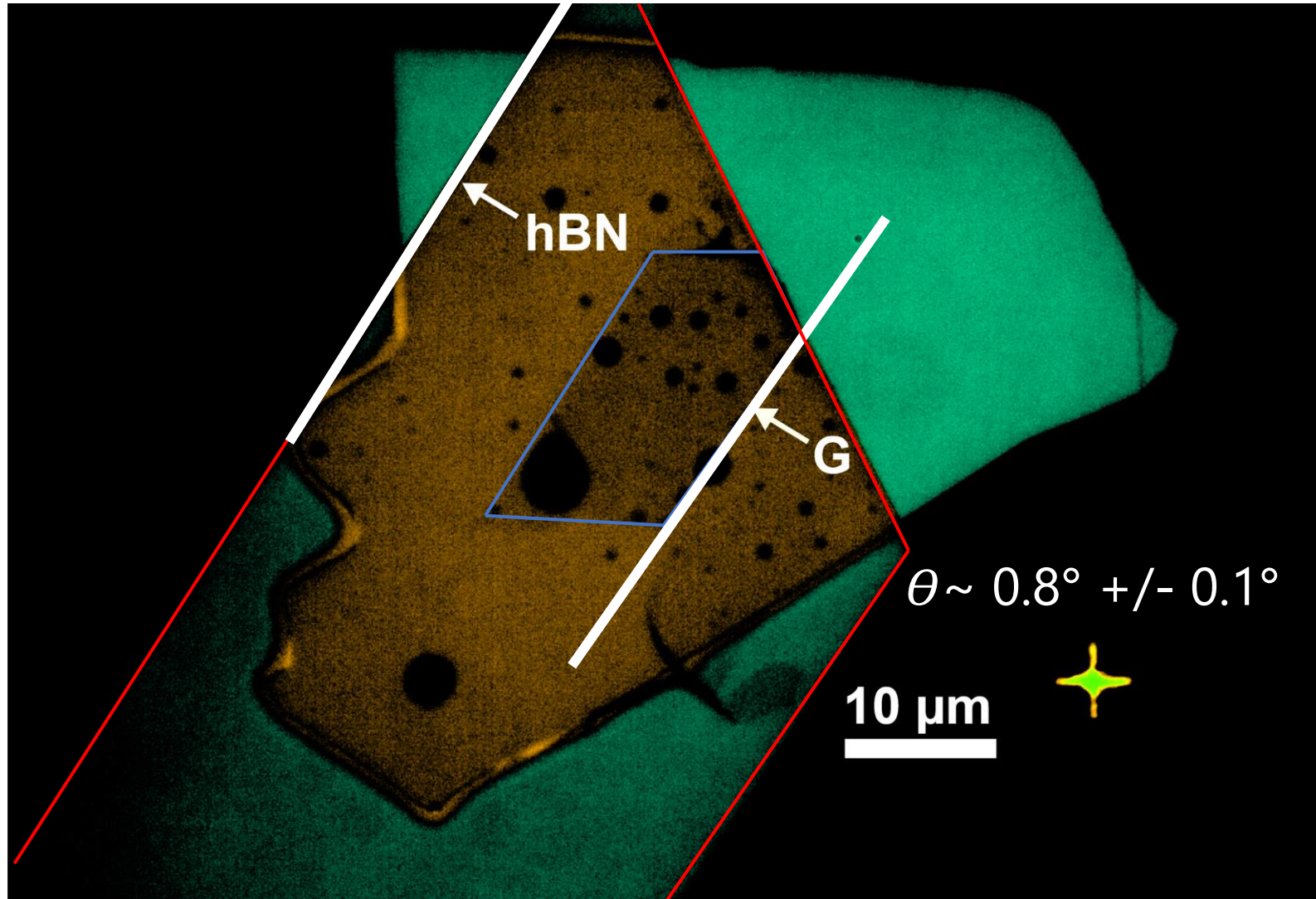
Visual hBN alignment



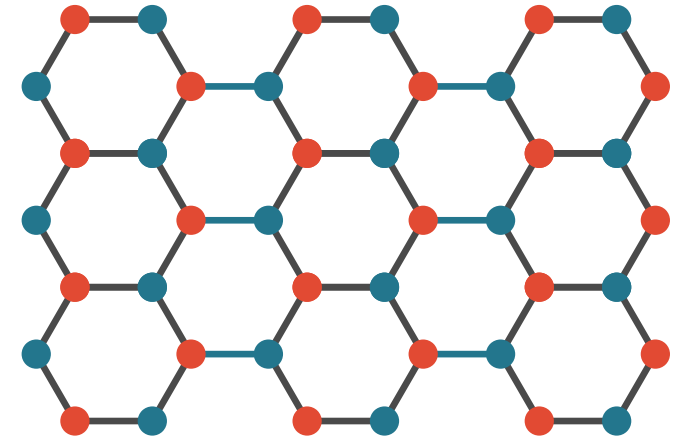
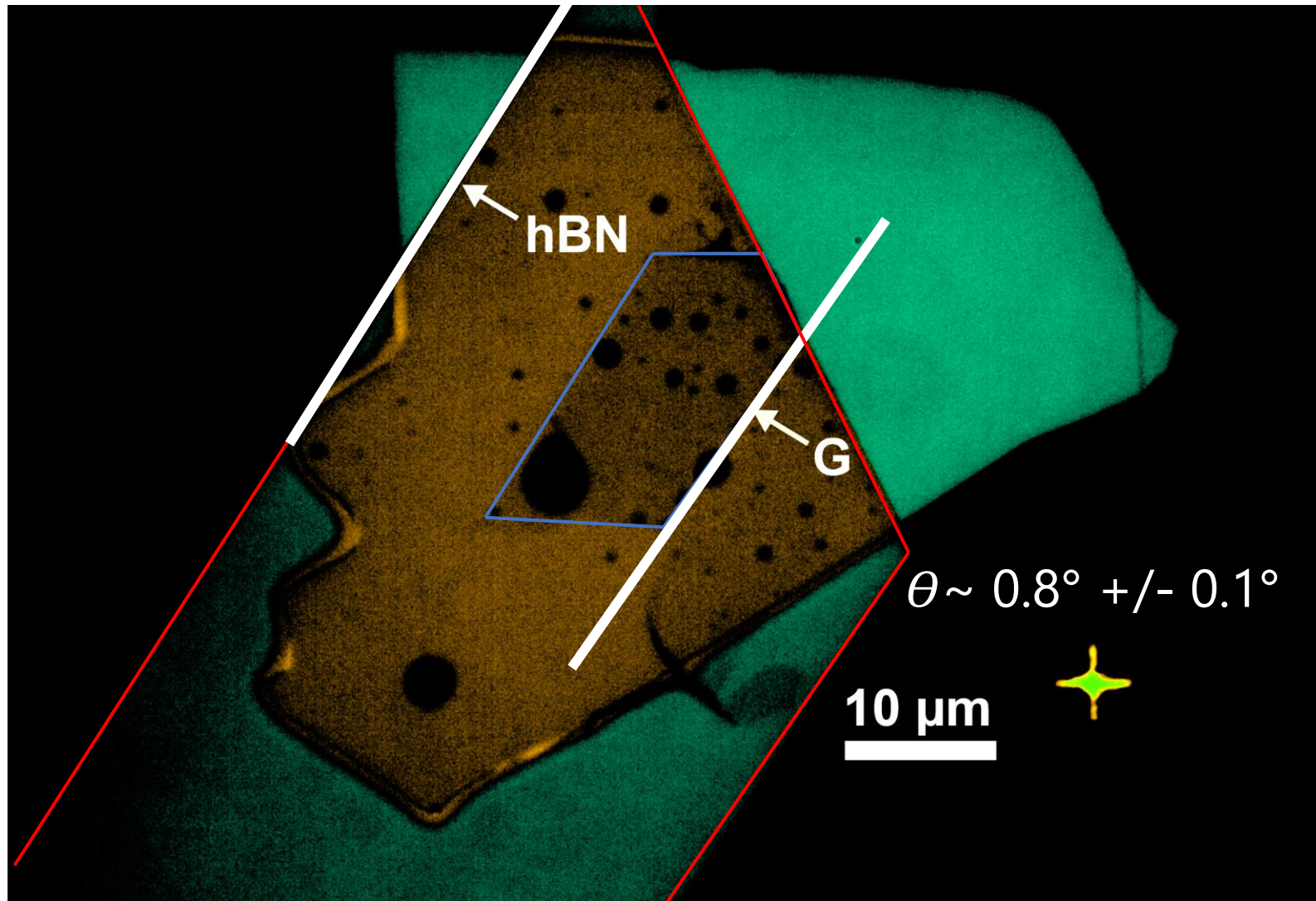
Visual hBN alignment



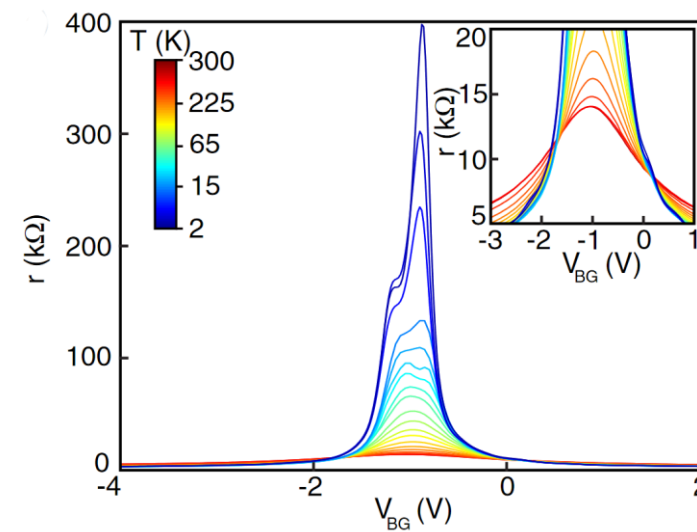
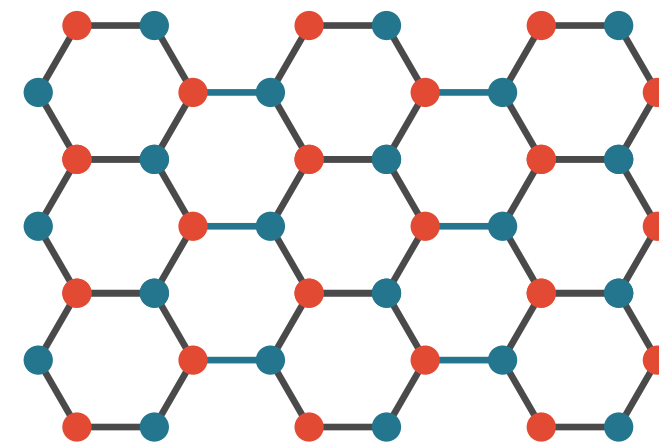
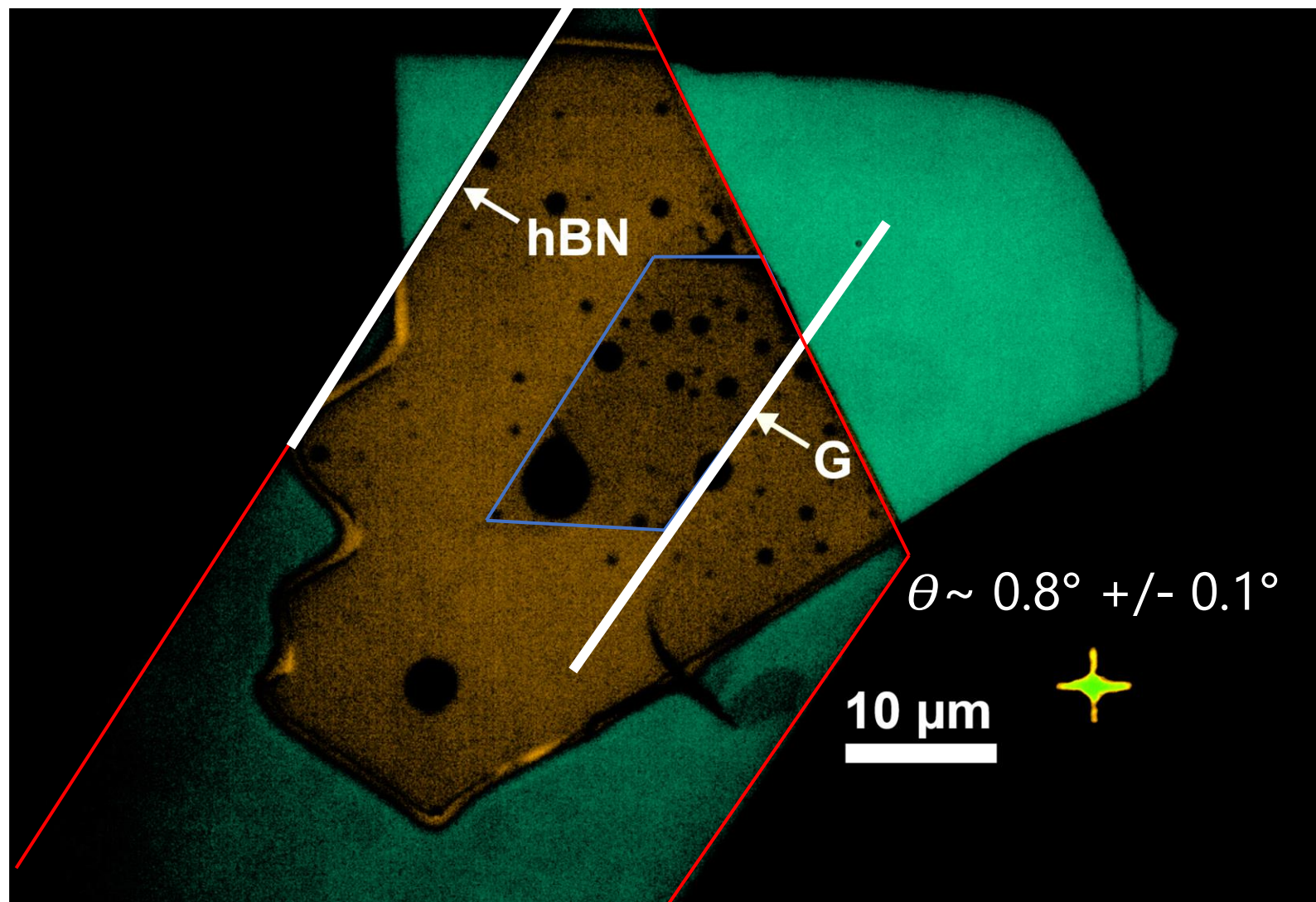
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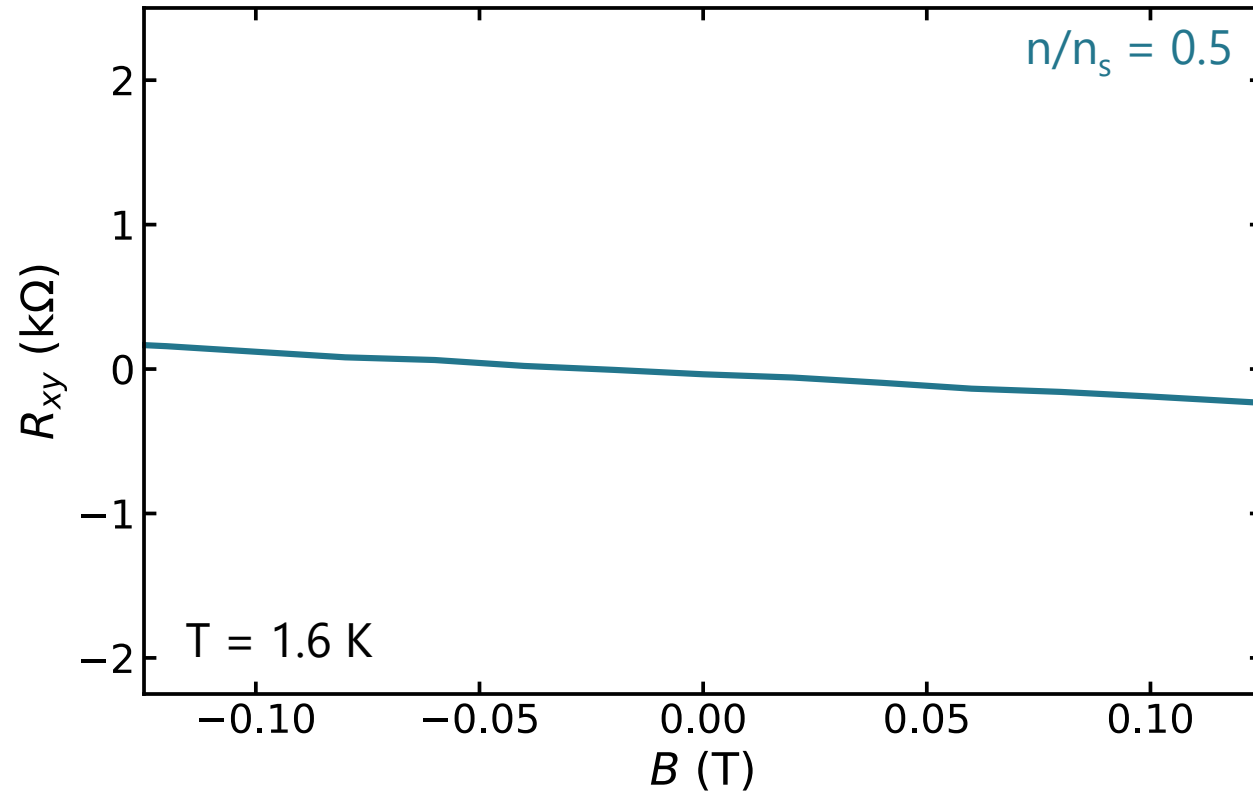
Visual hBN alignment



Visual hBN alignment

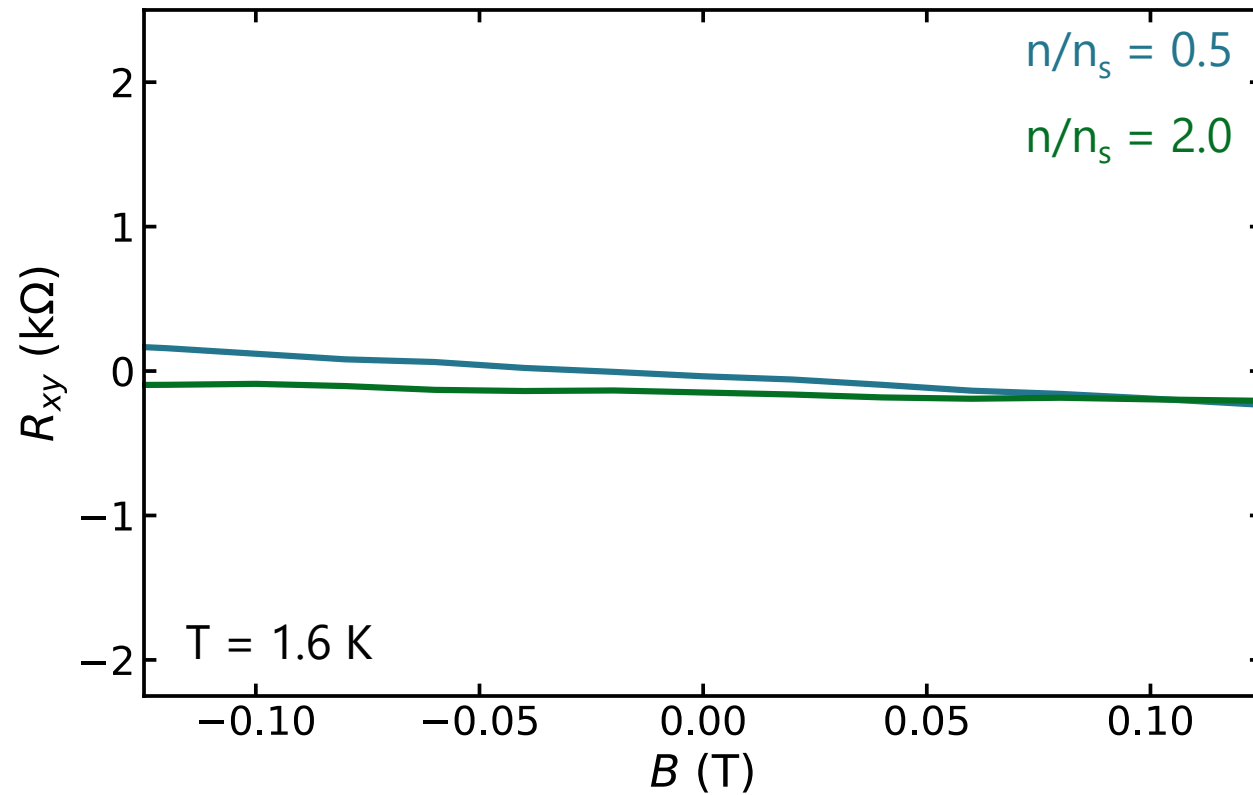


Hall slope density dependence



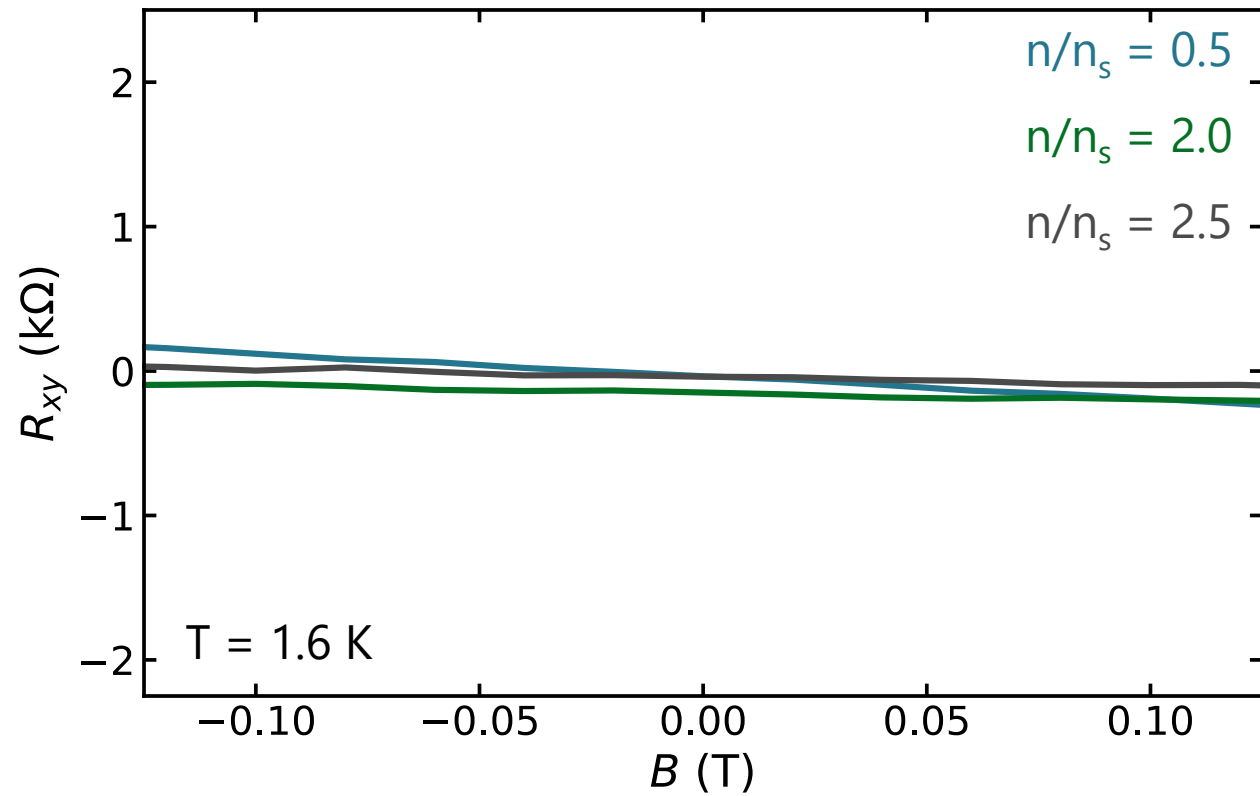
Classical Hall: $R_{xy} = \frac{V_H}{I} = -\frac{B}{ne}$

Hall slope density dependence



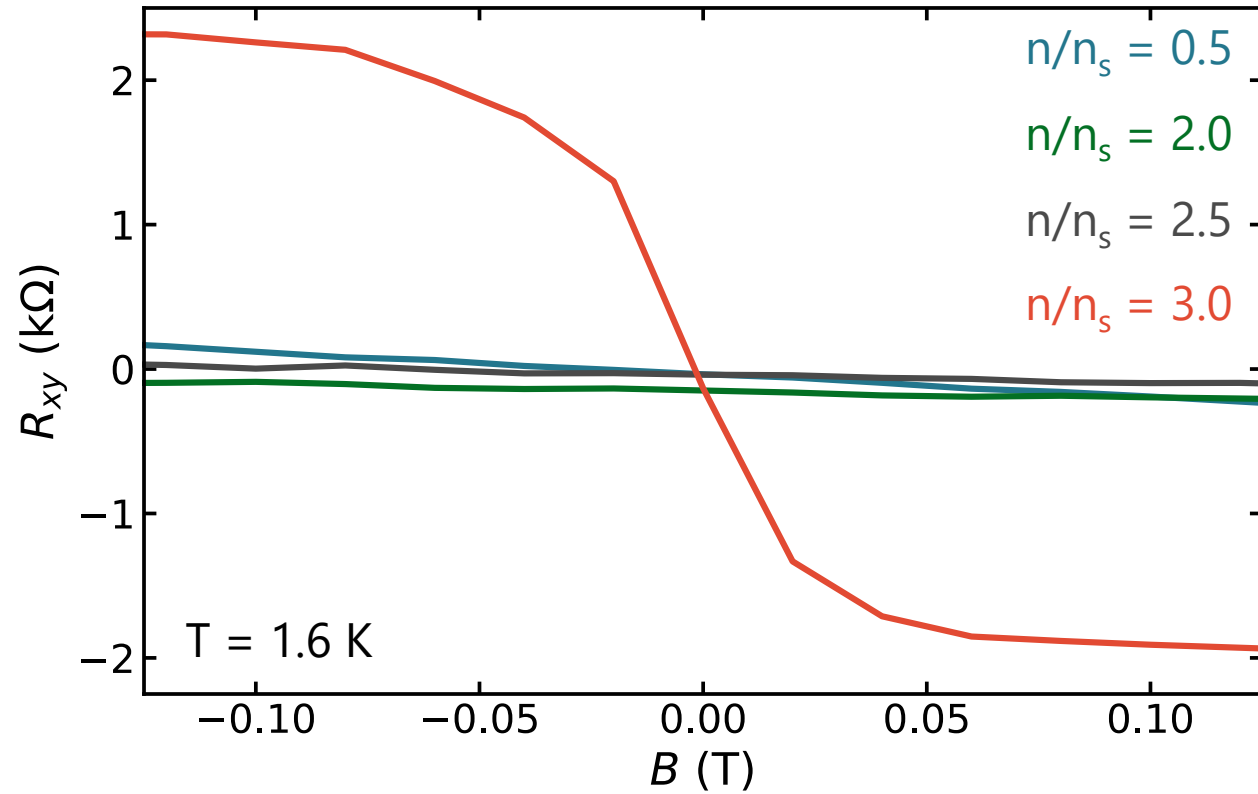
Classical Hall: $R_{xy} = \frac{V_H}{I} = -\frac{B}{ne}$

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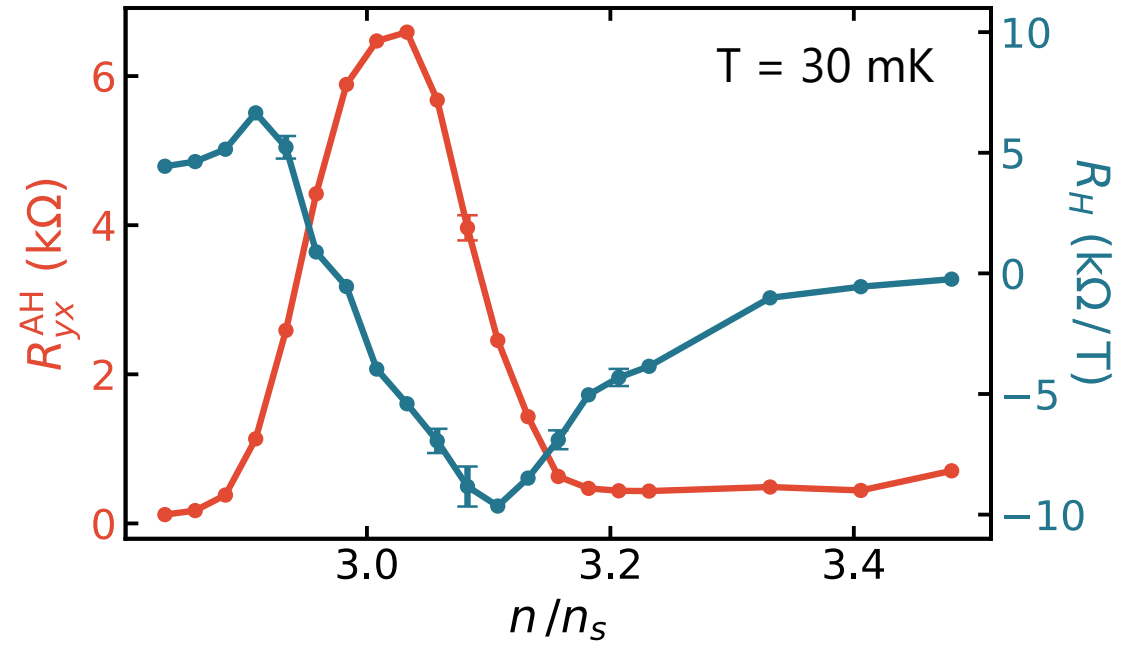
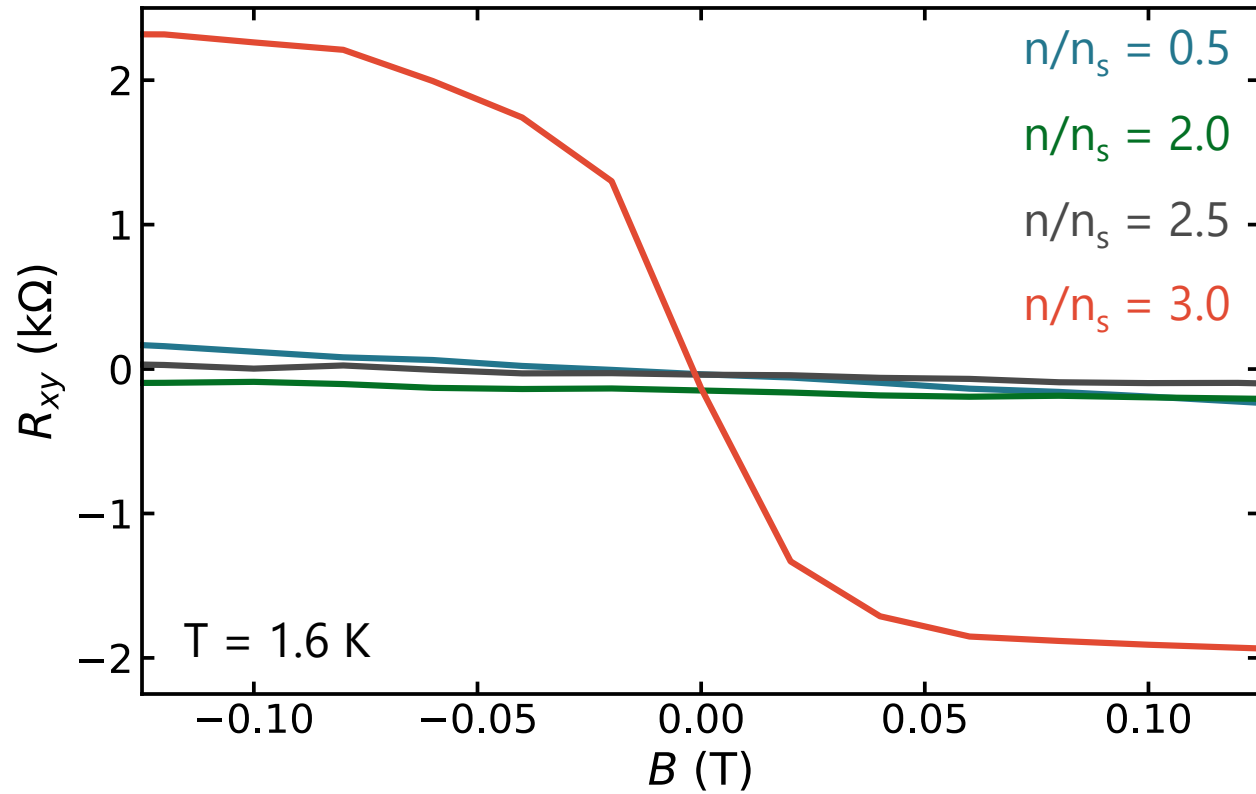
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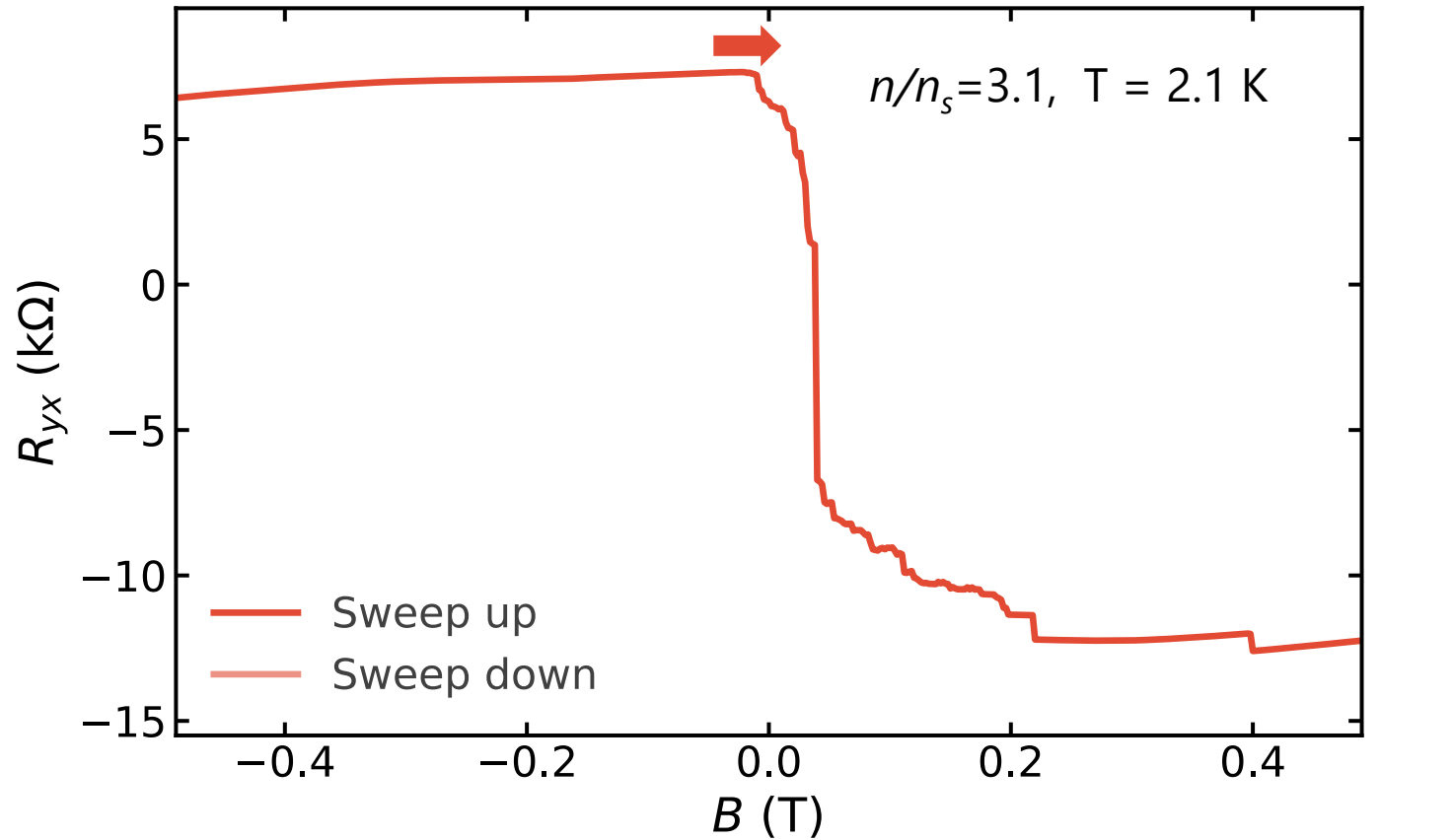
Classical Hall: $R_{xy} = \frac{V_H}{I} = -\frac{B}{ne}$

Hall slope density dependence



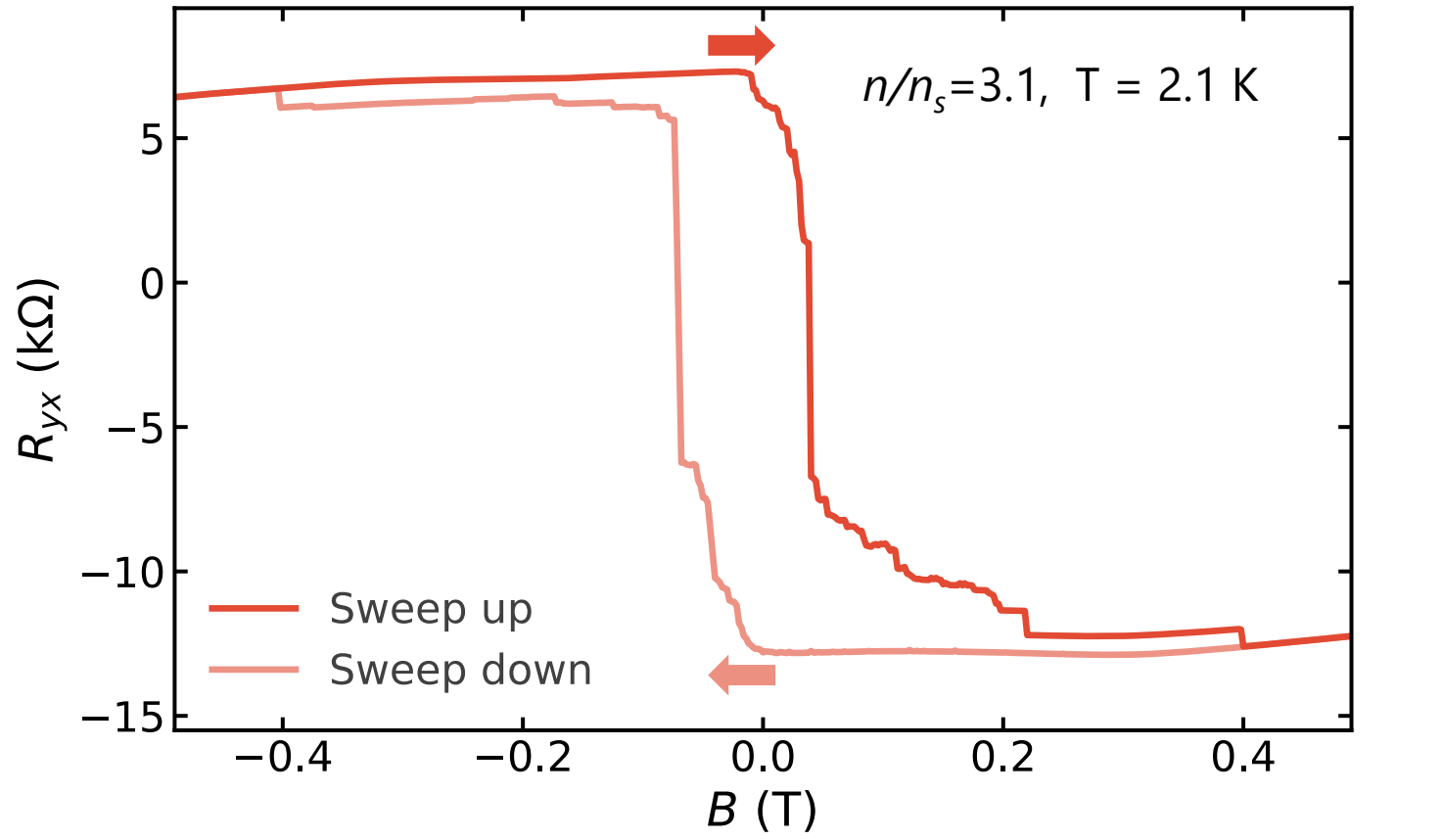
$$\text{Classical Hall: } R_{xy} = \frac{V_H}{I} = -\frac{B}{ne}$$

Anomalous Hall signal can be really large!



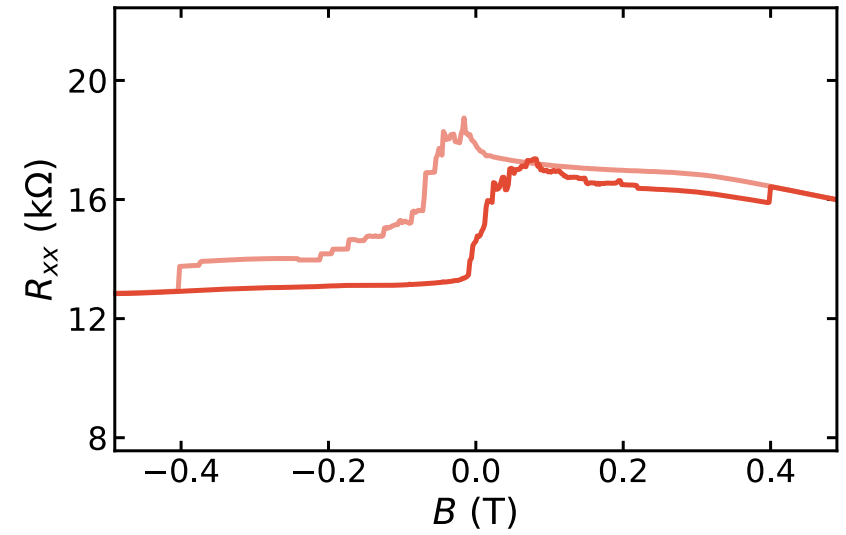
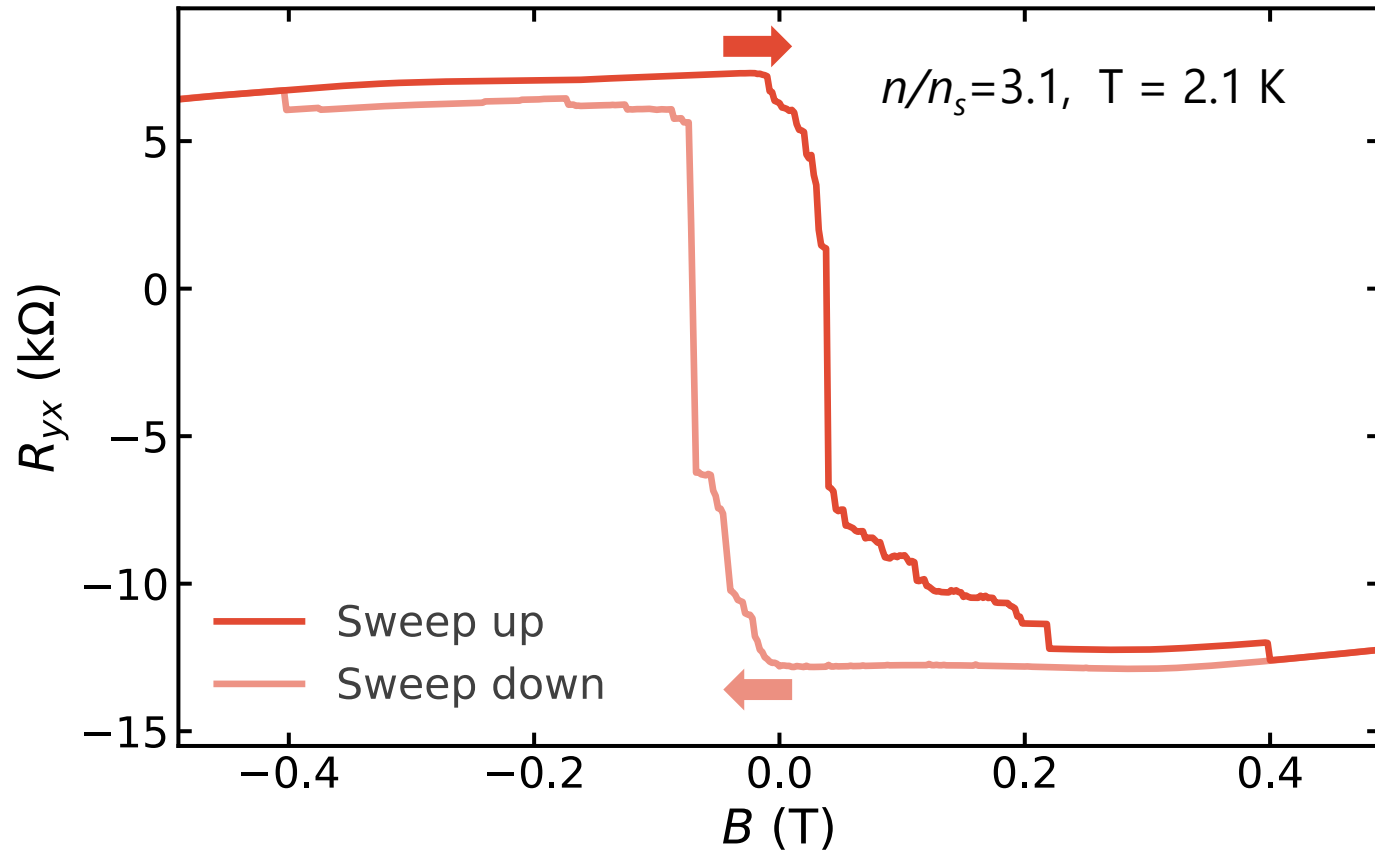
$$R_q = h/e^2 \approx 26 \text{ k}\Omega$$

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Summary

By controlling twist angle, graphene multilayers can become strongly correlated!

Large anomalous Hall (and R_{xx})

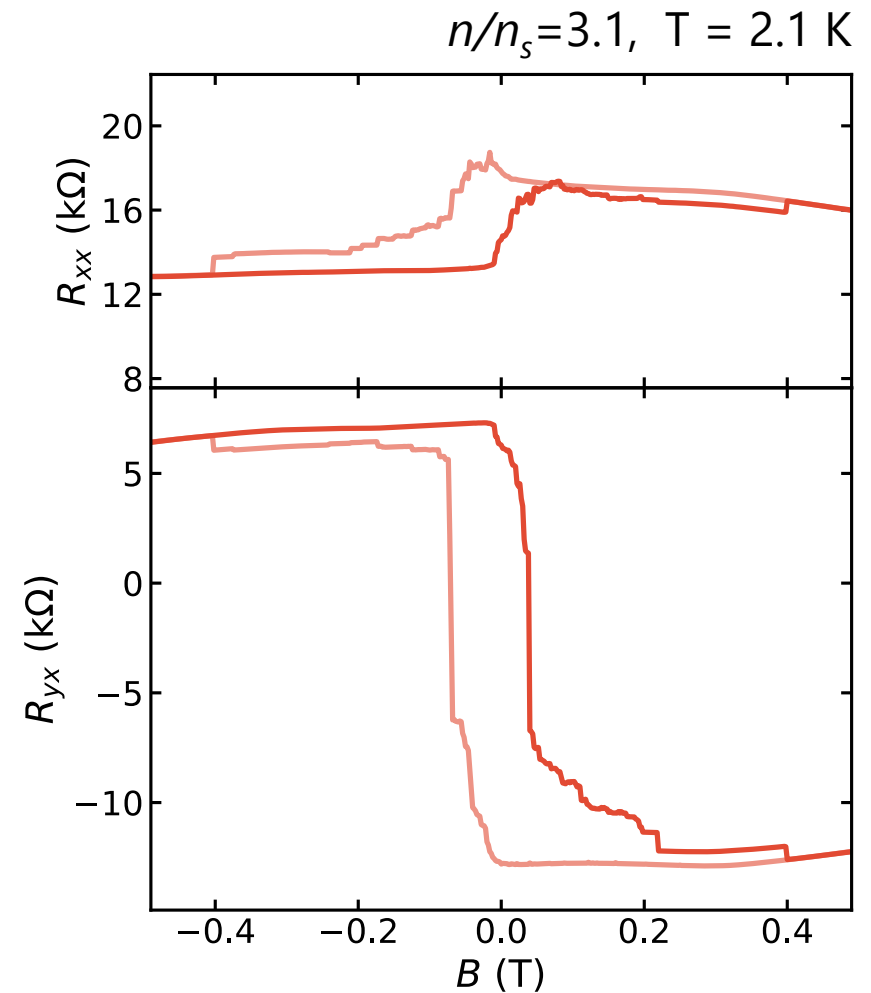
Apparent insulating state

Non-local transport

Survives up to $\sim 5\text{K}$

Evidence of domains

Reminiscent of early Magnetic Tis \rightarrow Chern insulator?



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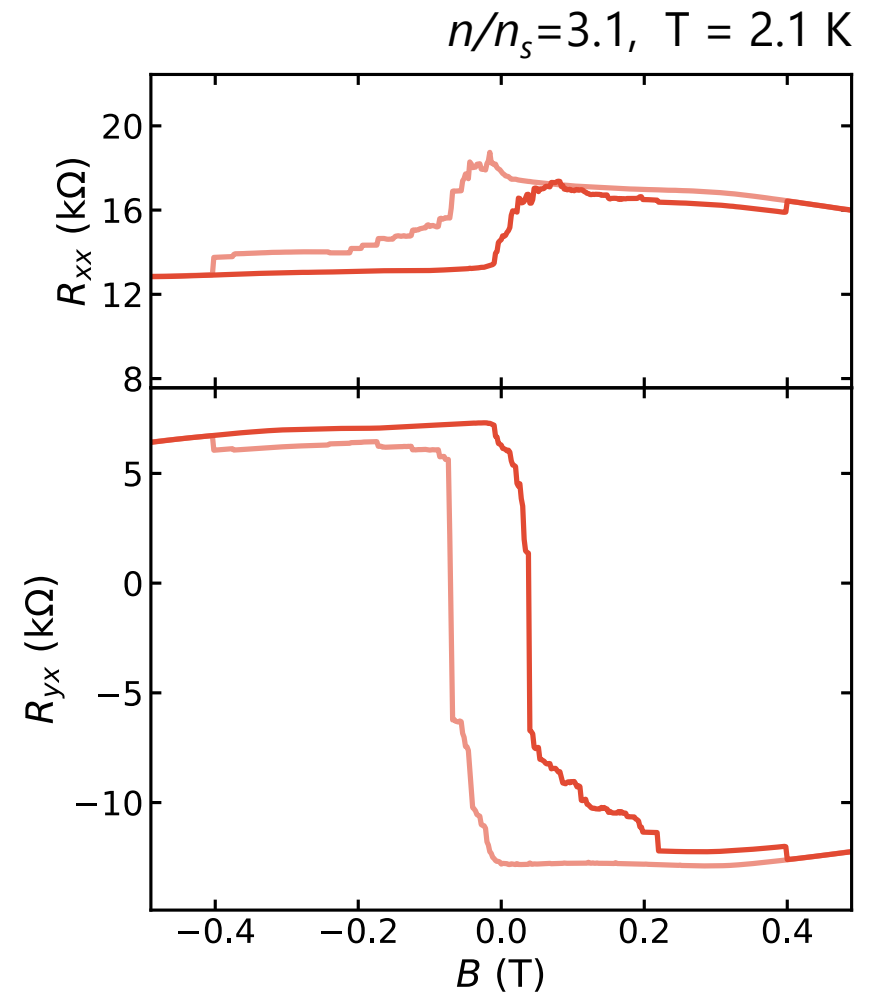
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Evidence of domains

Reminiscent of early Magnetic Tis \rightarrow Chern insulator?

Ideally: $\rho_{xx} = 0$

$$\rho_{xy} = h/e^2 \approx 26 \text{ k}\Omega$$



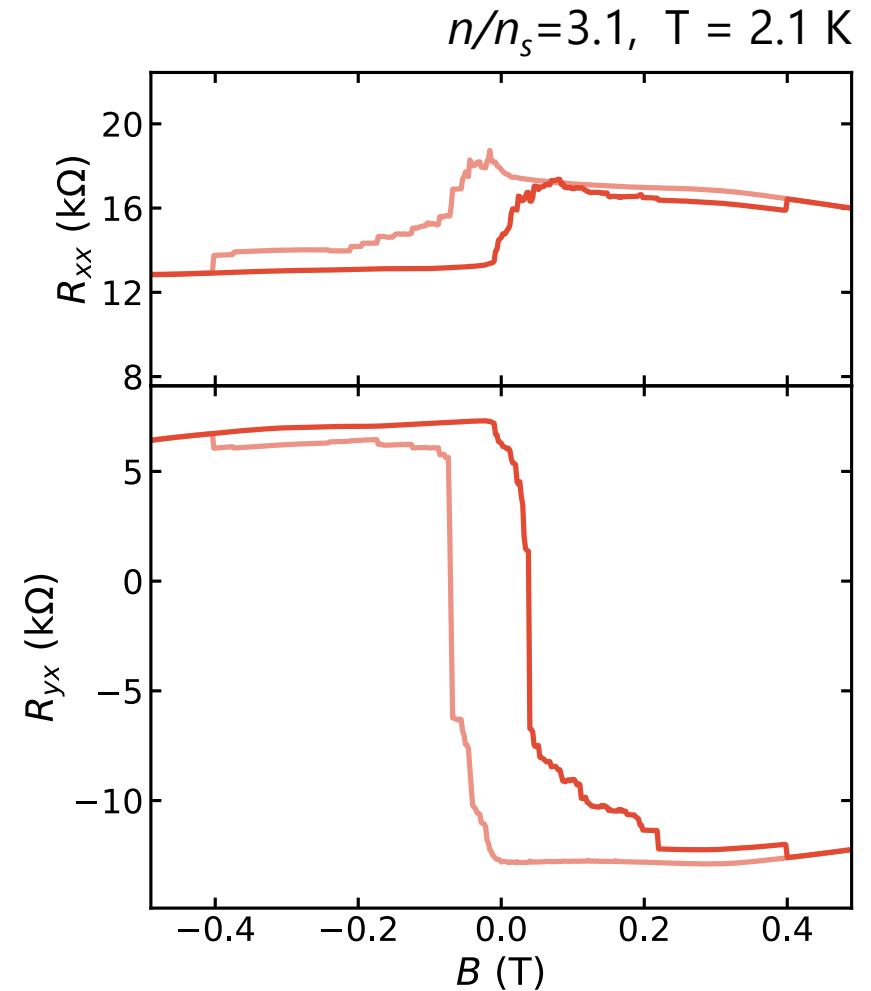
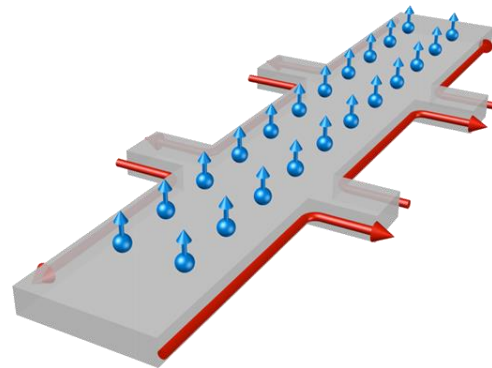
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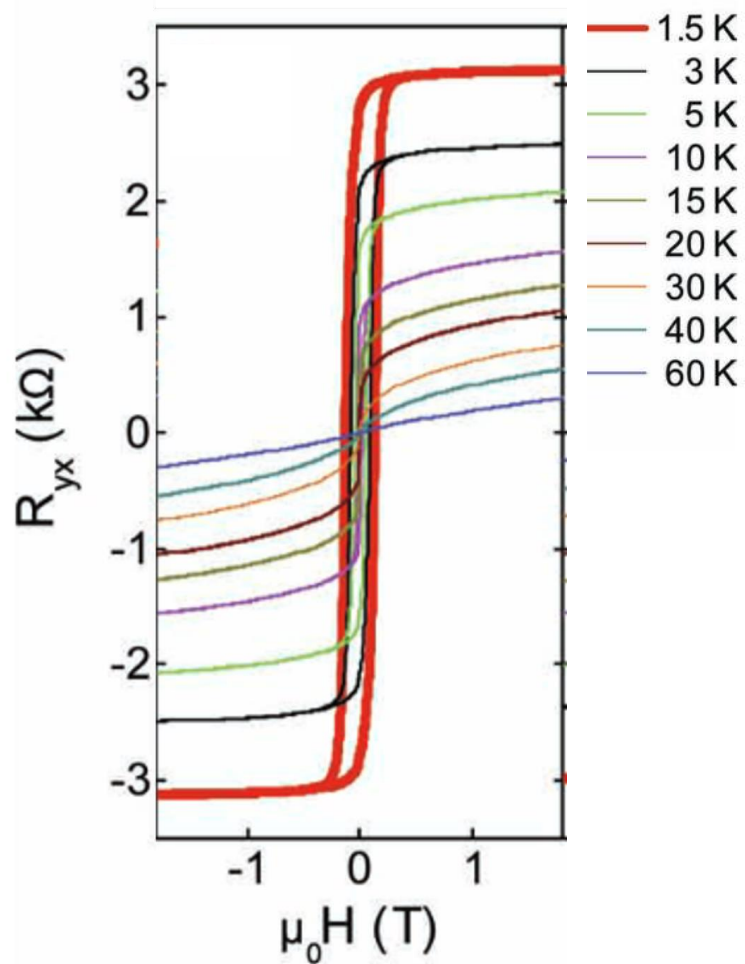
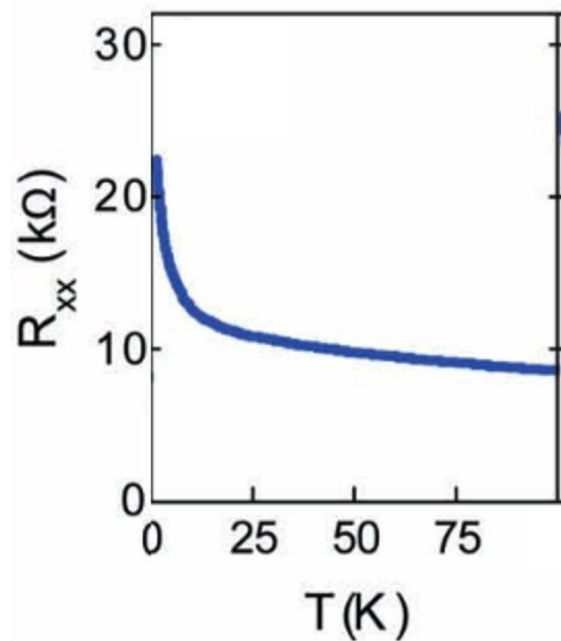
Large anomalous Hall (and R_{xx})
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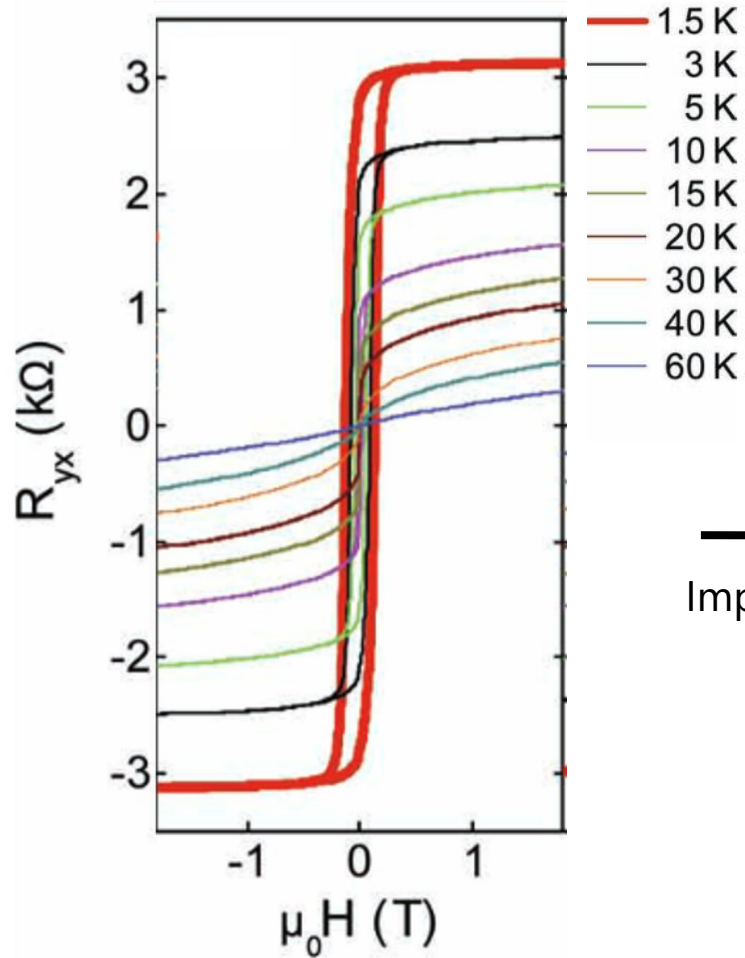
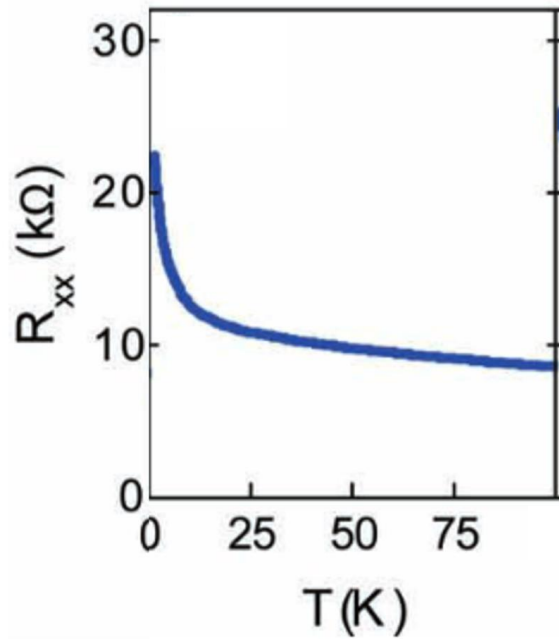
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Early magnetically doped topological insulators

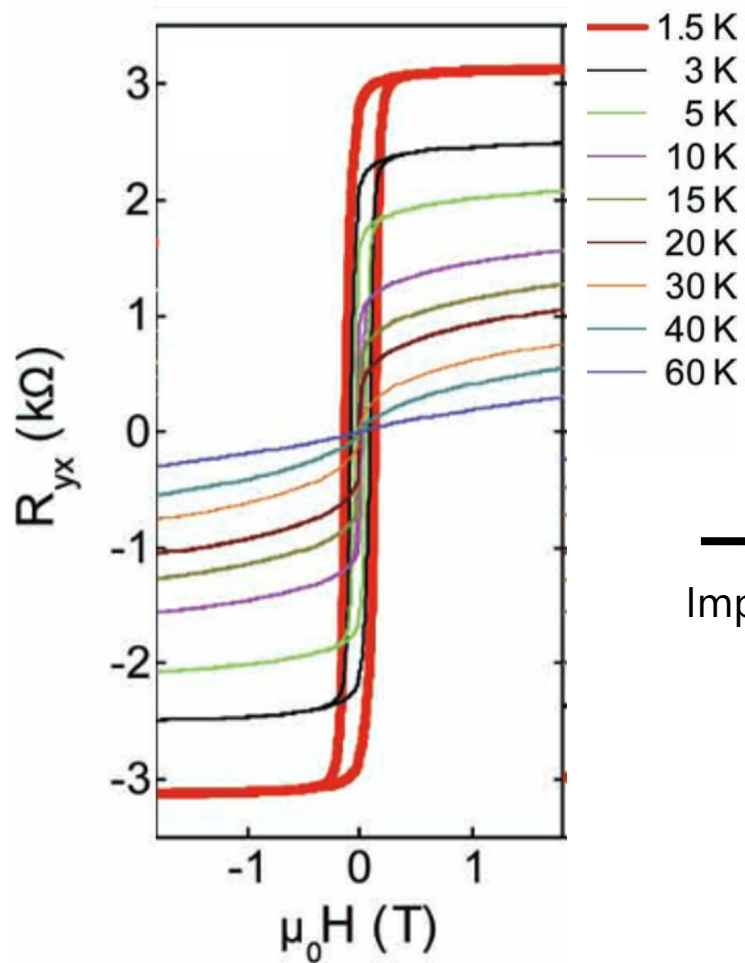
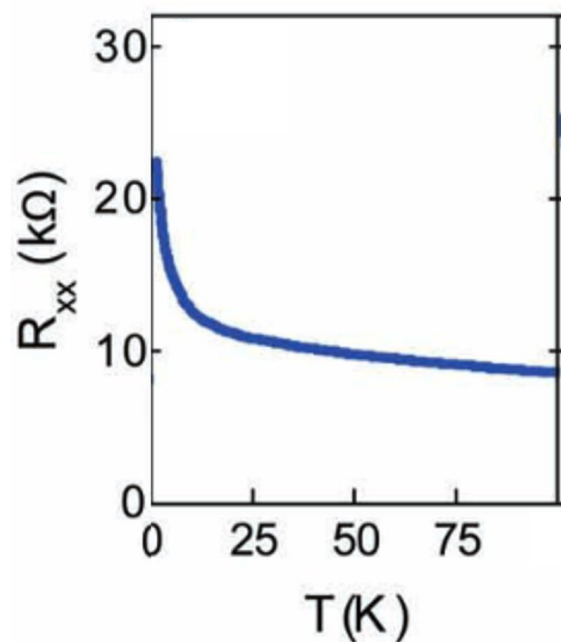


Early magnetically doped topological insulators

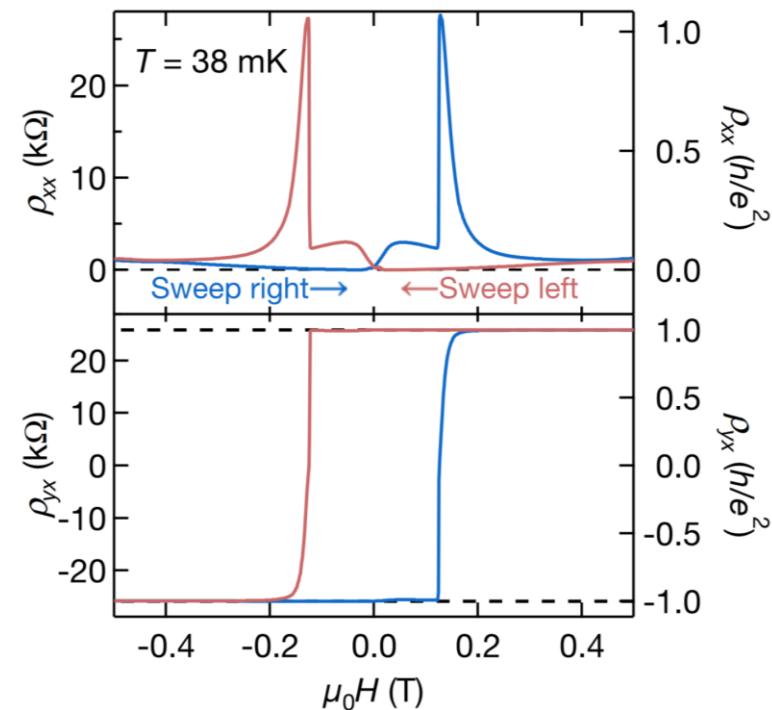


→
Improve films

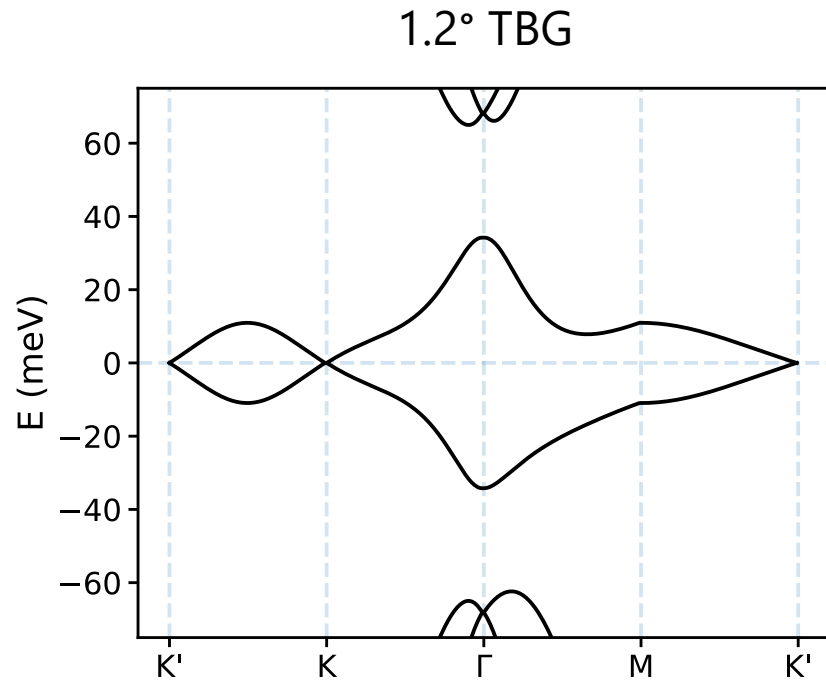
Early magnetically doped topological insulators



Improve films



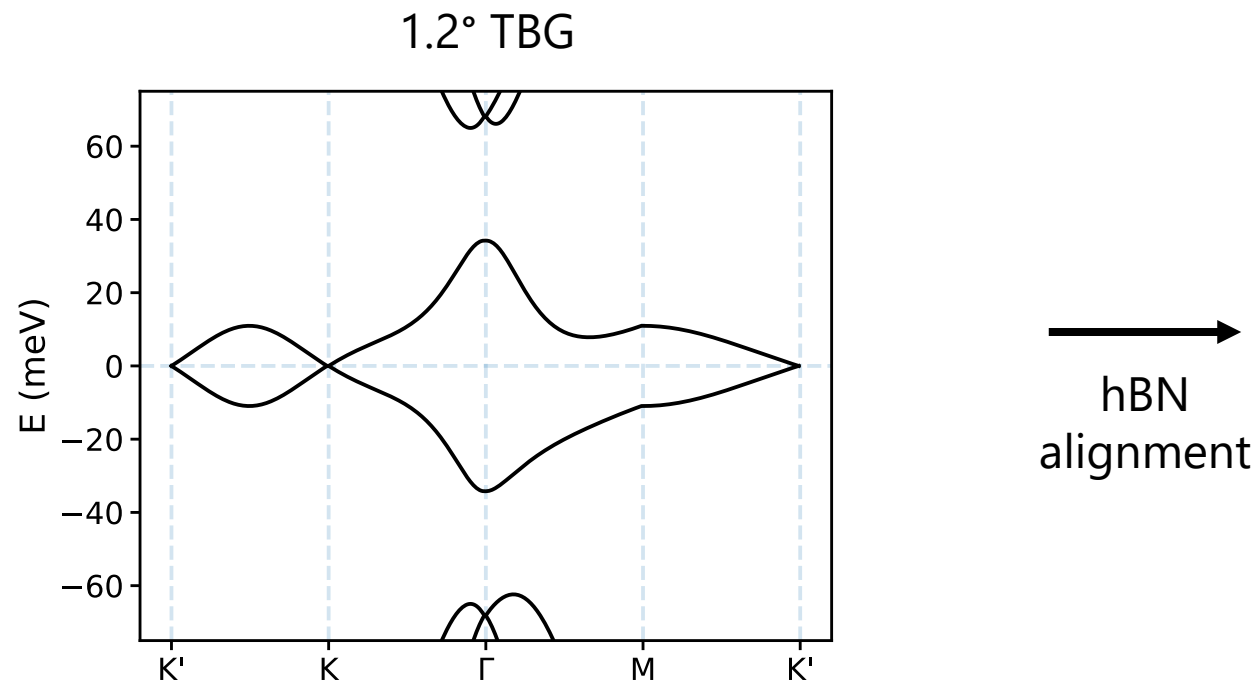
hBN alignment is the key for AH?



https://git.sr.ht/~spxtr/bm_model
Sharpe, et al. Science (2019)

Theory:
Zhang, et al. PRB (2019)
Bultinck, et al. PRL (2020)
Xie and MacDonald, PRL (2020) – Gap open spontaneously?

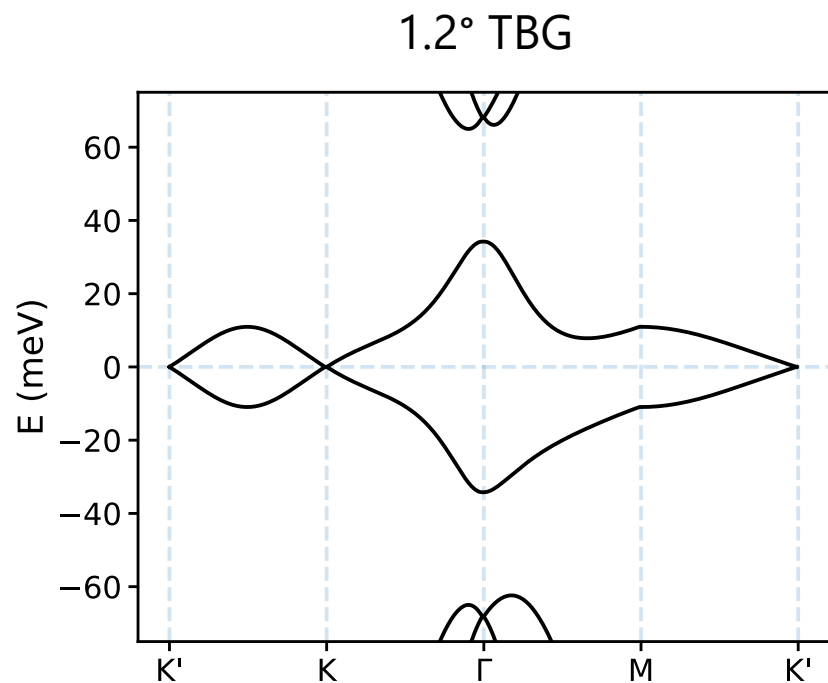
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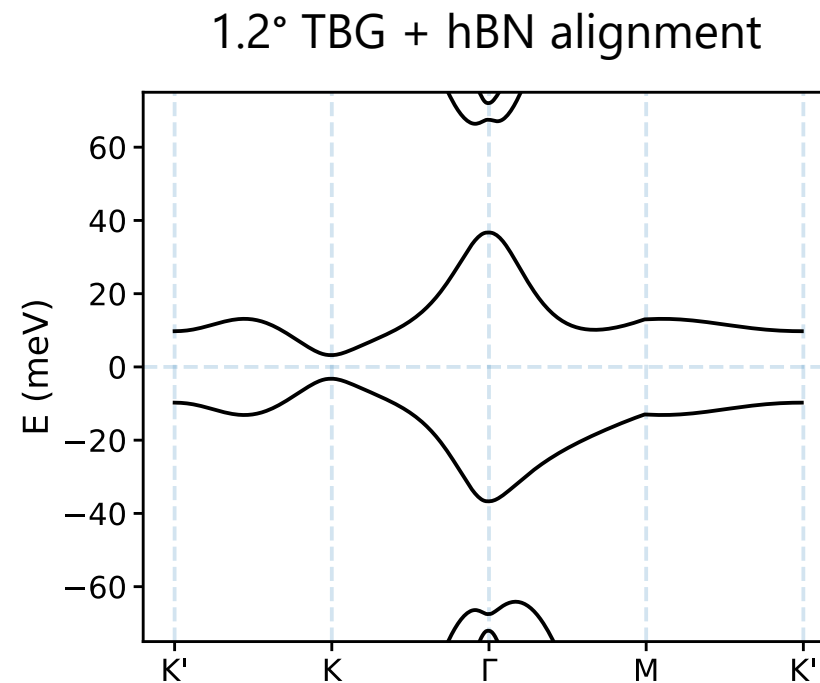
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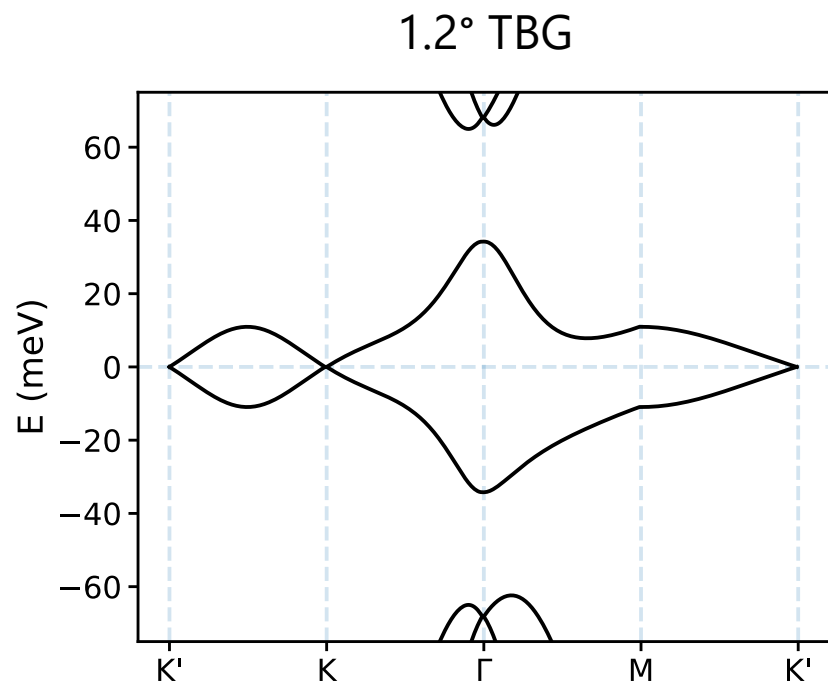
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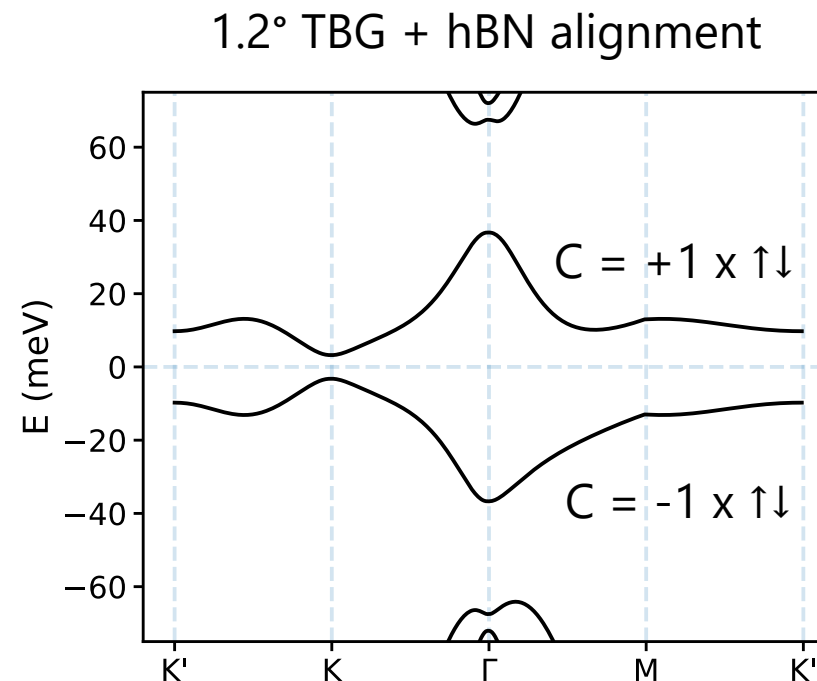
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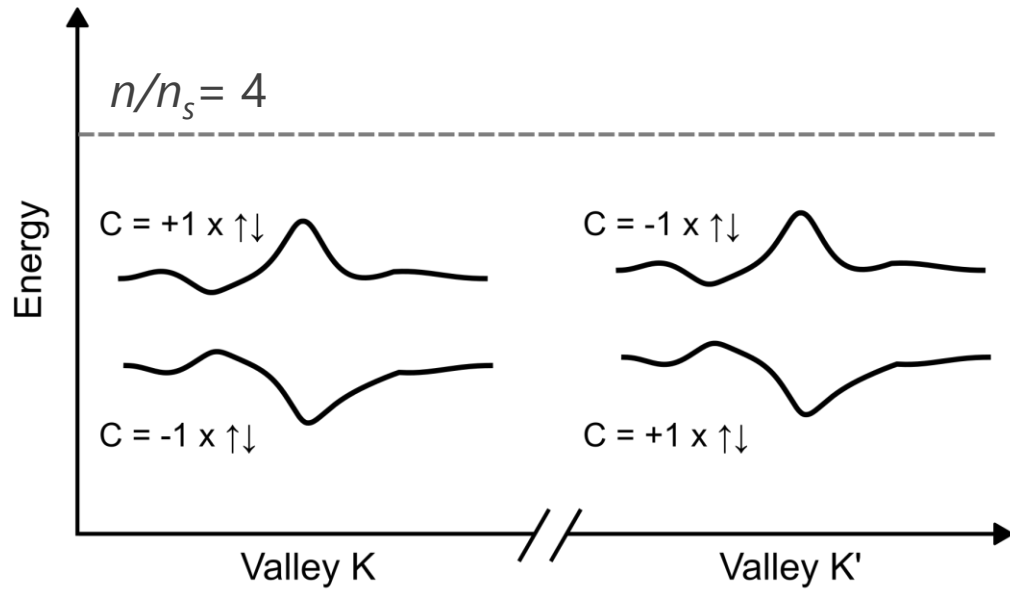
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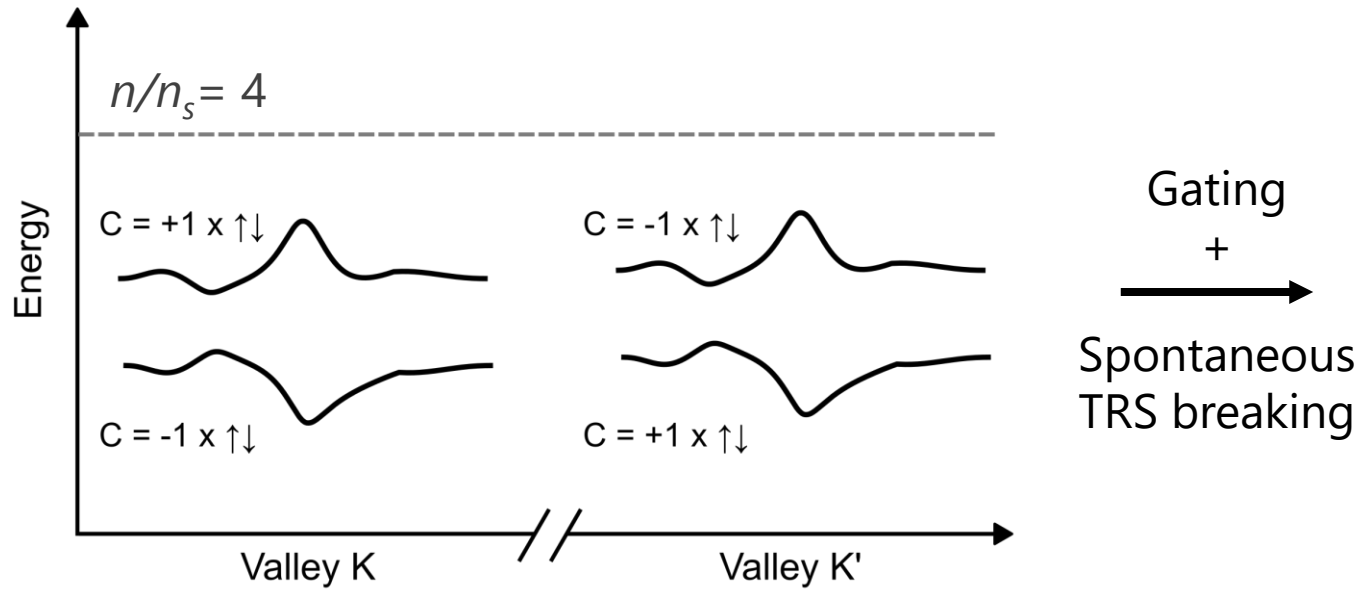
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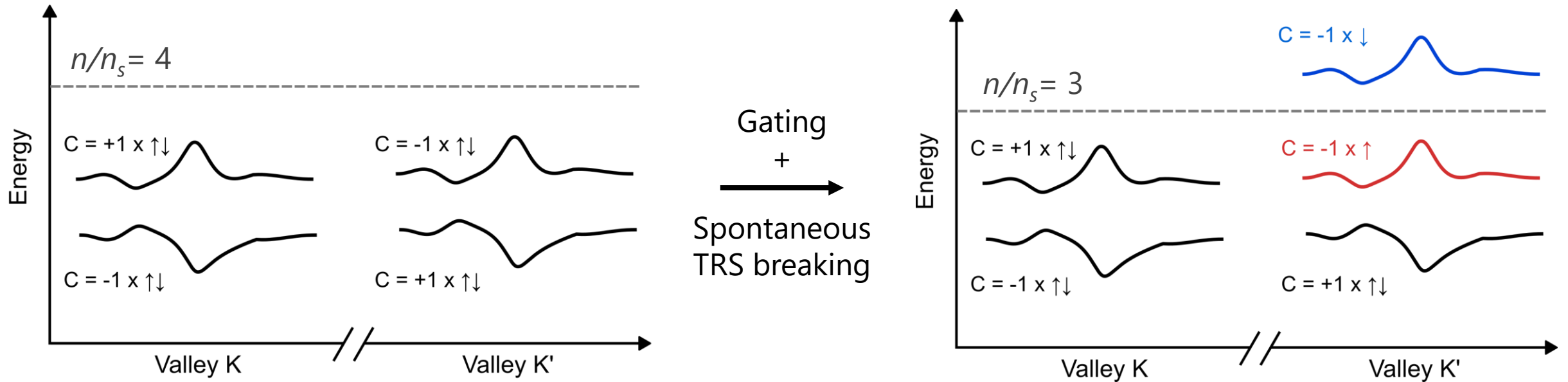
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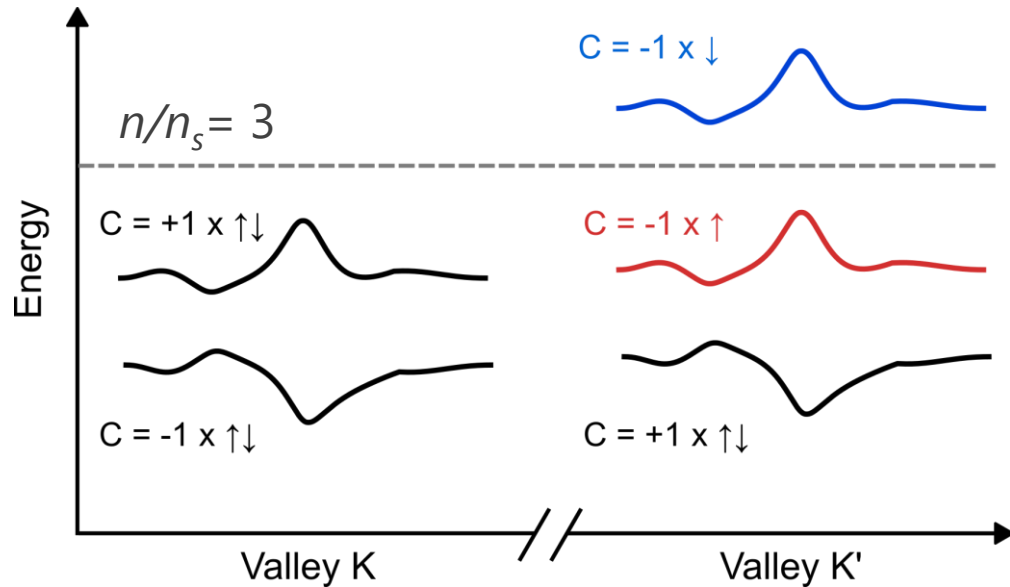


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Possible Scenarios and in-plane response

Interaction driven spin/valley polarization



Xie et al. PRL (2020)

Zhang et al. PRR (2019)

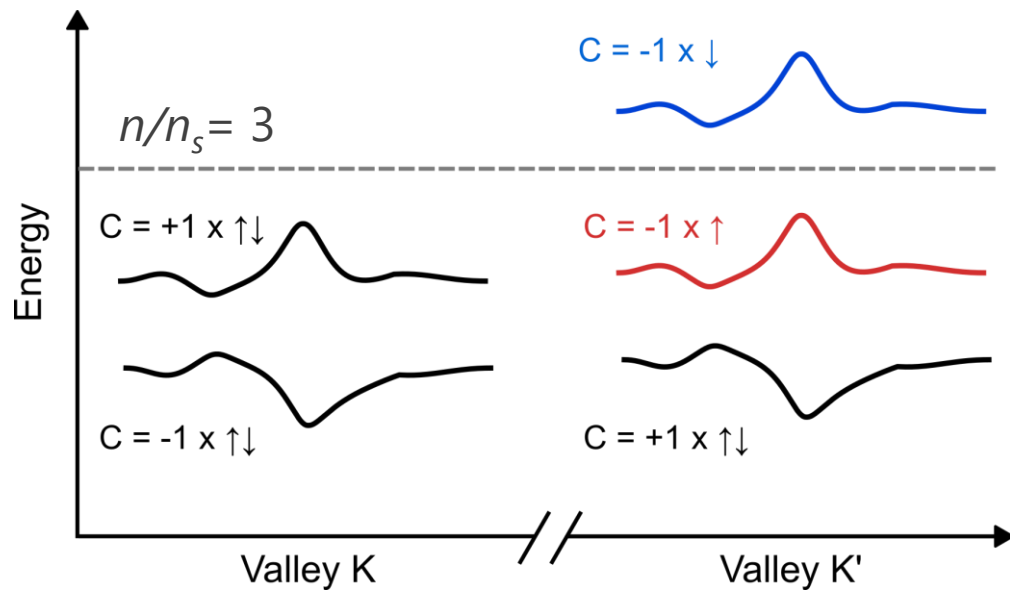
Bultinck et al., PRL (2020)

Martin et al., PRL (2008)

Lee et al., Nat. Comms (2019)

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Interaction driven spin/valley polarization



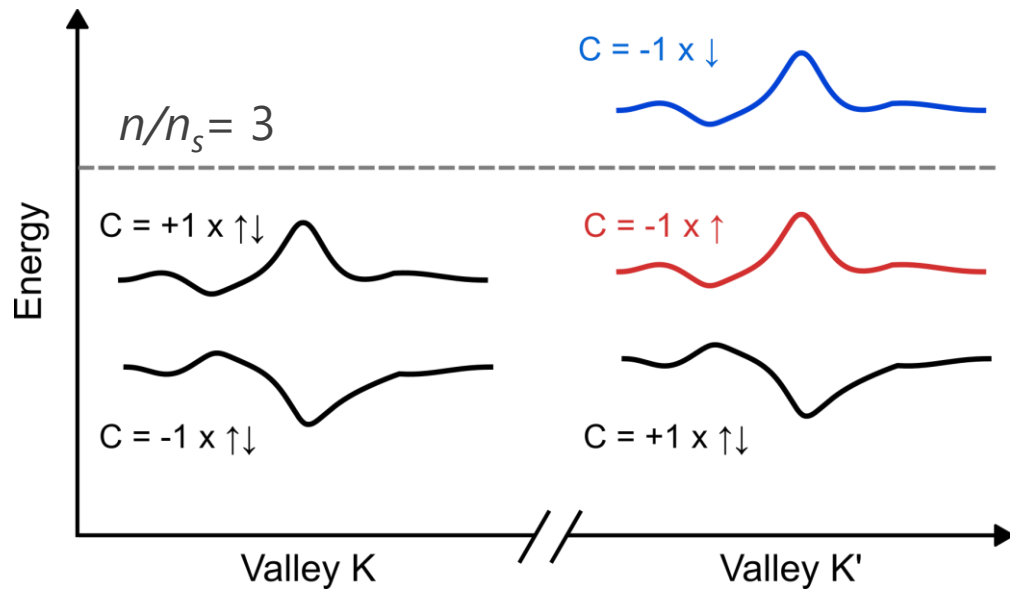
Spin?



- Xie et al. PRL (2020)
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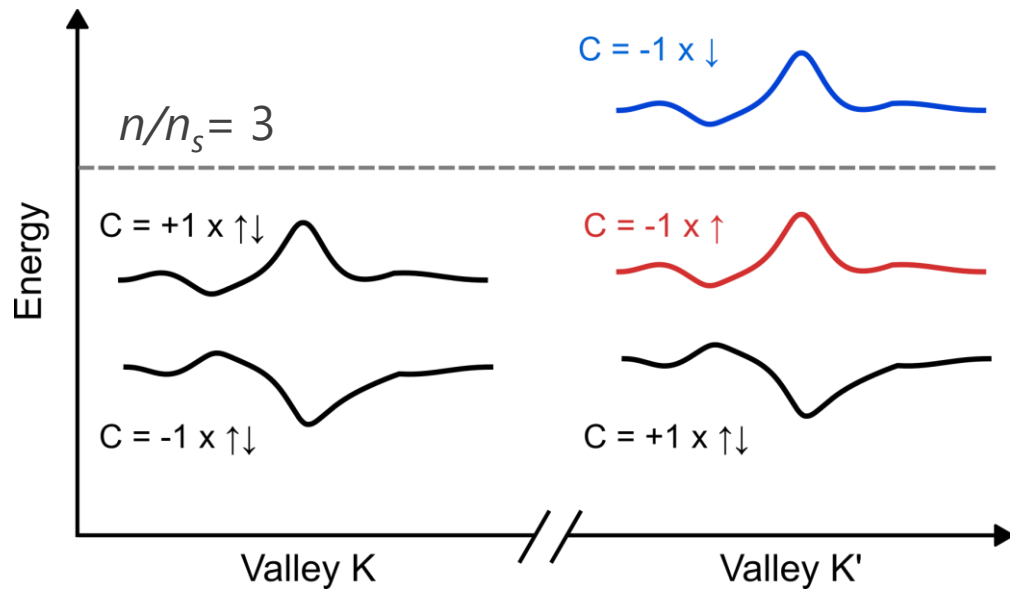


Orbital?

- Xie et al. PRL (2020)
- Zhang et al. PRR (2019)
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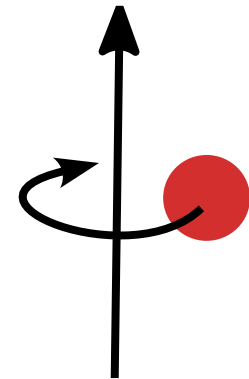
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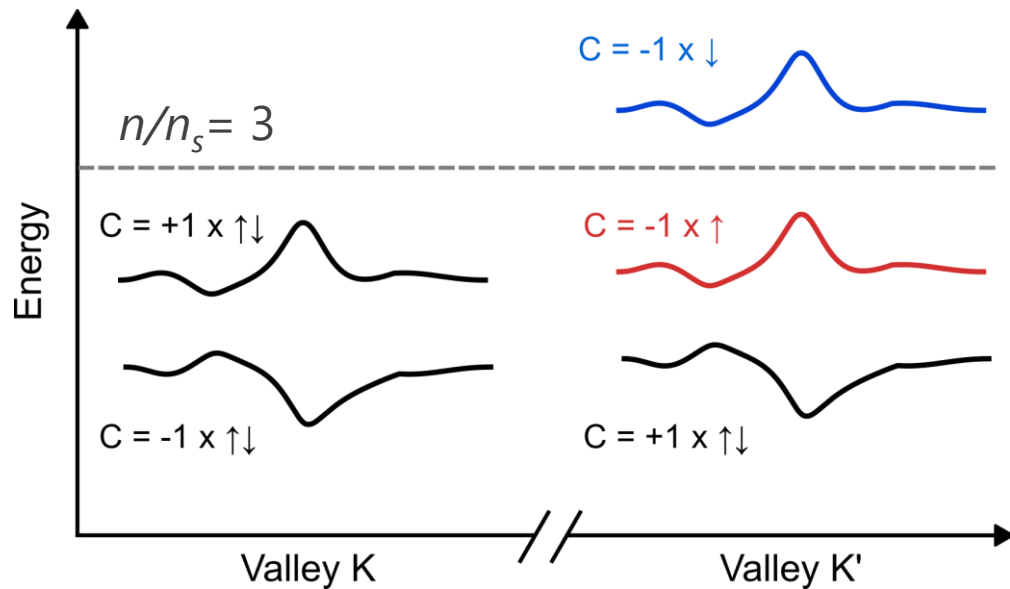
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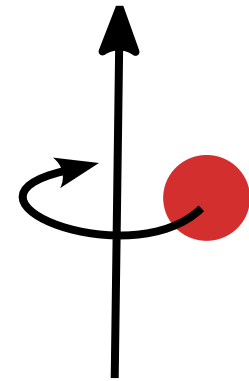
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Spin?



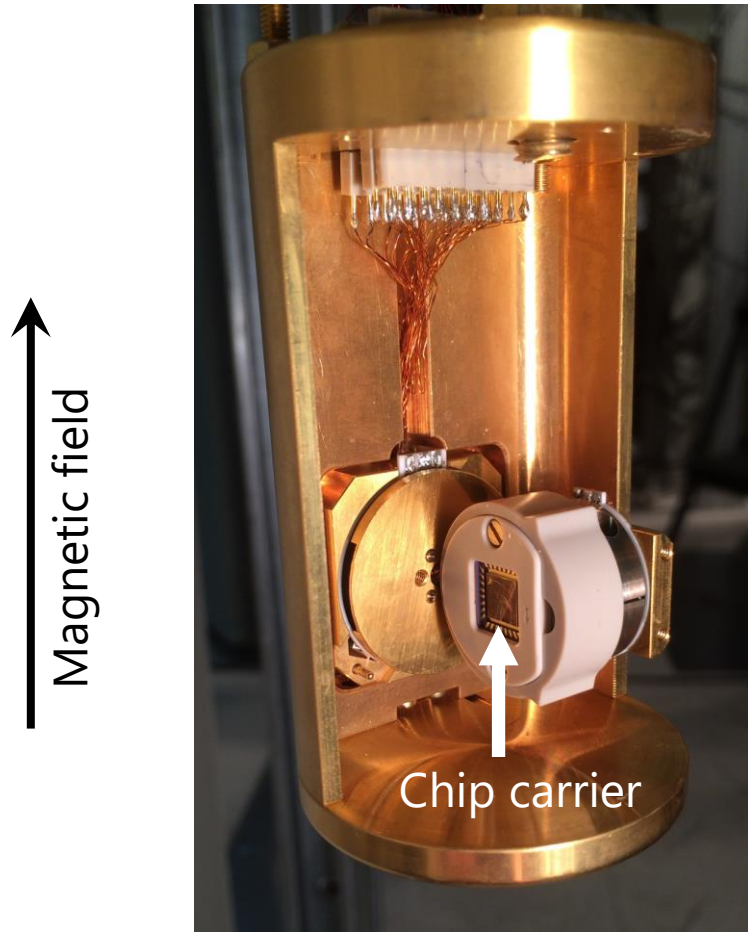
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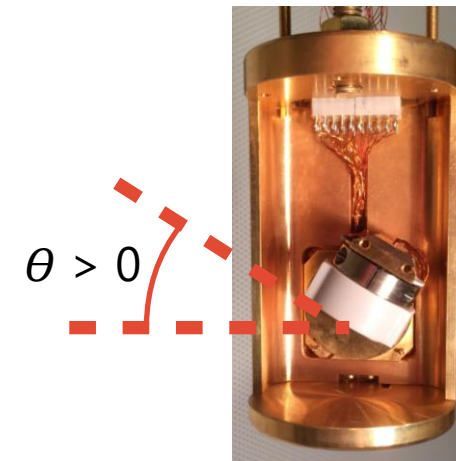
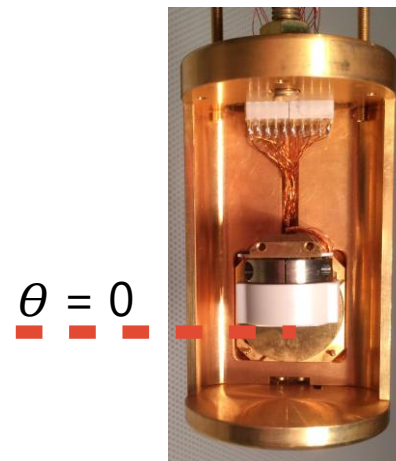
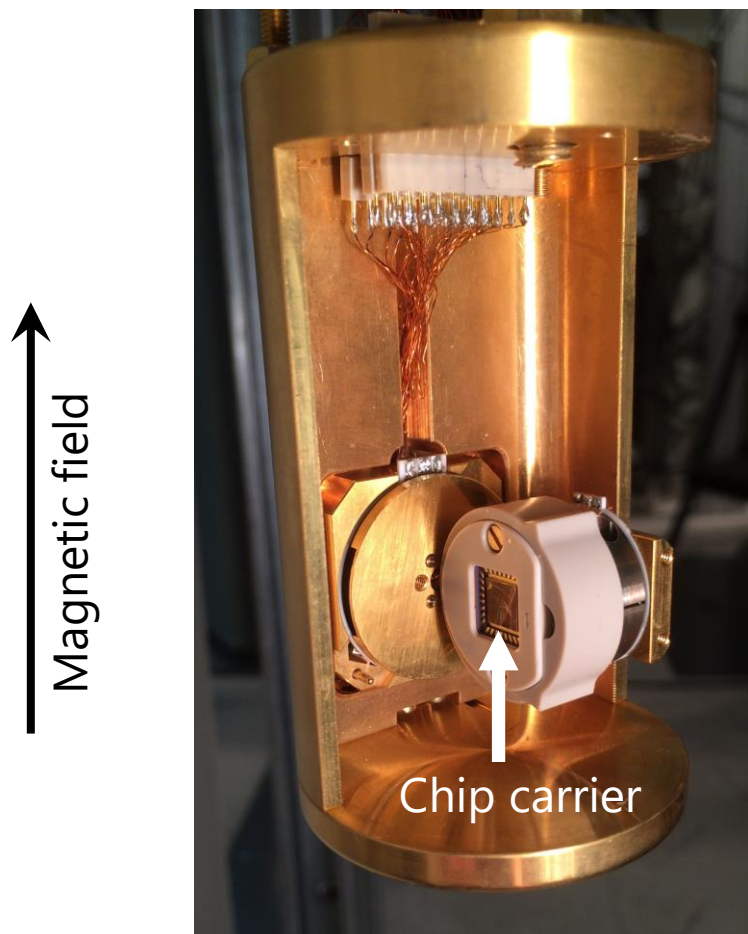
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- Bultinck et al., PRL (2020)
- Martin et al., PRL (2008)
- Lee et al., Nat. Comms (2019)

In-plane field can couple to valley!

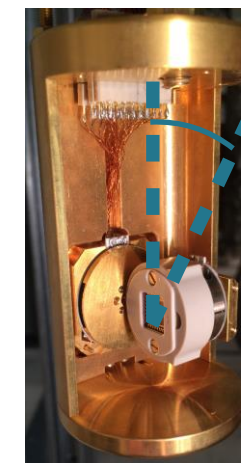
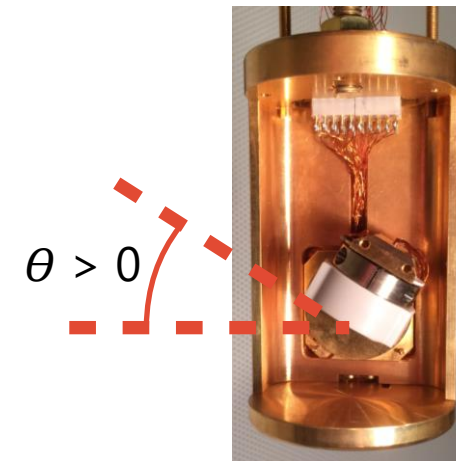
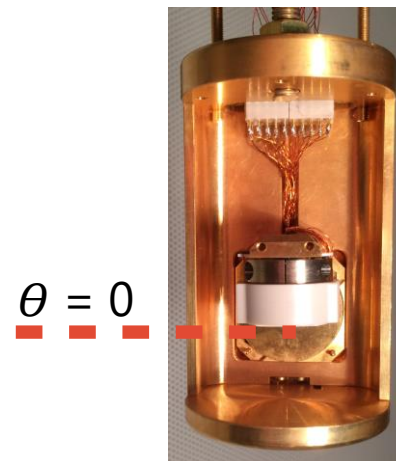
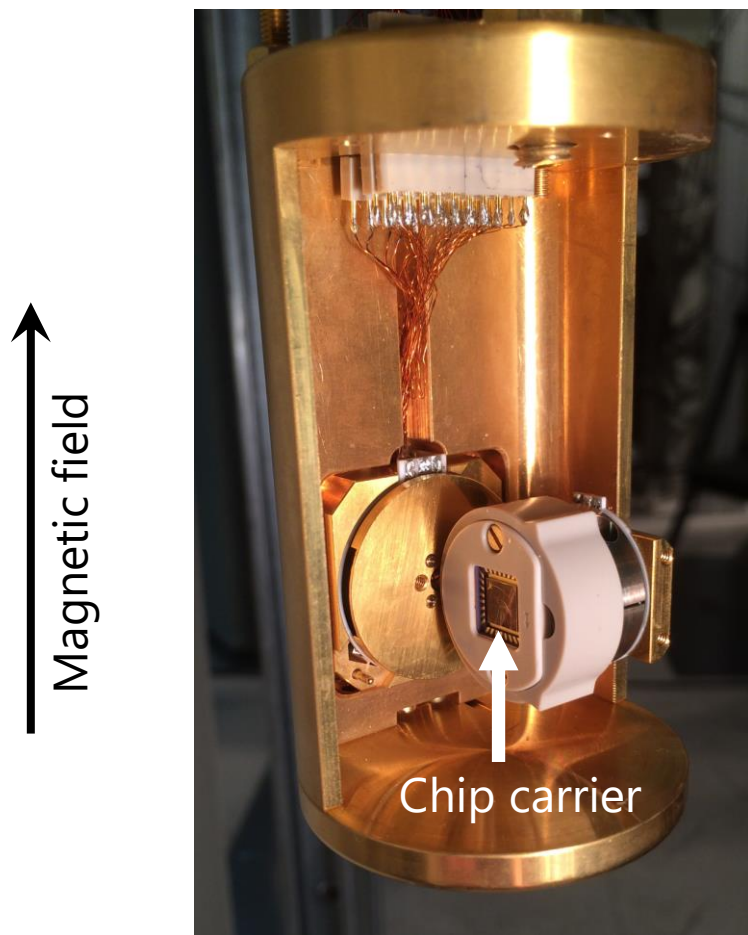
Probing Nature of Magnetism



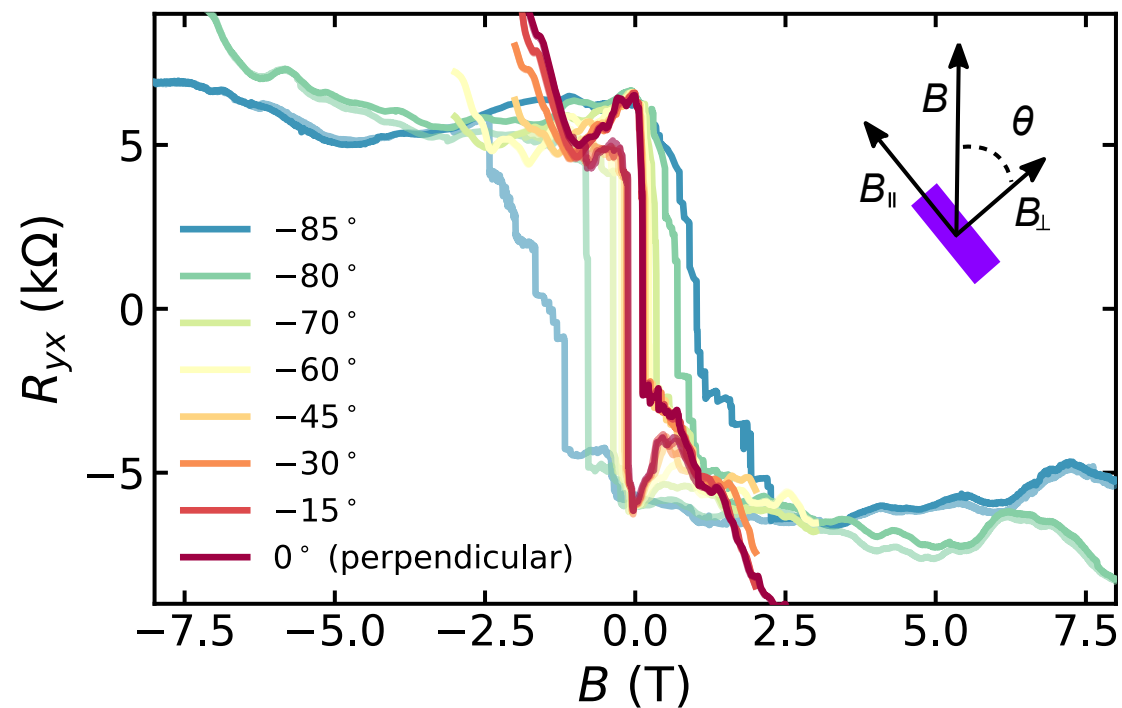
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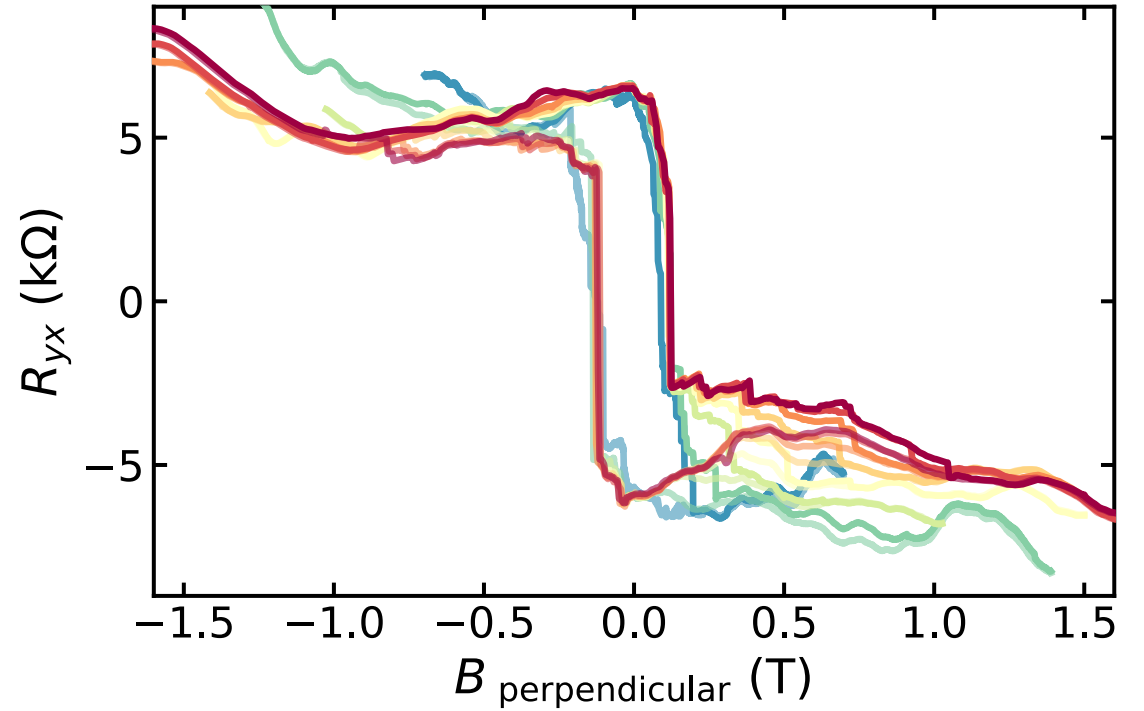
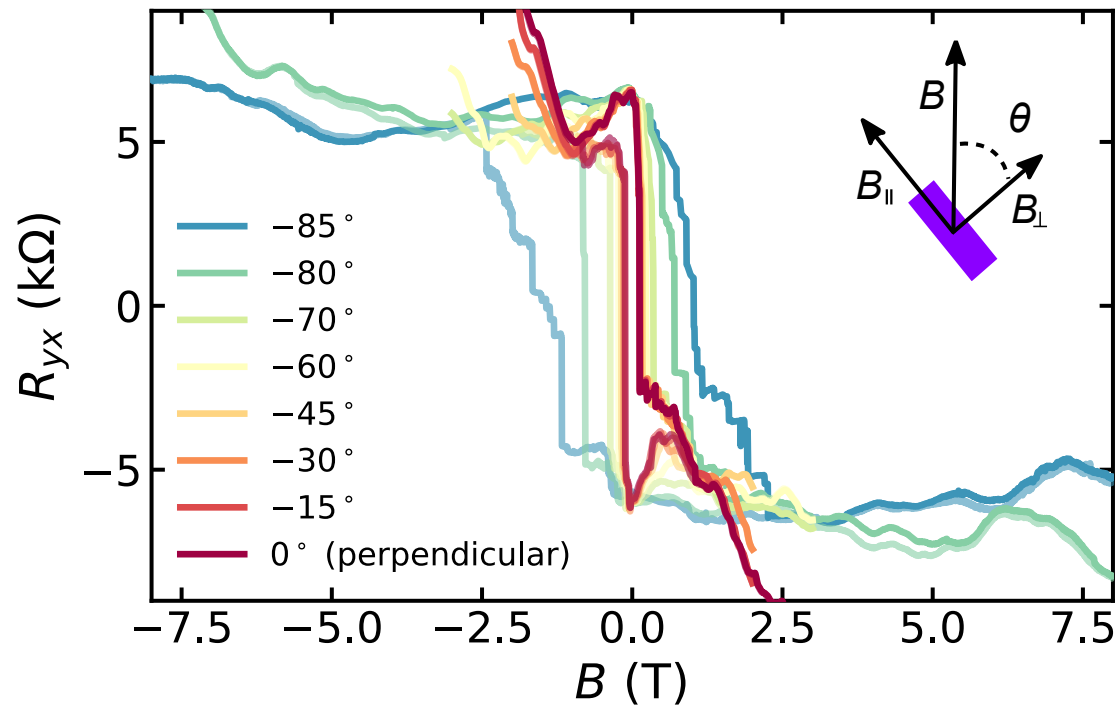


Hysteresis loops in tilted field



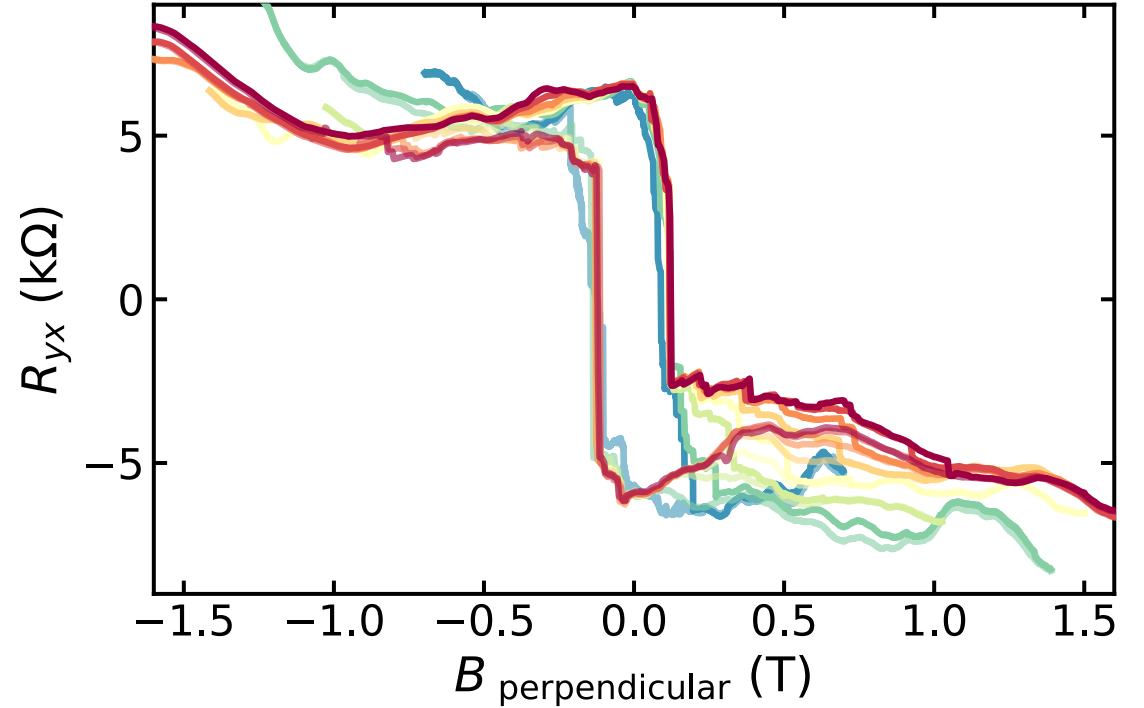
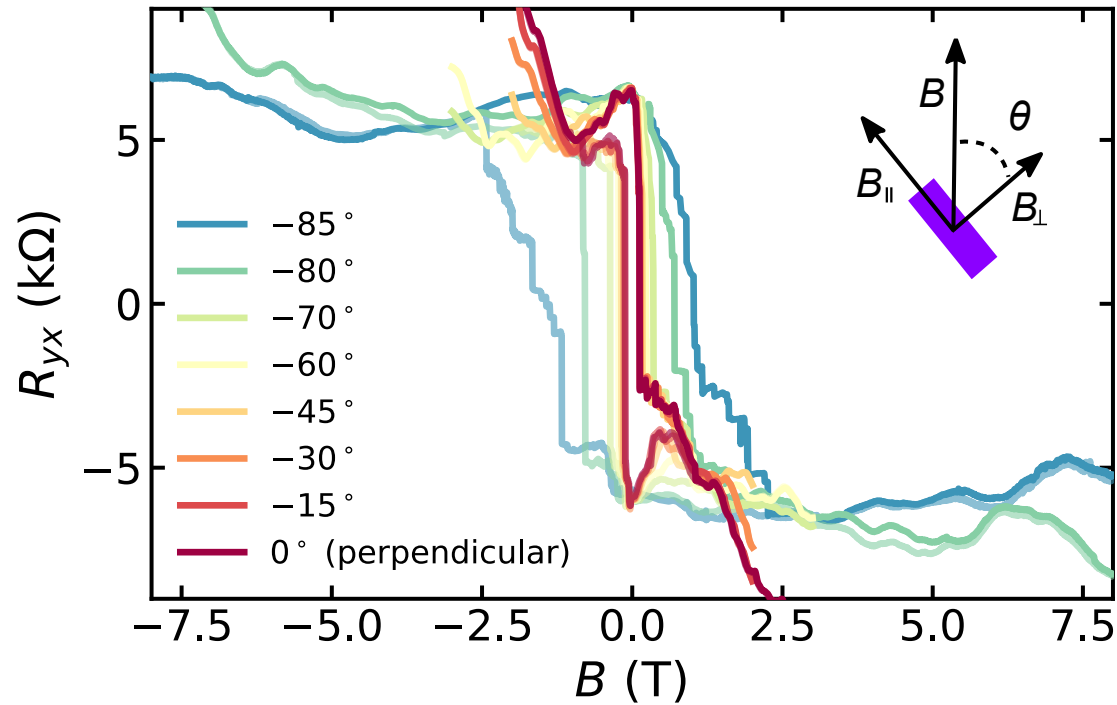
Similar conclusion: Tschirhart, et al. Science (2021)
Sharpe, et al. Nano Lett. (2021)

Hysteresis loops in tilted field



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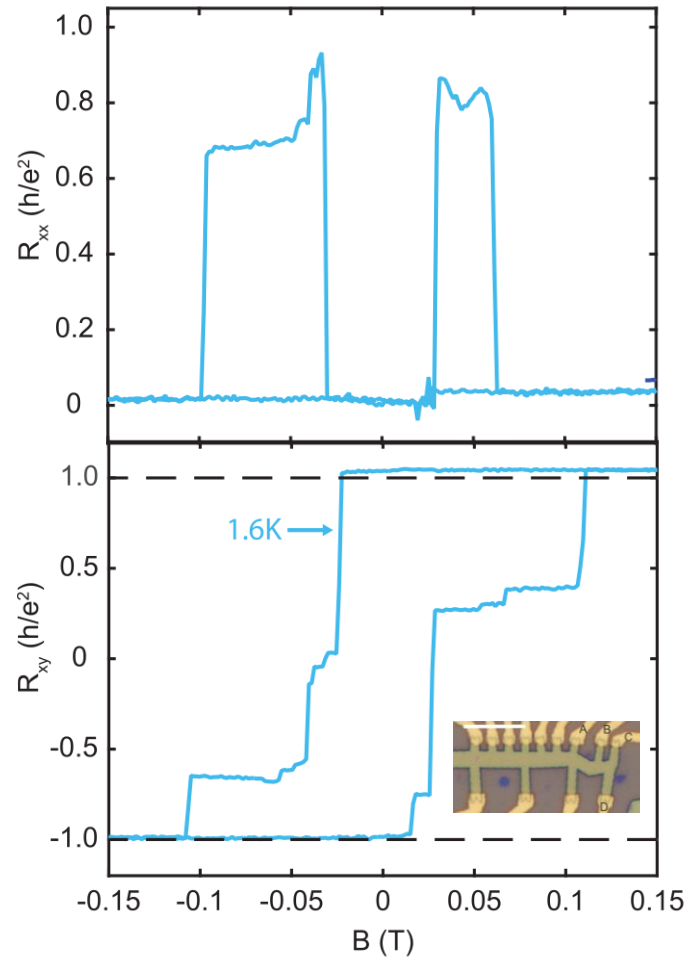
Hysteresis loops in tilted field



Data collapses when plotted vs B perpendicular!
Orbital Ferromagnet!

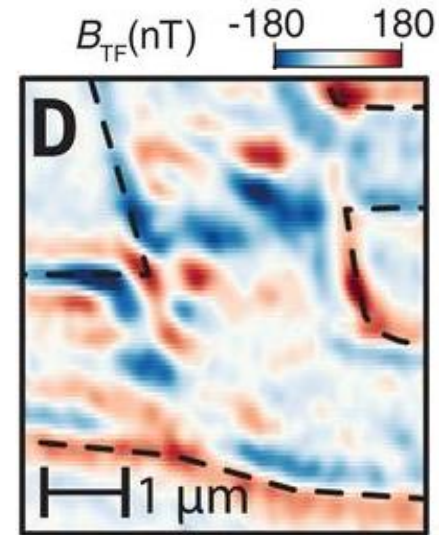
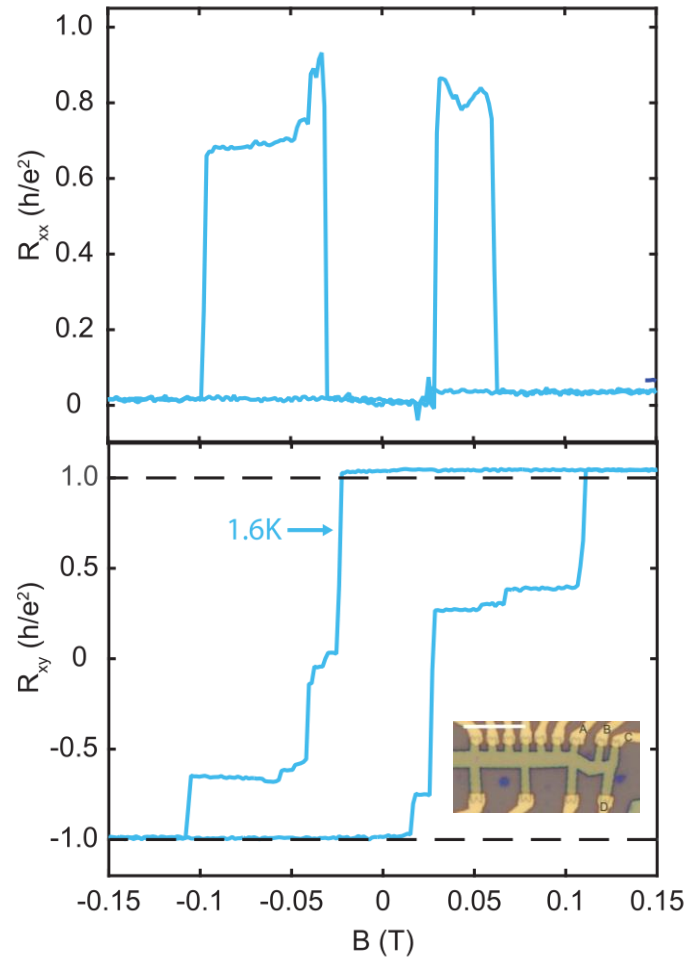
Quantum anomalous Hall in TBG

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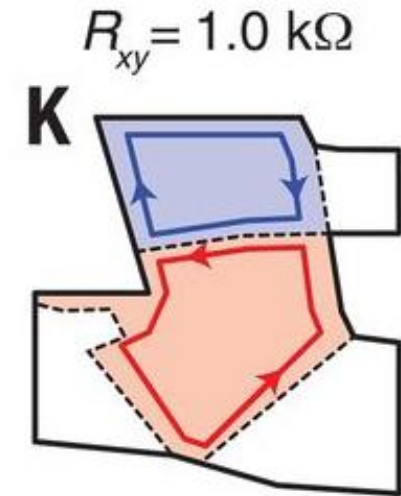
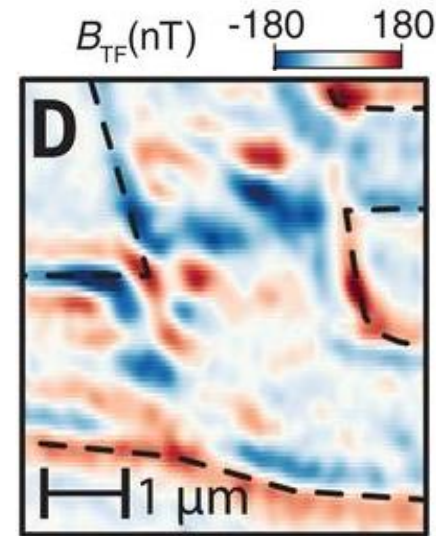
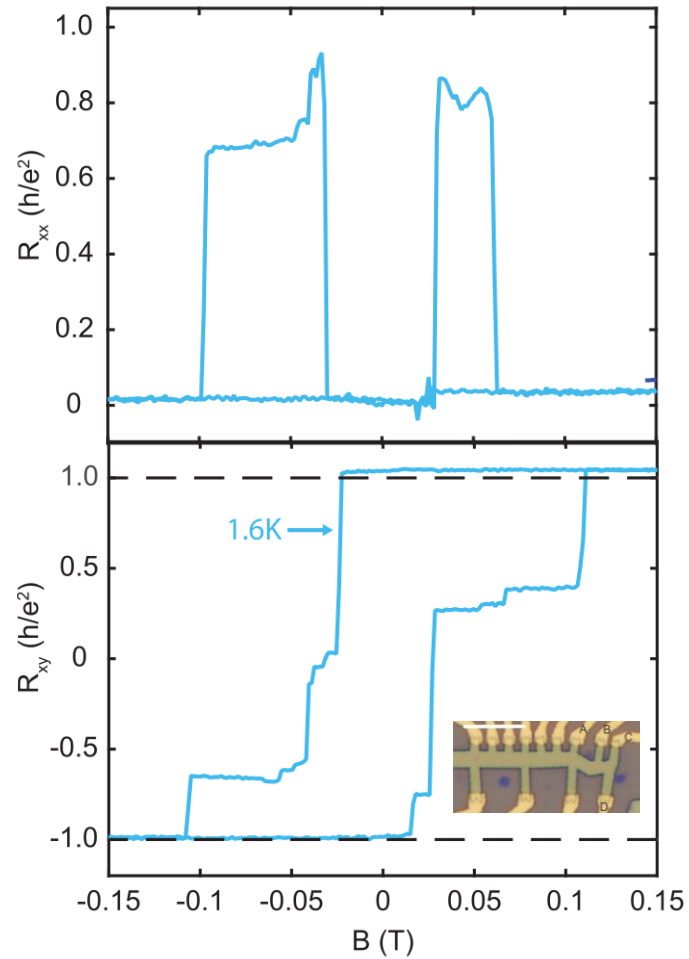


Serlin, et al. Science (2020)
Tschirhart, et al. Science (2021)

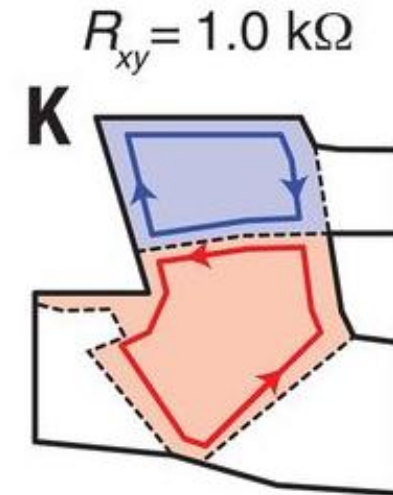
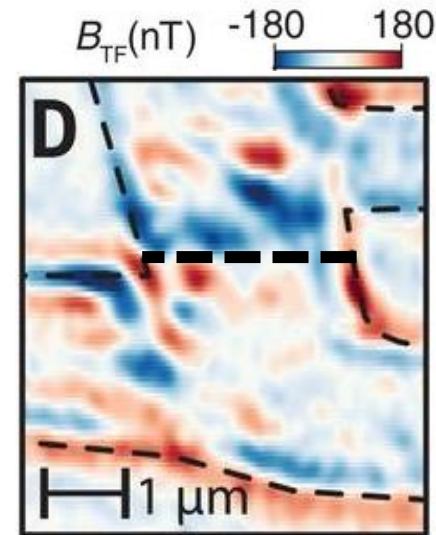
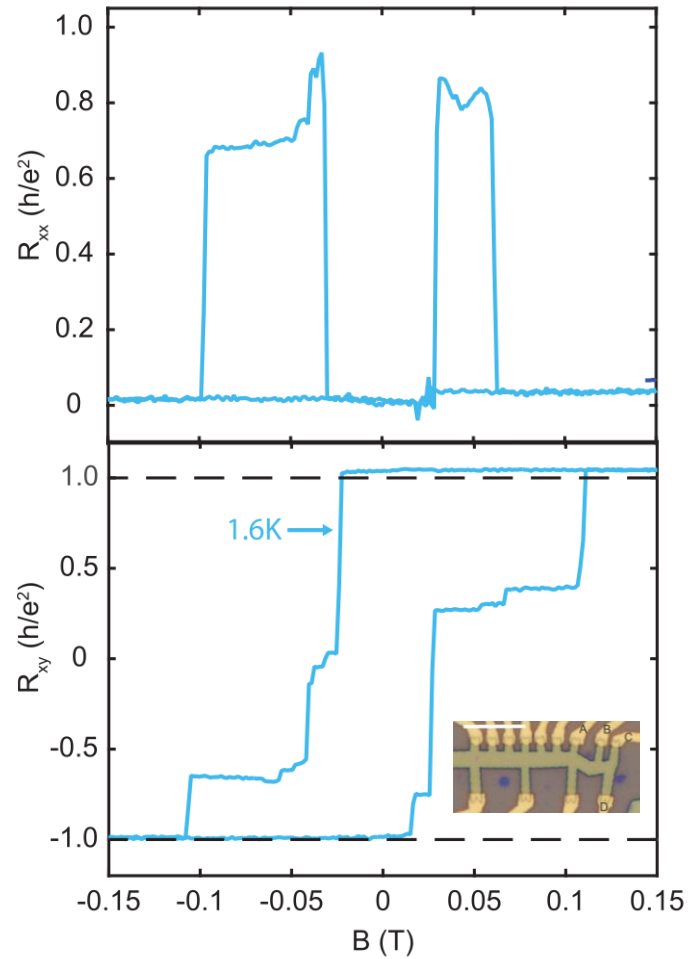
Quantum anomalous Hall in TBG



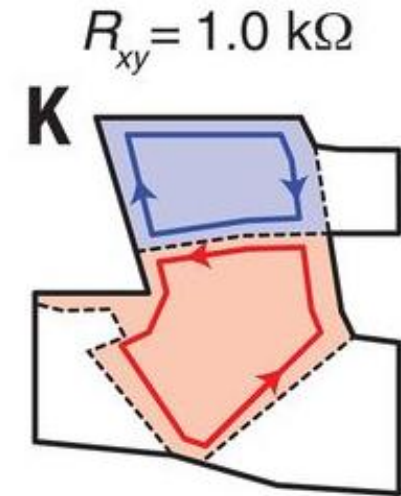
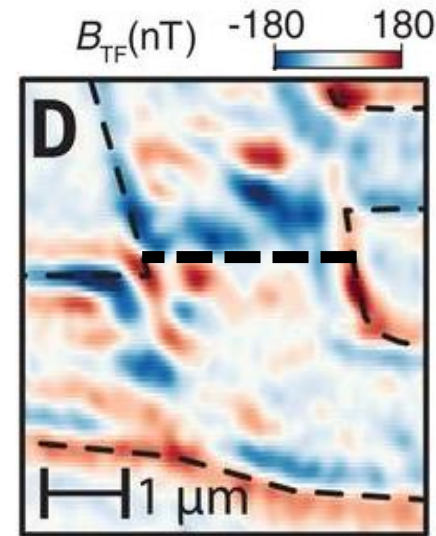
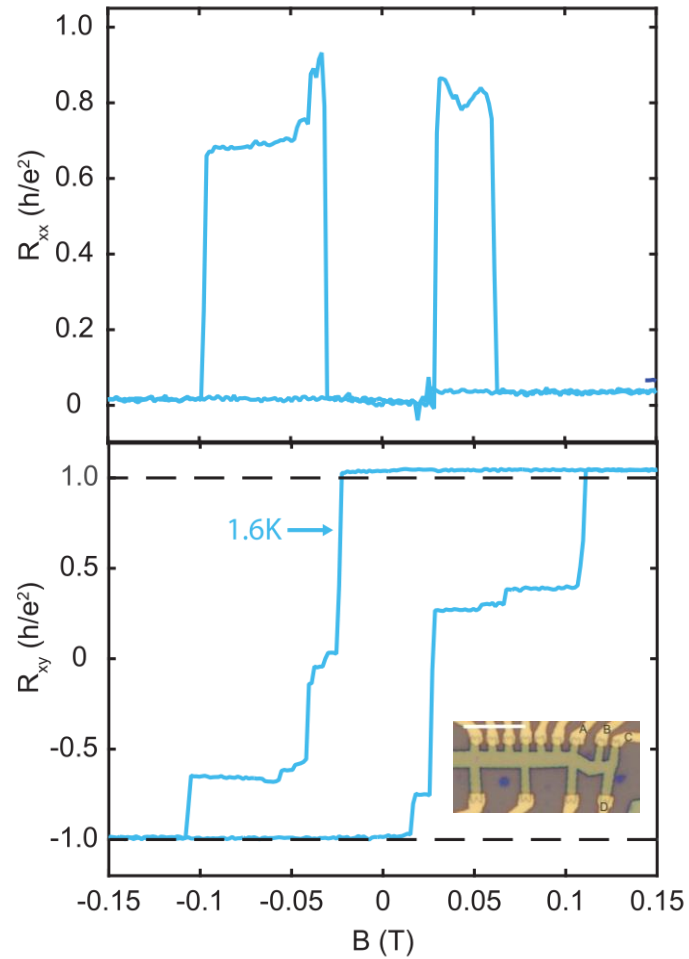
Quantum anomalous Hall in TBG



Quantum anomalous Hall in TBG



Quantum anomalous Hall in TBG



Spotty magnet yet quantized?

(Q)AH is quite common in moirés!

MATBG aligned/commensurate with hBN:

A. Sharpe, et al. *Science* (2019)

M. Serlin, et al. *Science* (2020)

Tschirhart, et al. *Science* (2021)

A. Sharpe, et al. *Nano Lett.* (2021)

P. Stepanov, et al. *PRL* (2021)

C-C. Tseng, et al. *Nat. Phys* (2022)

S. Grover, et al. *Nat. Phys* (2022)

Z. Zhang, et al. arXiv:2408.12509

MATBG + WSe₂:

J-X. Lin, et al. *Science* (2022)

Rhombohedral graphene

Trilayer aligned to hBN (FCI?)

G. Chen, A. Sharpe, et al. *Nature* (2020)

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Pentalayer (FCI when aligned to hBN)

T. Han, et al. *Nature* (2023)

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Hexalayer aligned to hBN (FCI?)

J. Xie, et al. arXiv:2405.16944

Twisted bilayer MoTe₂ (FCI)

E. Anderson, et al. *Science* (2023)

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Y. Zeng, et al. *Nature* (2023)

H. Park, et al. *Nature* (2023)

F.. Xu, et al. *PRX* (2023)

AB-stacked MoTe₂/WSe₂:

T. Li, et al. *Nature* (2021)

Twisted mono-bilayer graphene:

S. Chen, et al. *Nat. Phys* (2020)

H. Polshyn, et al. *Nature* (2020)

M. He, et al. *Nat. Comms* (2021)

Twisted double bilayer graphene:

[AB-AB] M. Kouri, et al. *Nat. Comms* (2022)

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Helical trilayer graphene

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M+N graphene:

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Summary

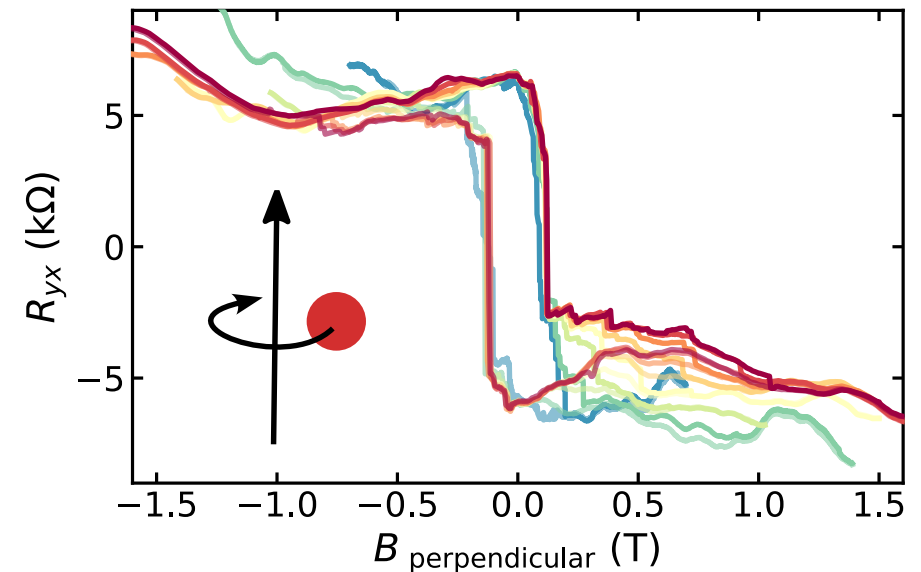
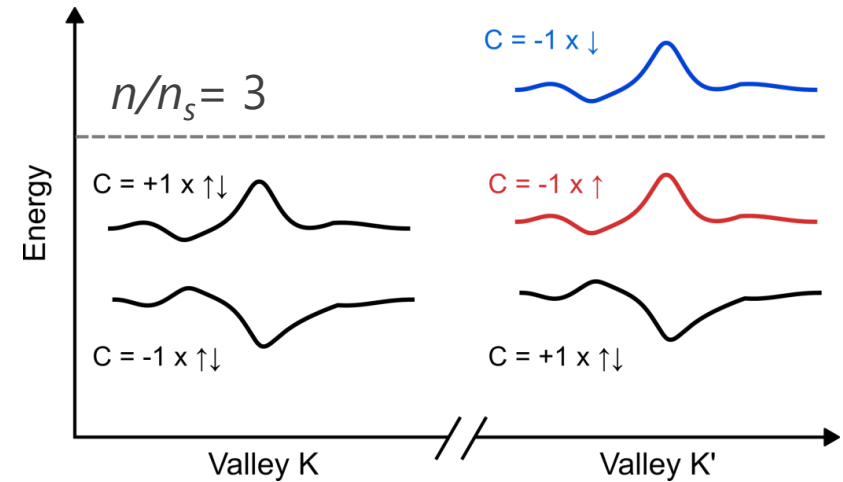
By controlling twist angle, graphene multilayers can become strongly correlated!

TBG is a Chern insulator at filling factor 3!

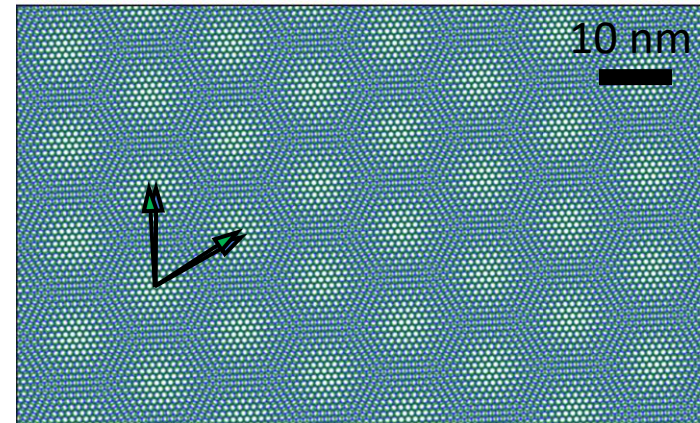
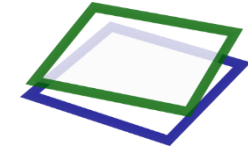
Magnetism is orbital in character
hBN alignment is likely crucial

Why is this orbital magnet so hard to reproduce in TBG?

Magnetism appears splotchy
(Q)AH appears to be quite ubiquitous in moirés
Shouldn't the hBN/graphene form a moiré?
How should we model this?

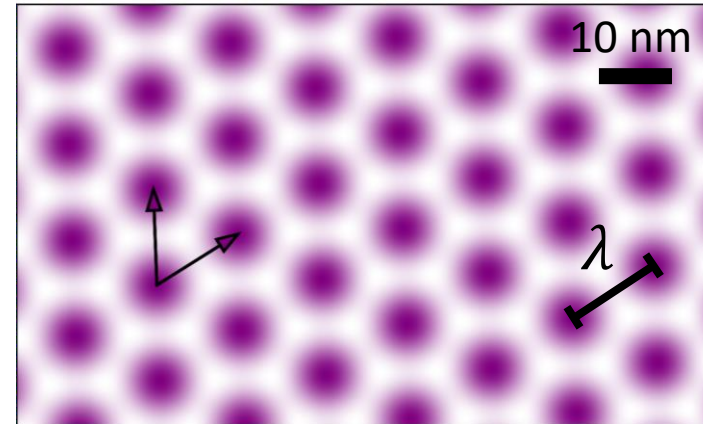
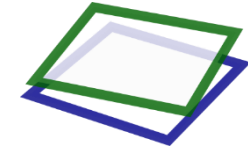


From moiré to multimoiré



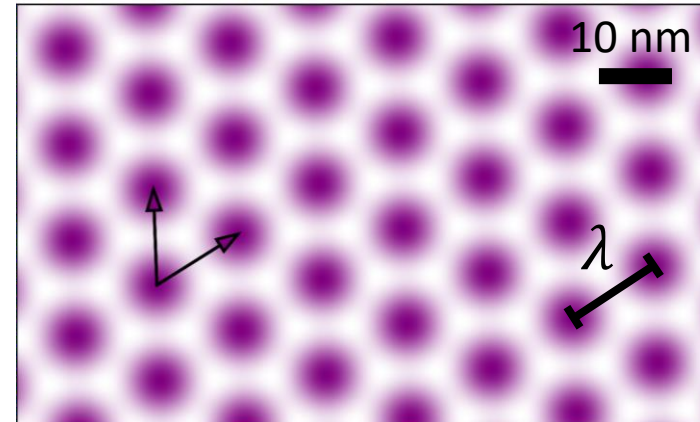
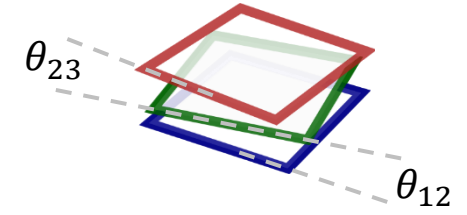
Yang, et al. arXiv:2310.12961
Nakatsuji, et al. PRX (2023)
Foo, et al. PRR (2024)
Bistritzer and MacDonald, PNAS (2011)

From moiré to multimoiré



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From moiré to multimoiré



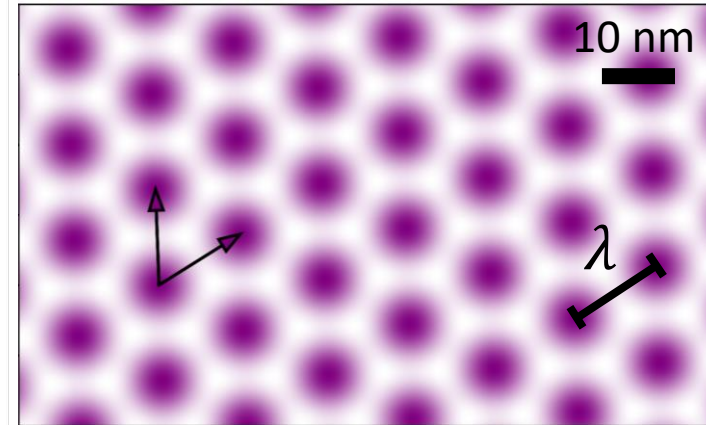
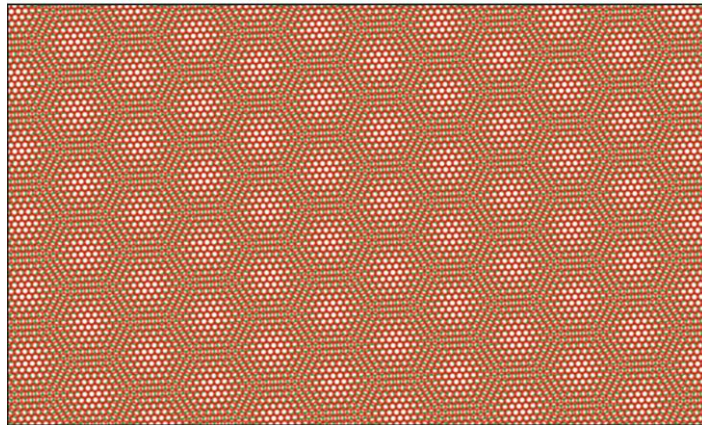
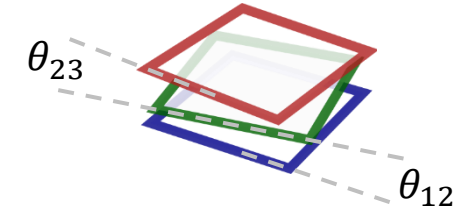
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From moiré to multimoiré



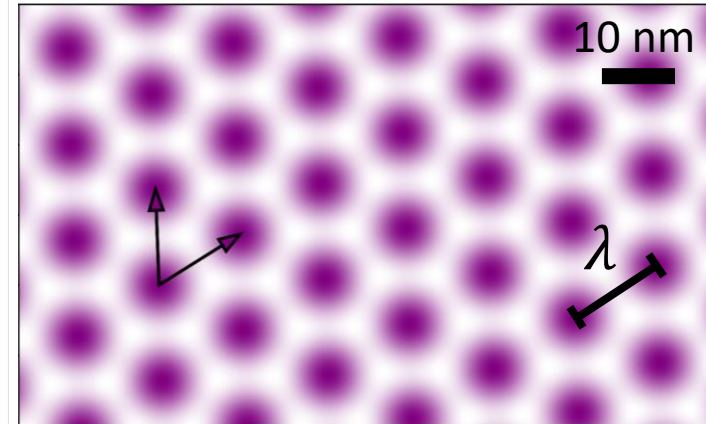
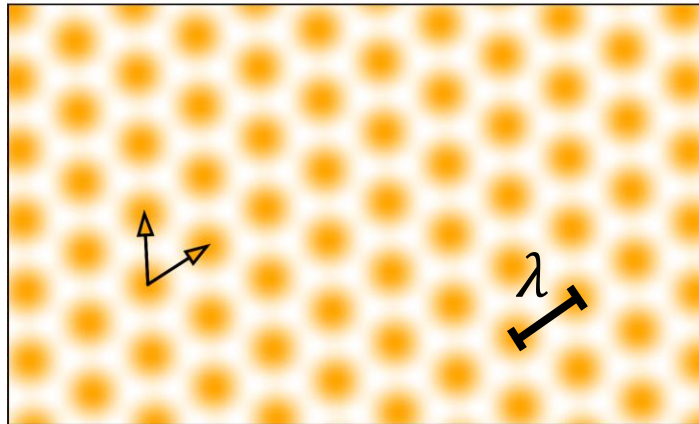
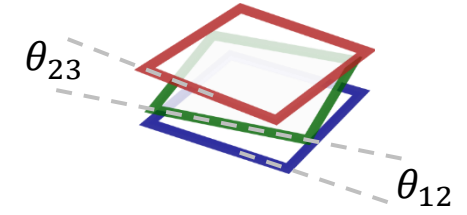
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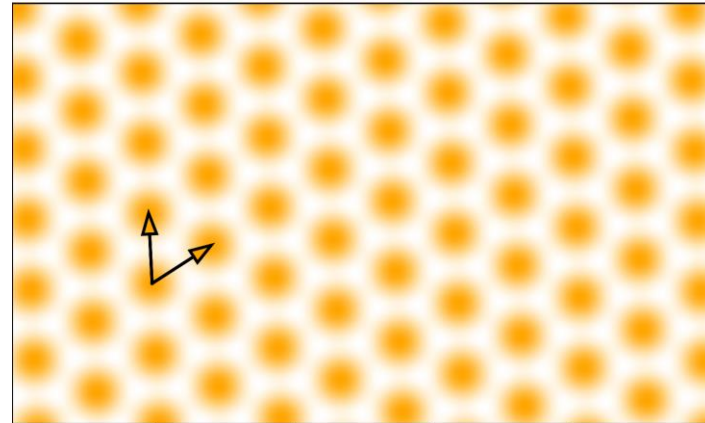
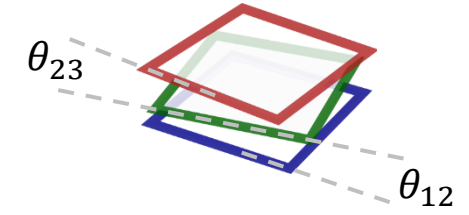
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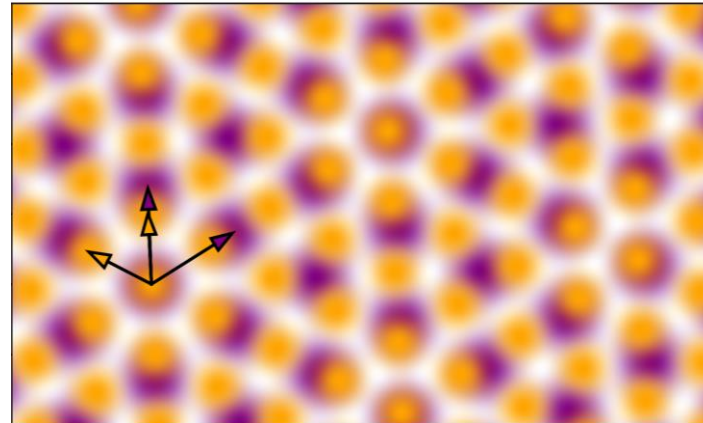
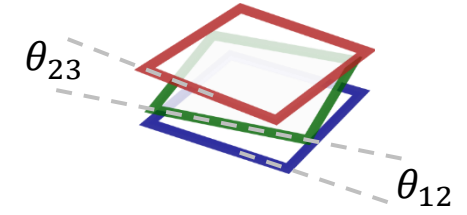
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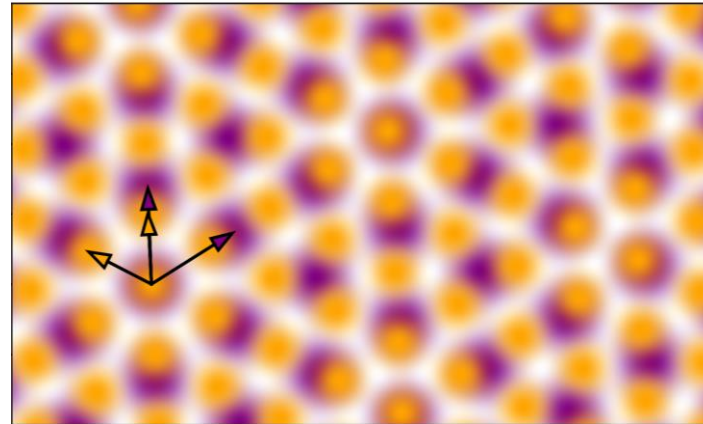
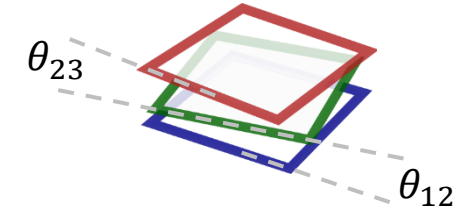
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From moiré to multimoiré



Moiré quasicrystal

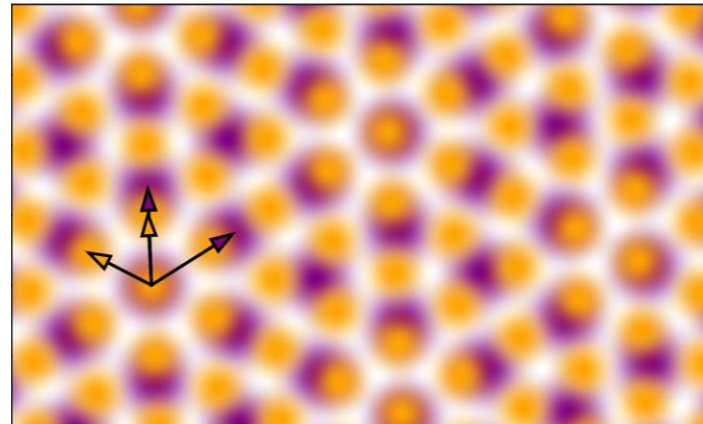
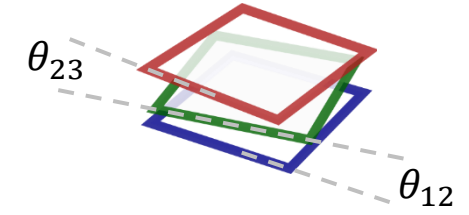
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Moiré quasicrystal

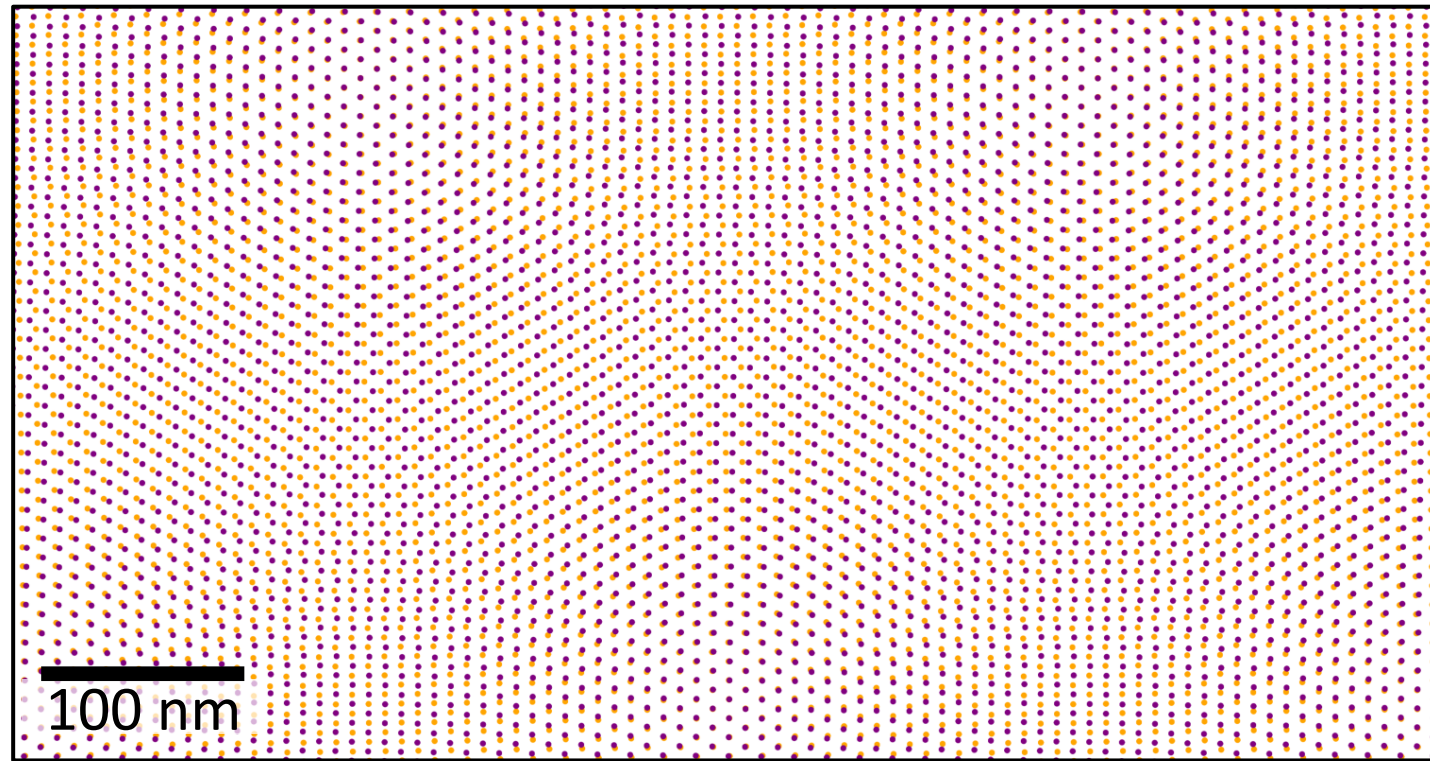
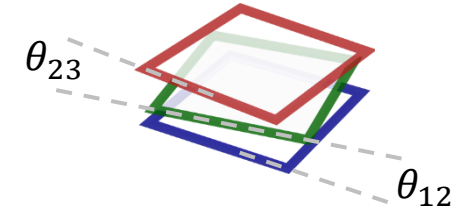
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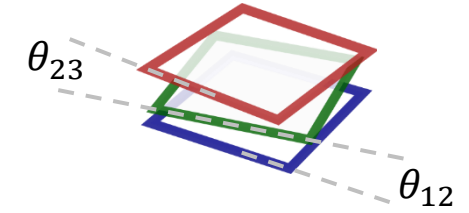
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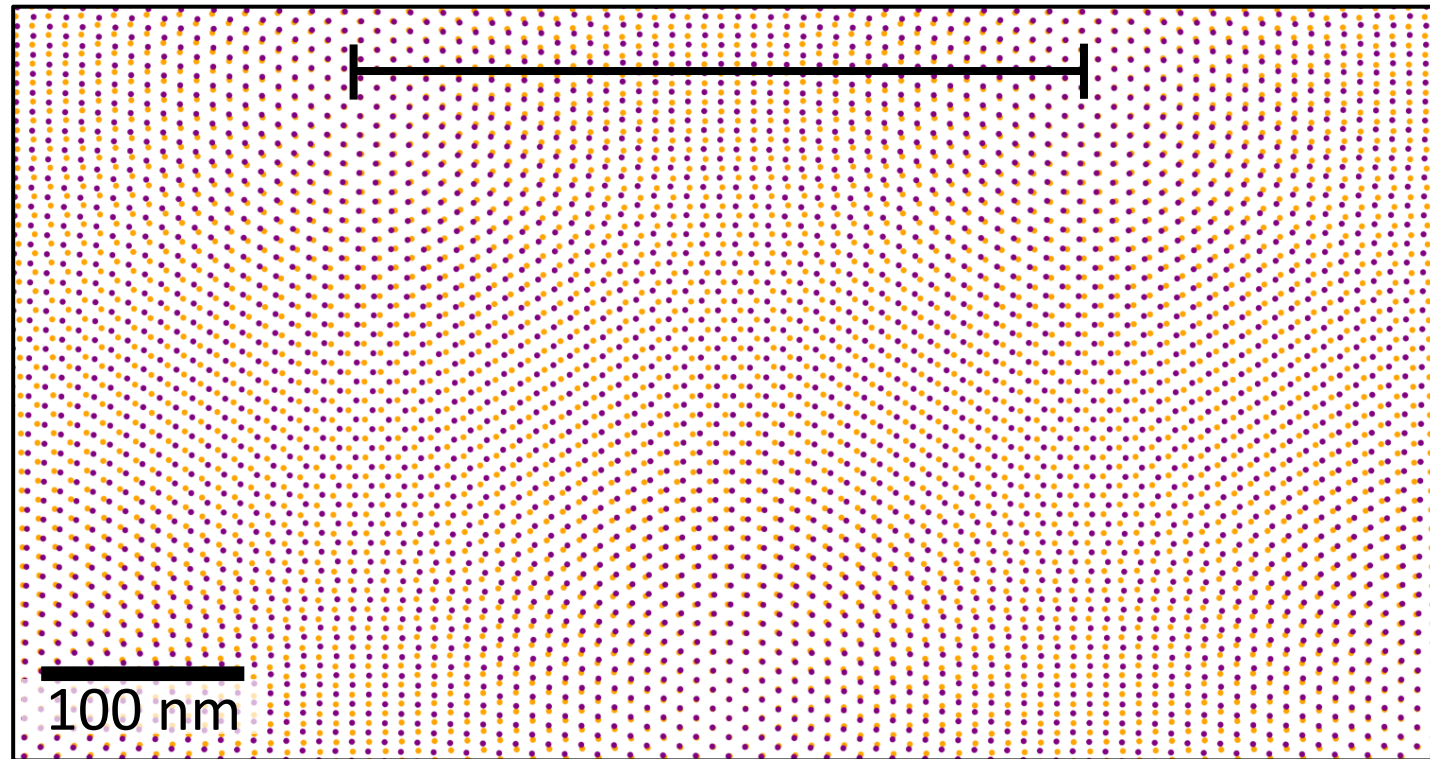
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● AA12 ● AA23

From moiré to multimoiré



$$\text{Supermoiré: } \lambda_{\text{sm}} = \frac{\lambda_{\text{m}}}{\theta} = \frac{a}{\theta^2}$$



● AA12 ● AA23

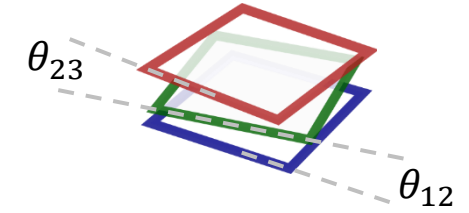
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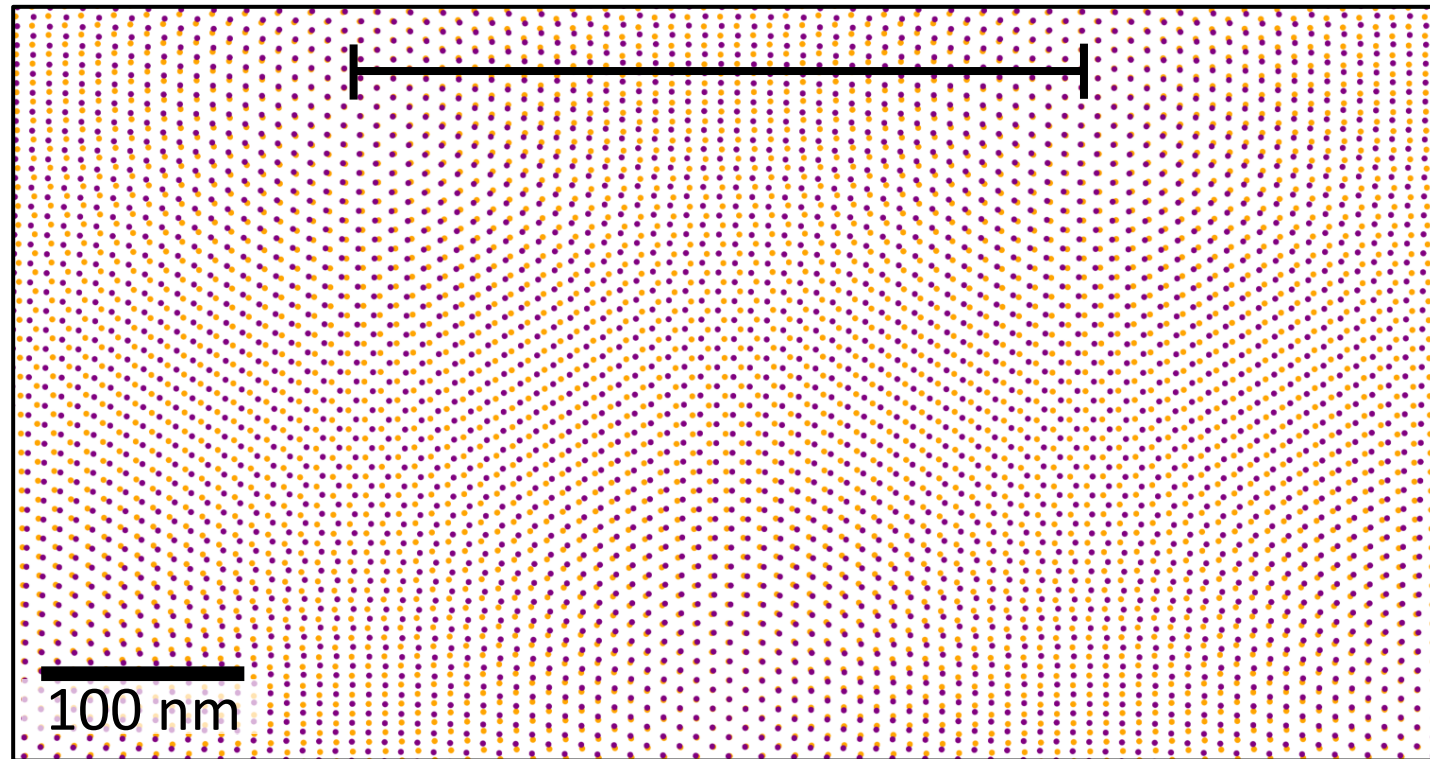
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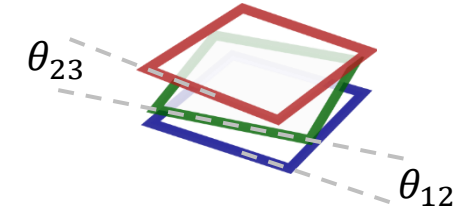
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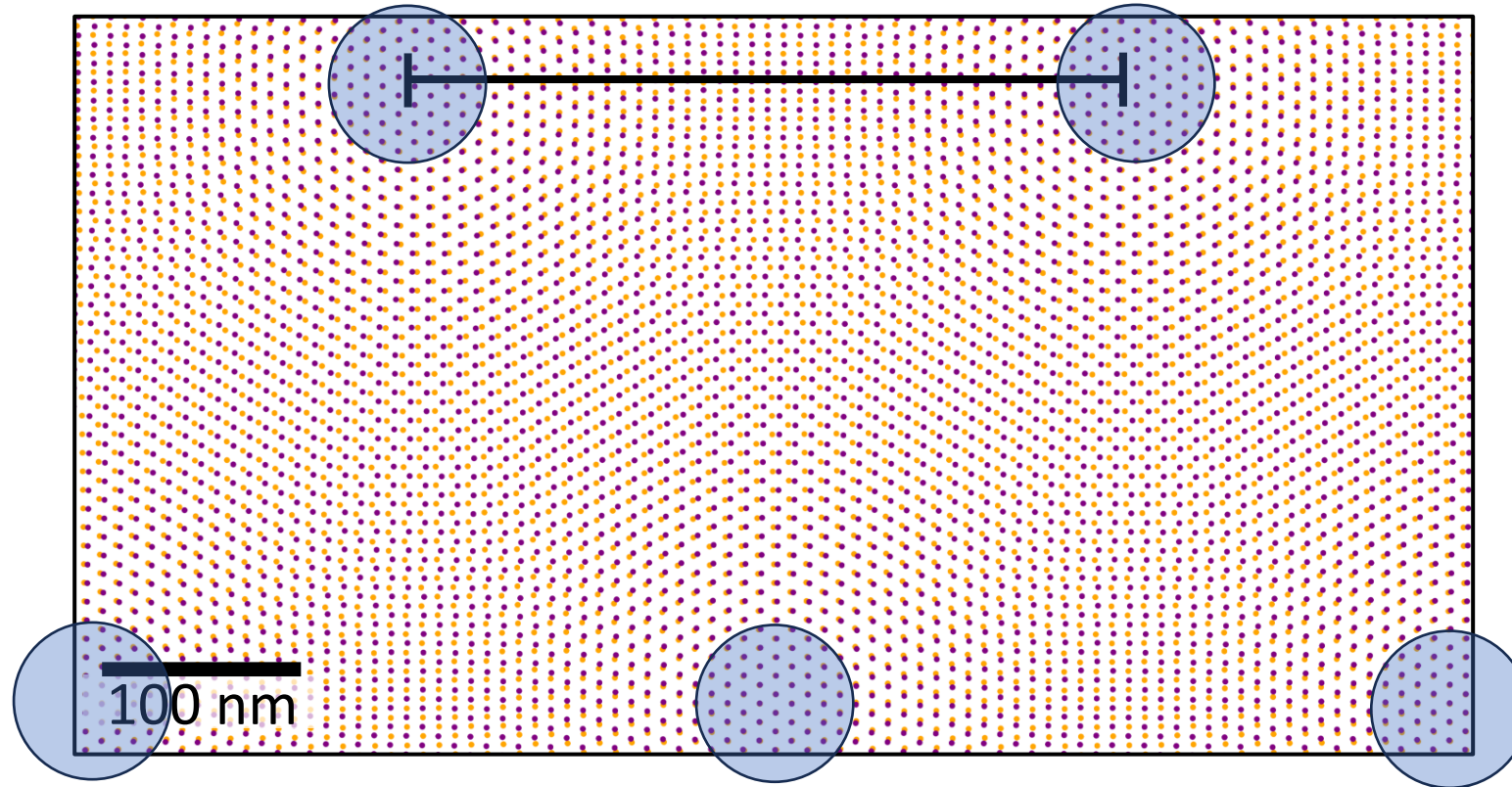
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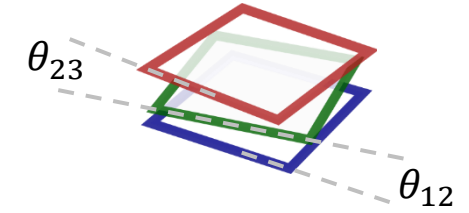
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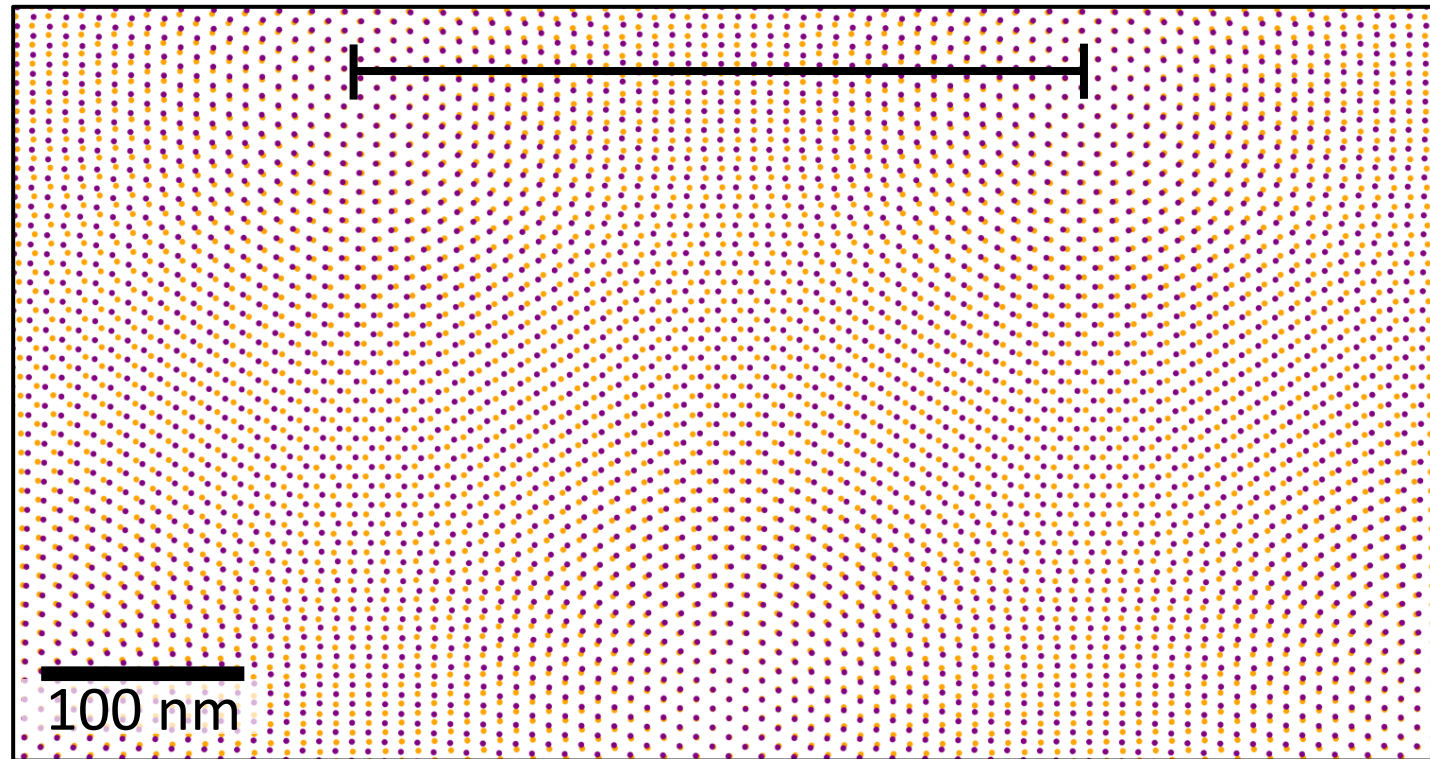
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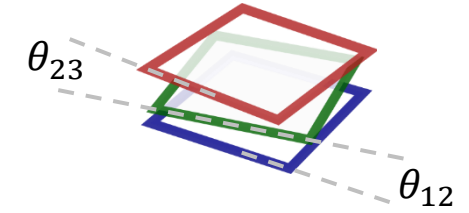
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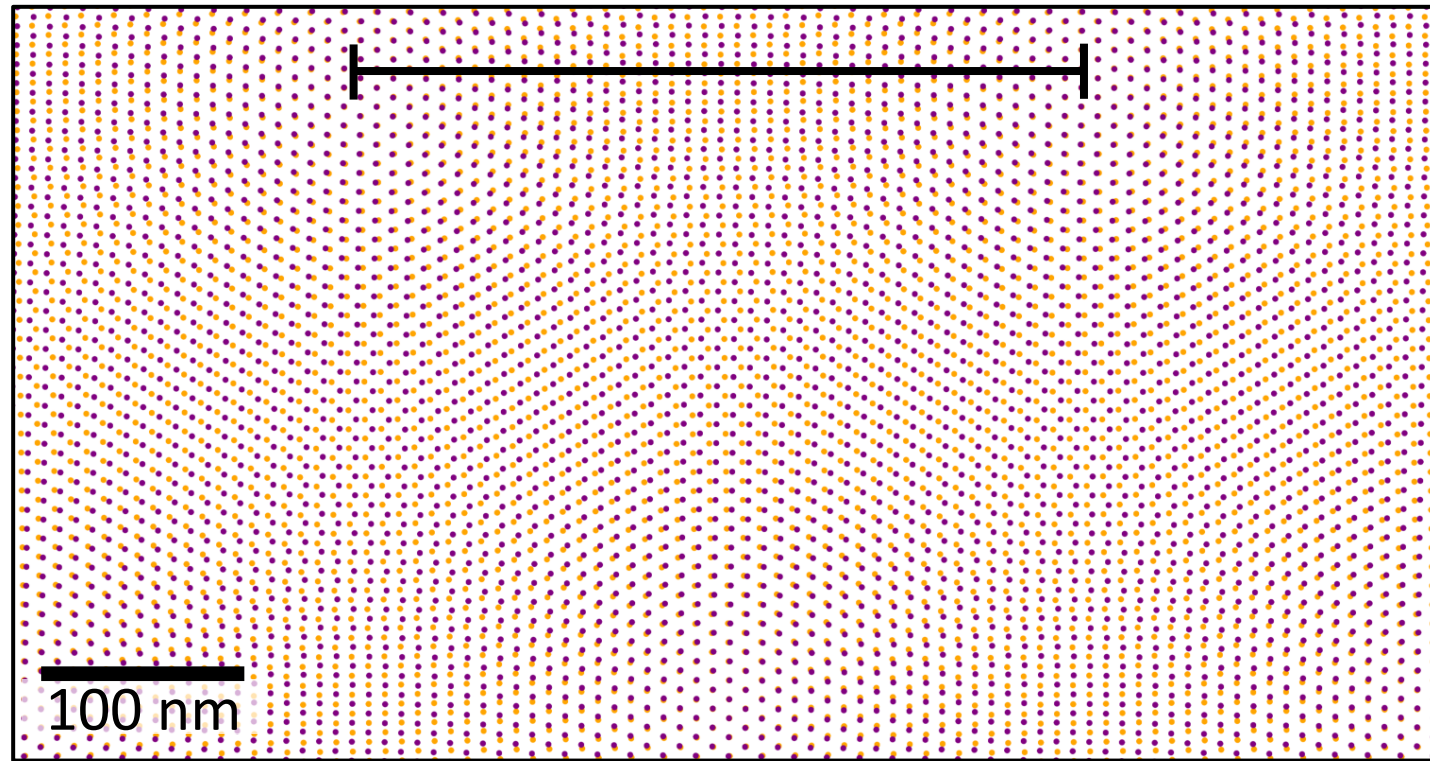
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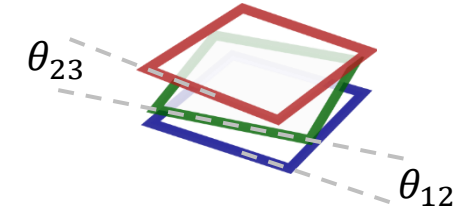
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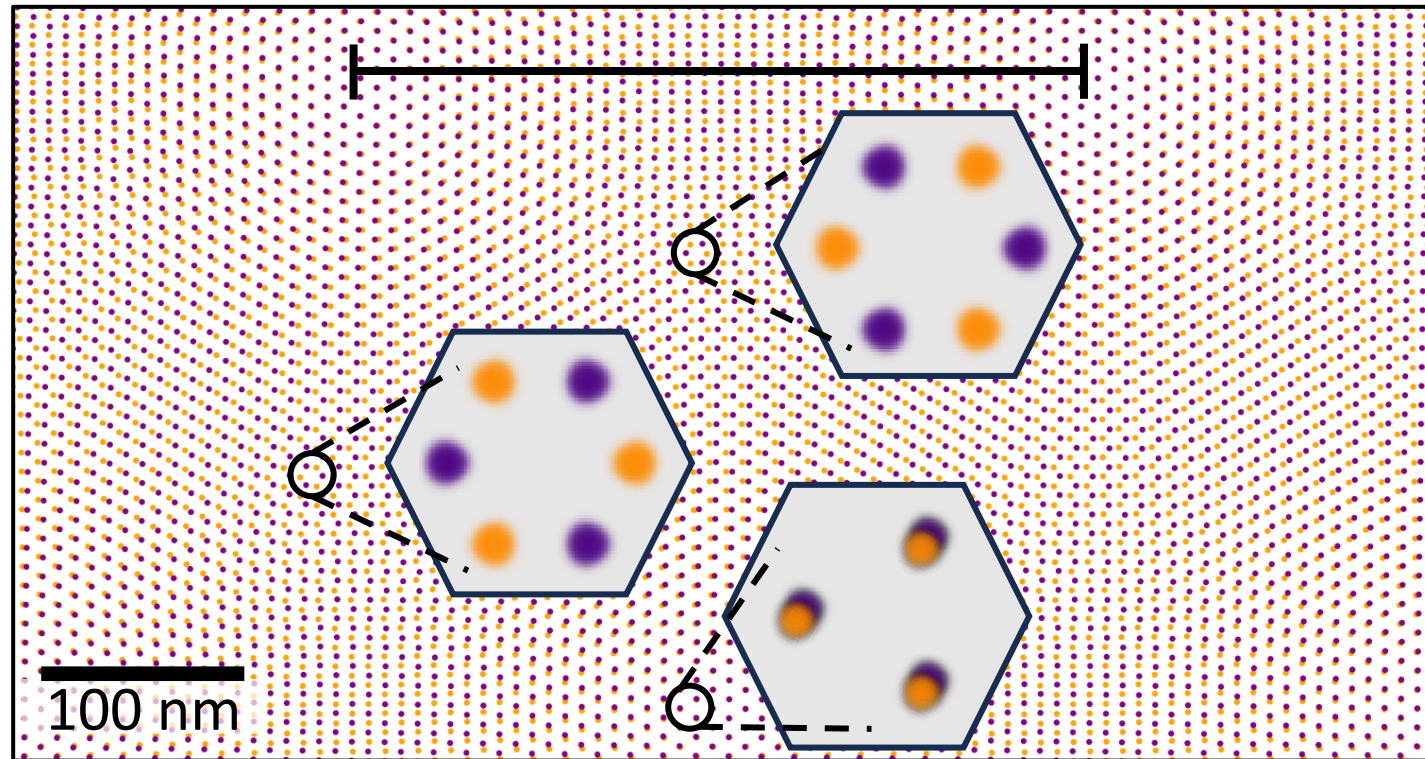
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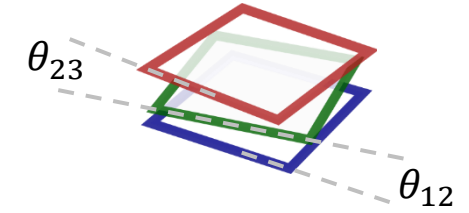
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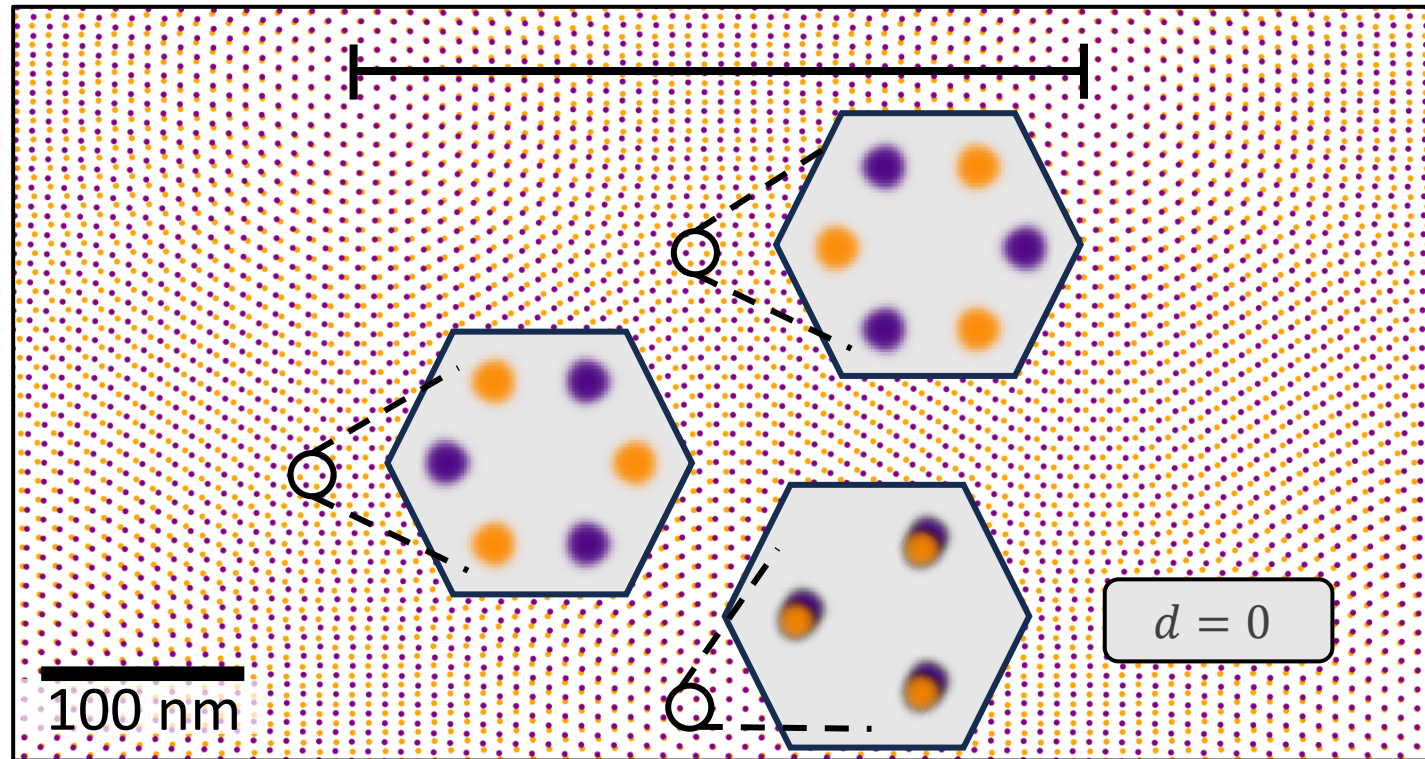
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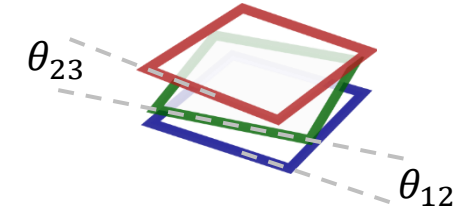
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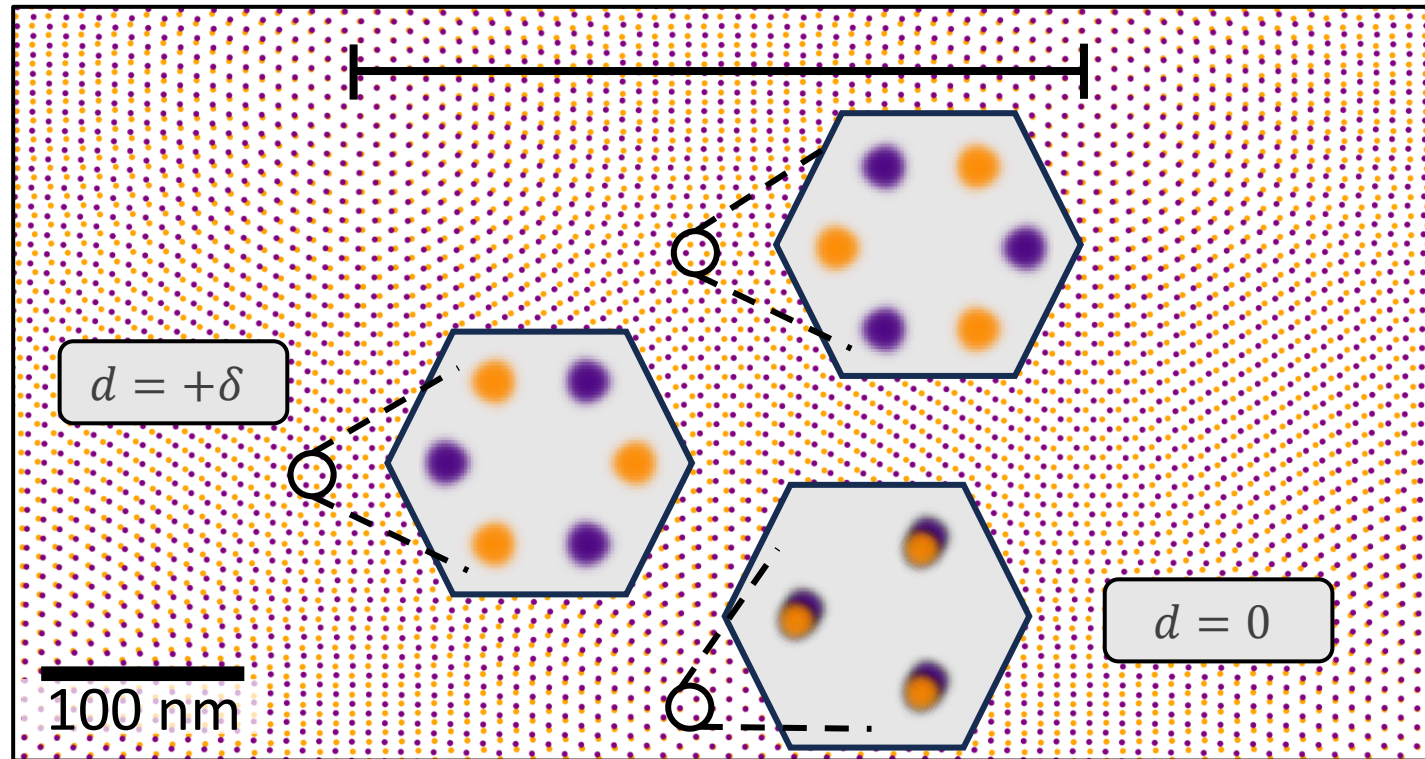
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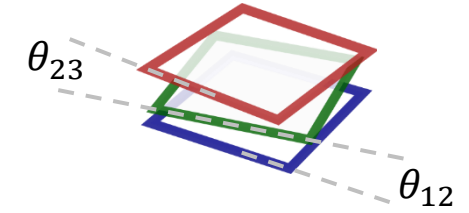
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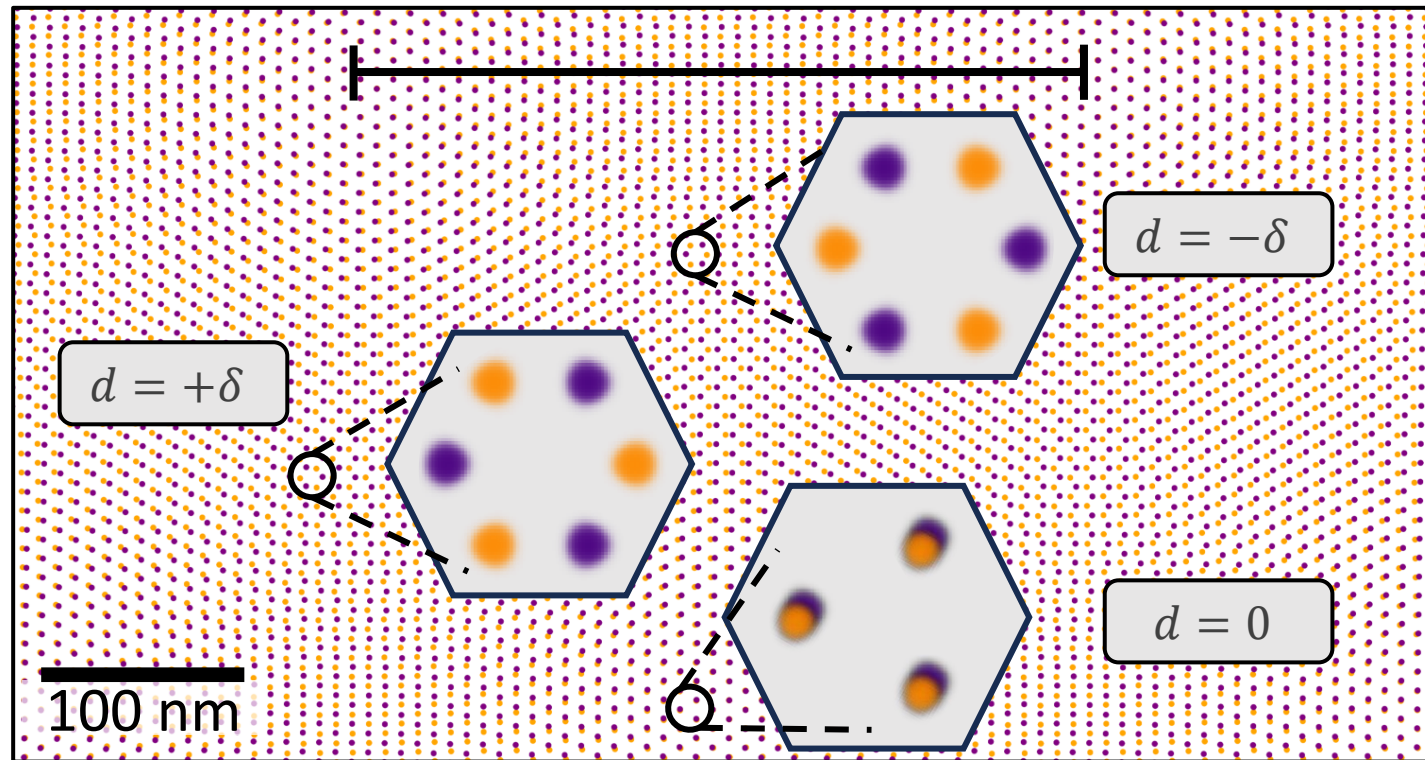
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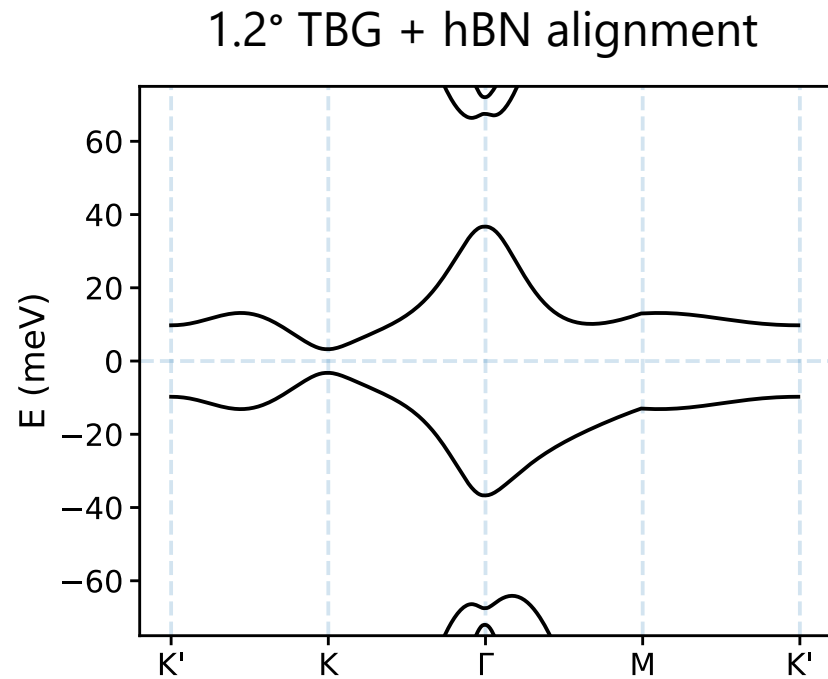
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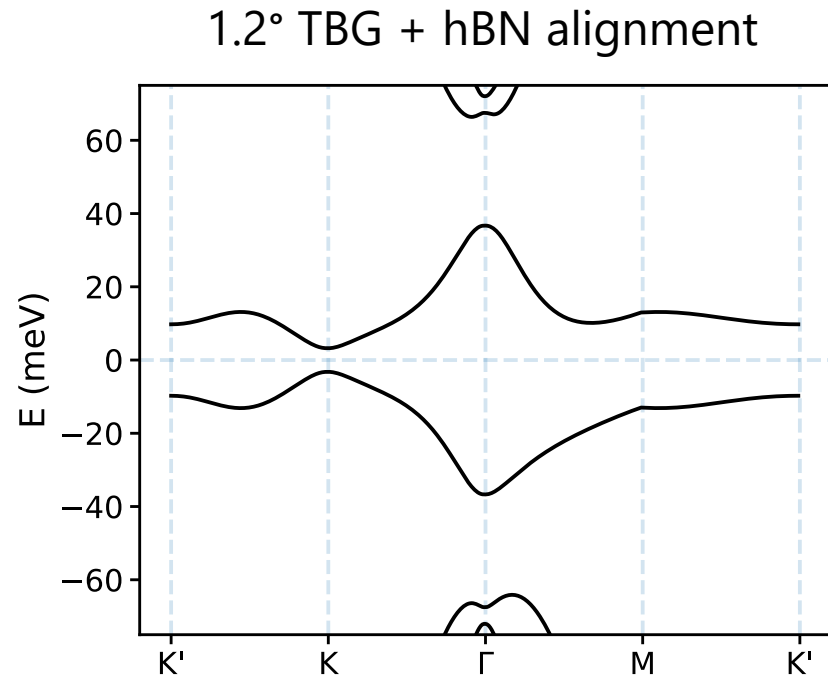
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TBG/hBN multimoiré



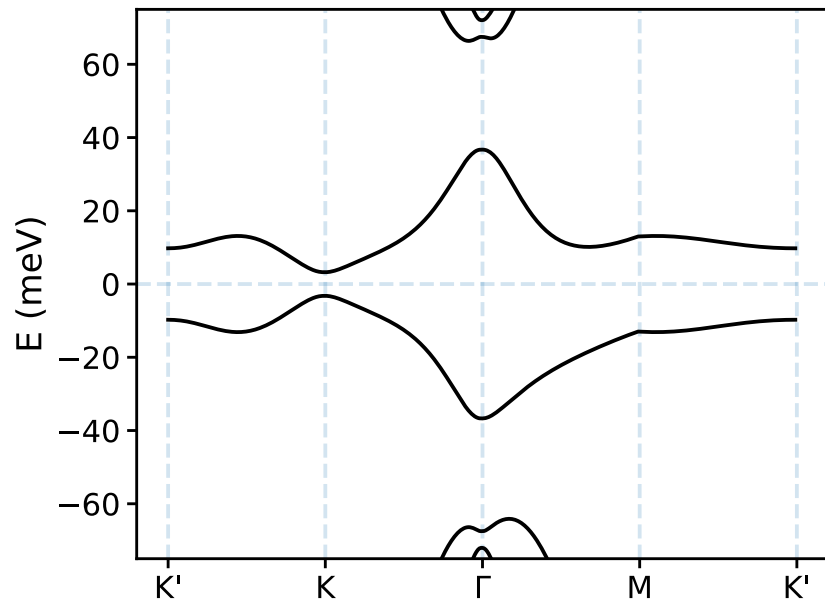
TBG/hBN multimoiré



$$V_{BN} = \sum_{\mathbf{k}} \psi_{1\mathbf{k}}^\dagger (m_0 \sigma^z) \psi_{1\mathbf{k}}$$

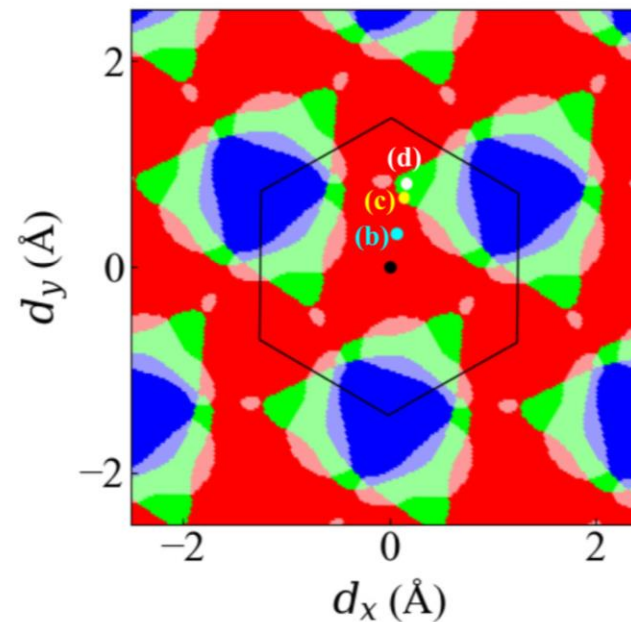
TBG/hBN multimoiré

1.2° TBG + hBN alignment



$$V_{BN} = \sum_{\mathbf{k}} \psi_{1\mathbf{k}}^\dagger (m_0 \sigma^z) \psi_{1\mathbf{k}}$$

120° commensurate, $U = 0$

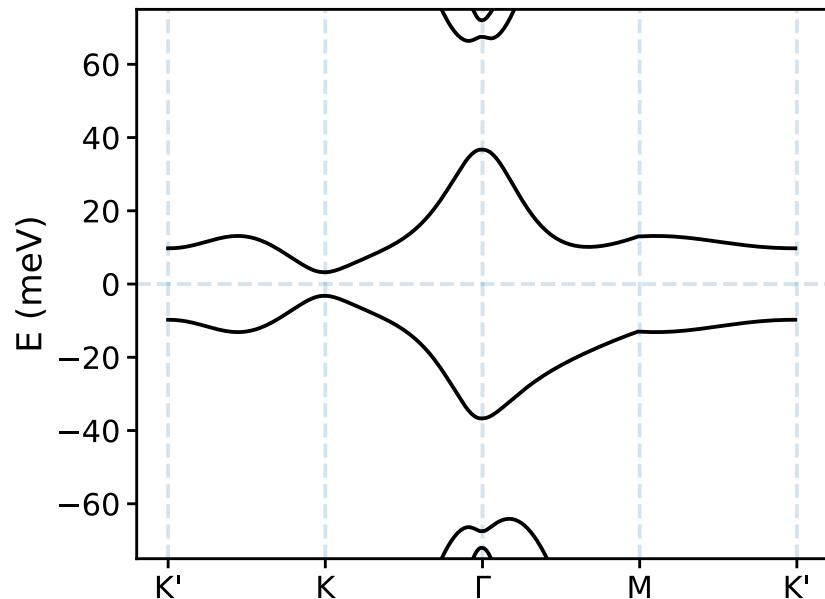


■ $C = +1$
 ■ $C = 0$
 ■ $C = -1$

$$V_{BN}(\mathbf{d}) = \sum_{\mathbf{k}} \left(\psi_{1\mathbf{k}}^\dagger (m_0 \sigma^z) \psi_{1\mathbf{k}} + \sum_{j=1} \psi_{1\mathbf{k}}^\dagger V_j(\mathbf{d}) \psi_{1(\mathbf{k}+\mathbf{g}_j)} \right)$$

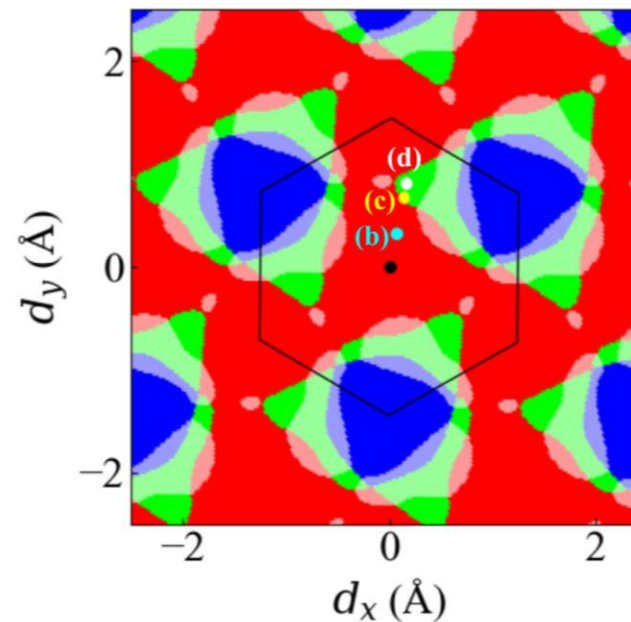
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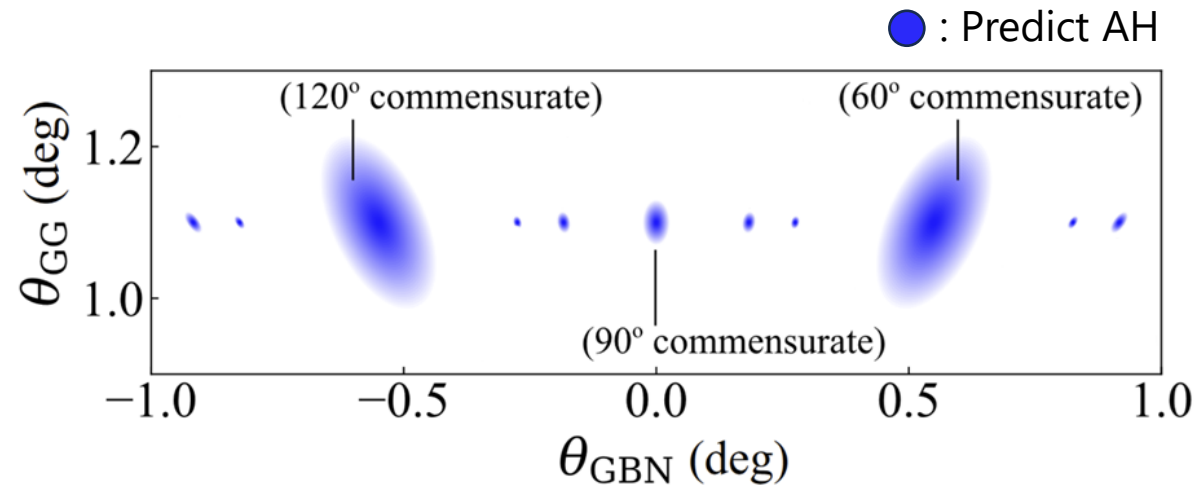
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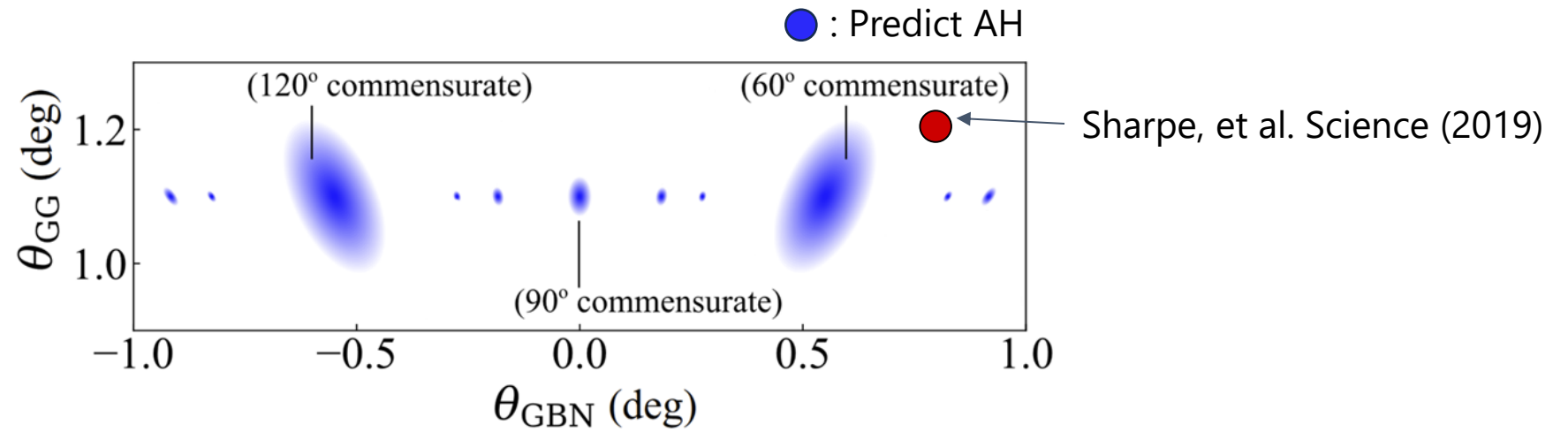
We must take the mesoscopics seriously!
 Previous treatment too simplistic

TBG/hBN multimoiré

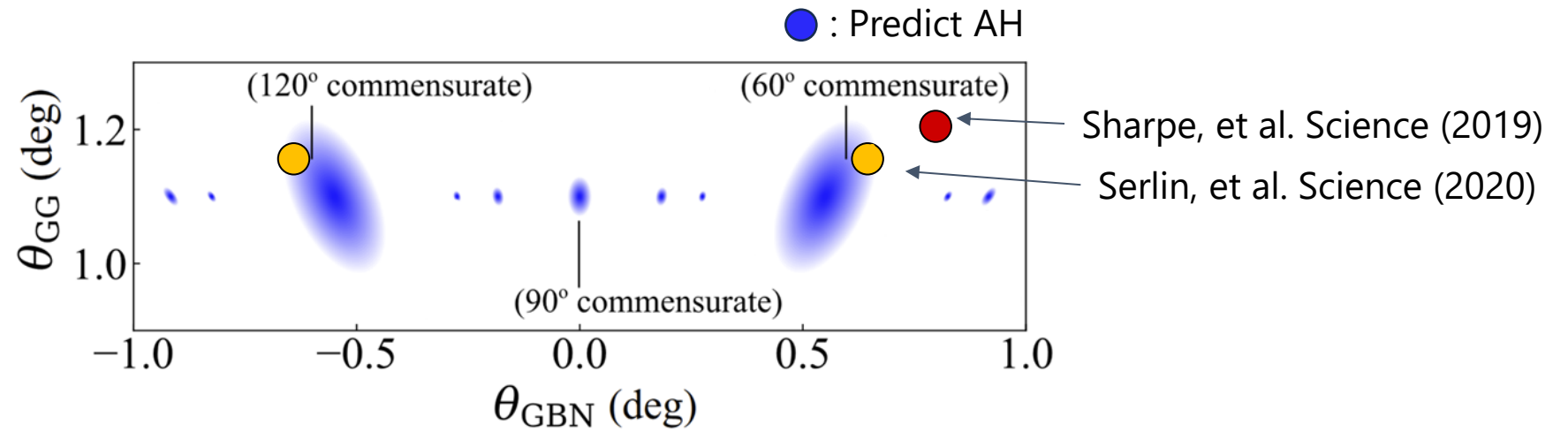
TBG/hBN multimoiré



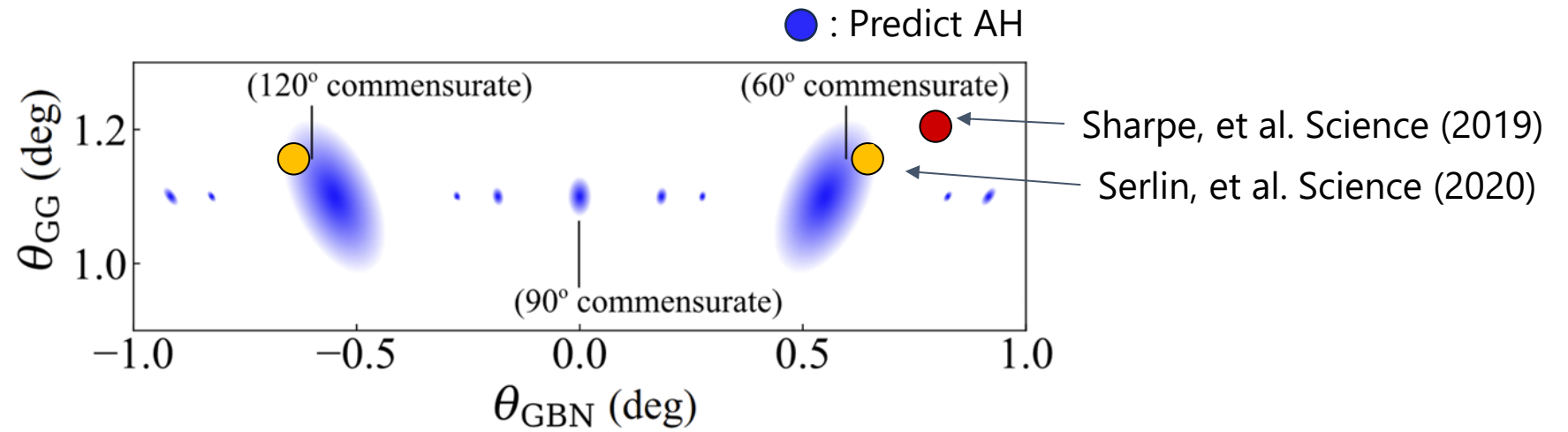
TBG/hBN multimoiré



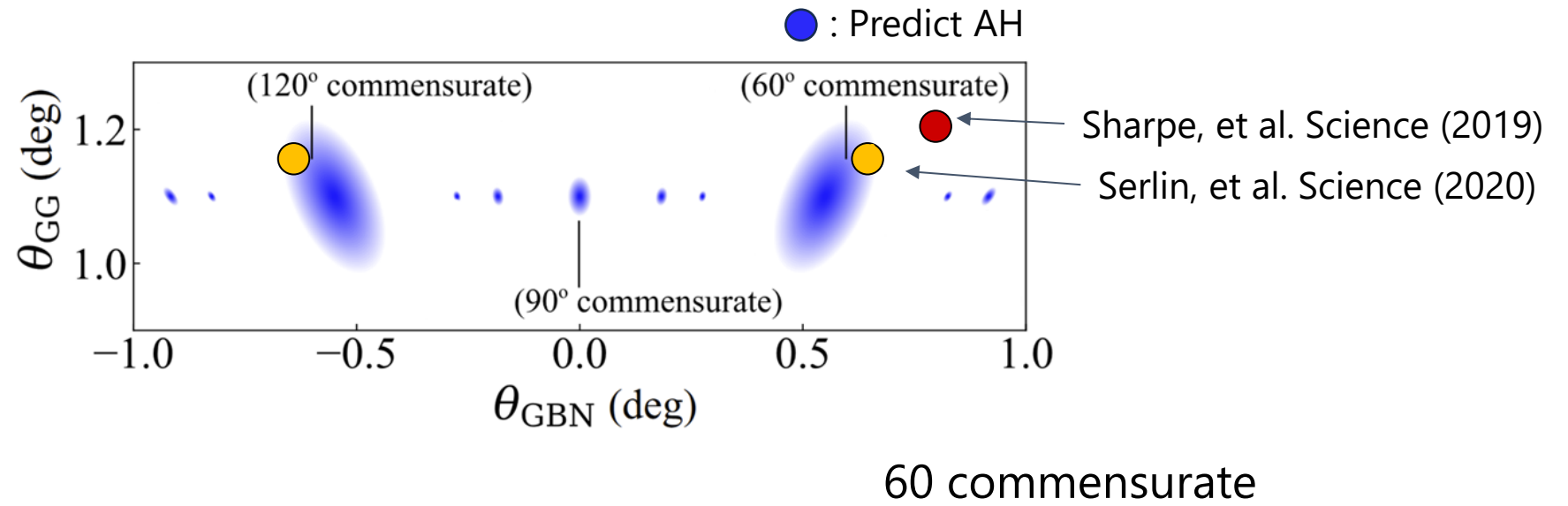
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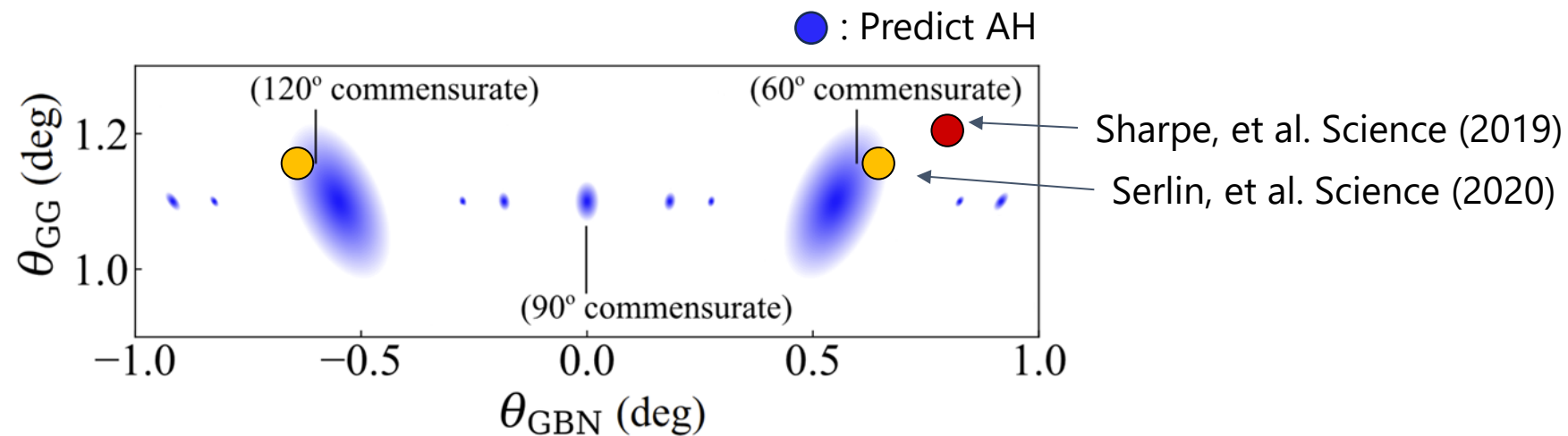
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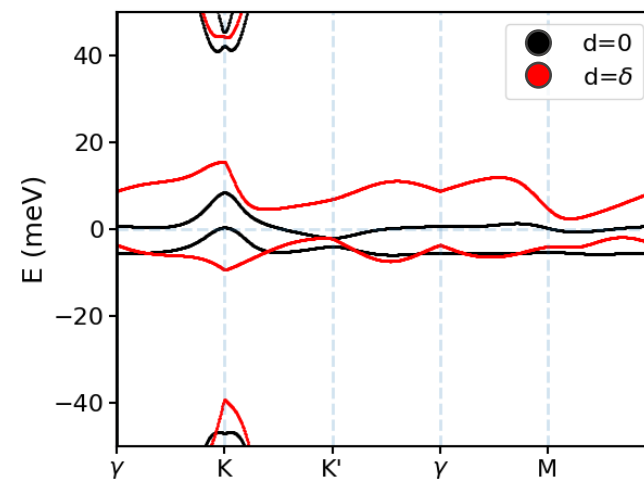
TBG/hBN multimoiré



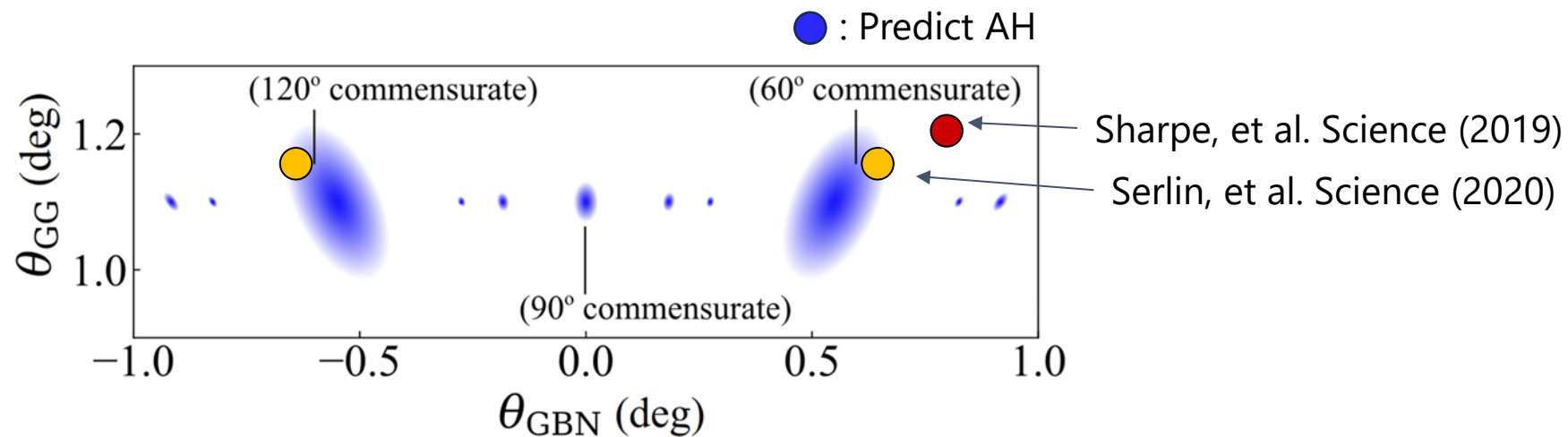
TBG/hBN multimoiré



60 commensurate

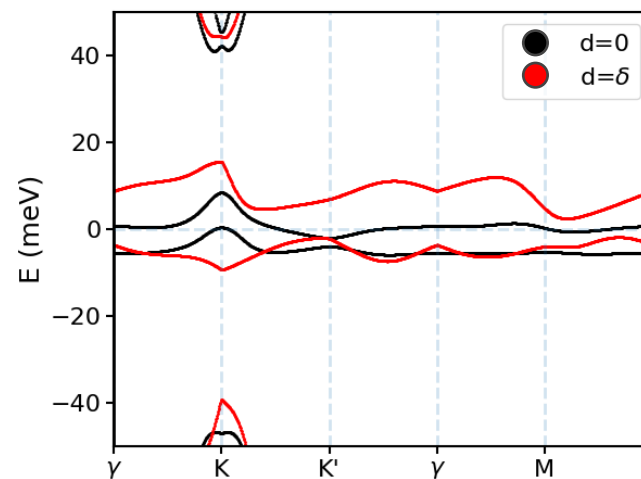


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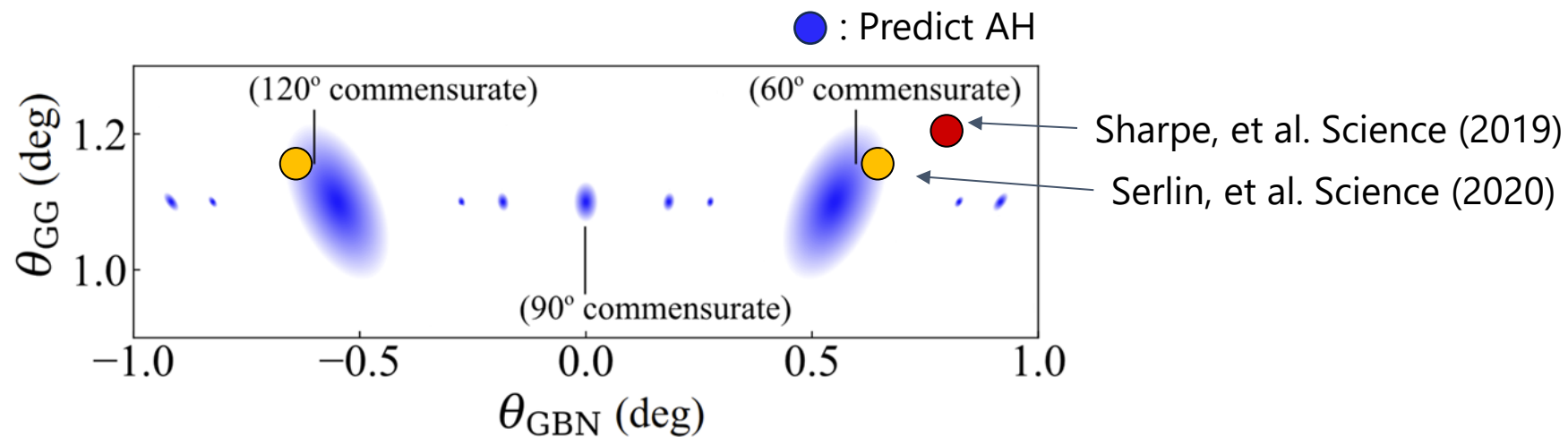


120 commensurate

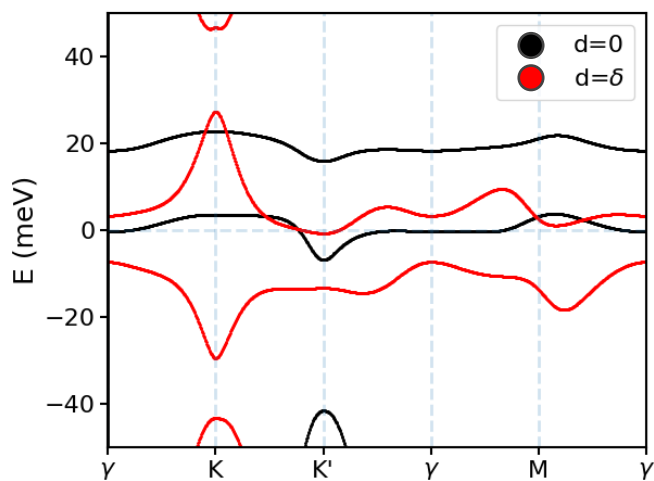
60 commensurate



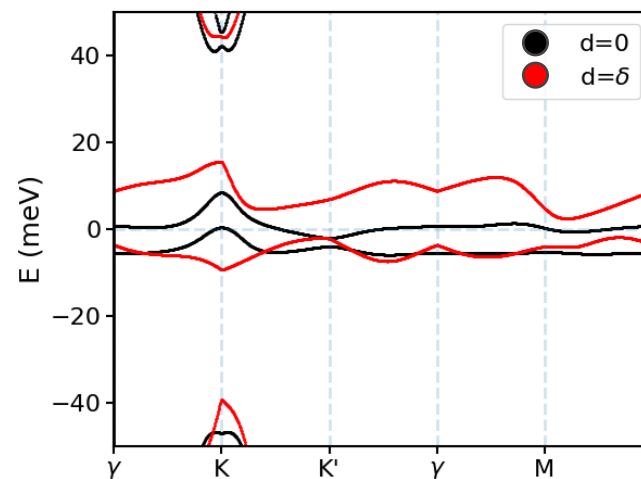
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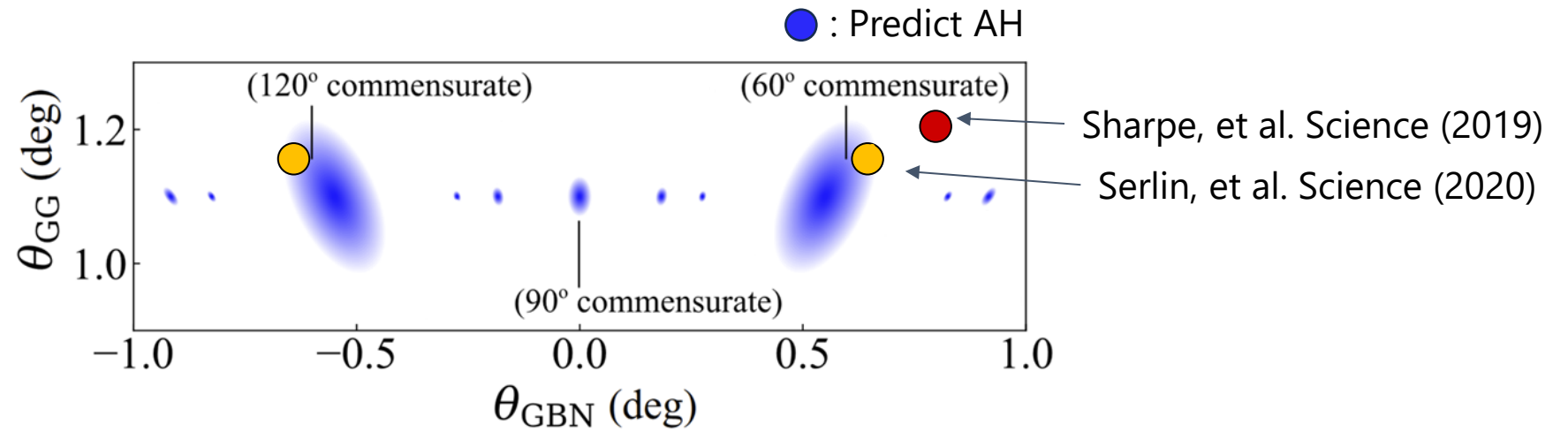
120 commensurate



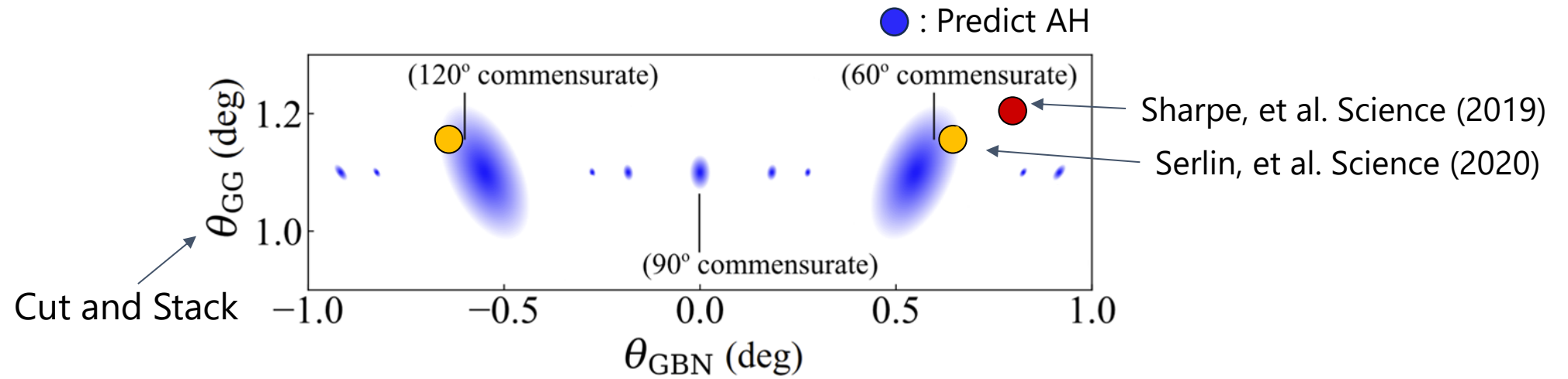
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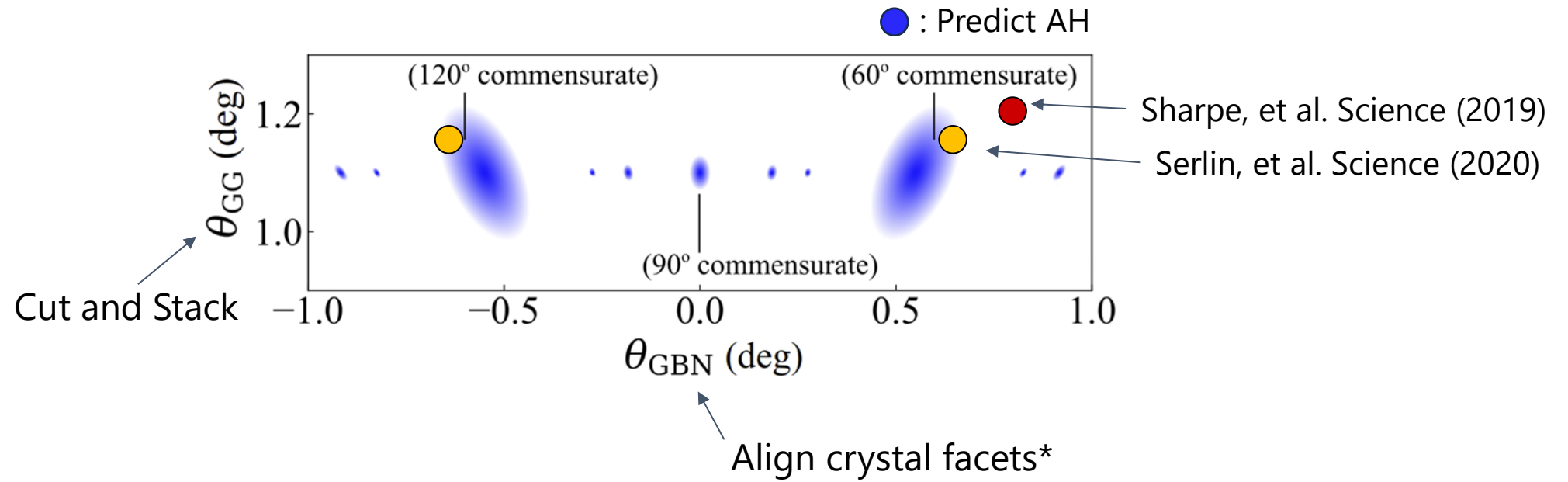
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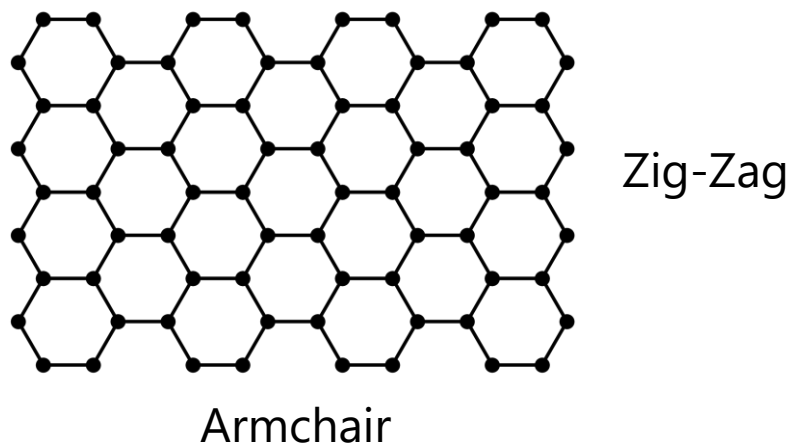
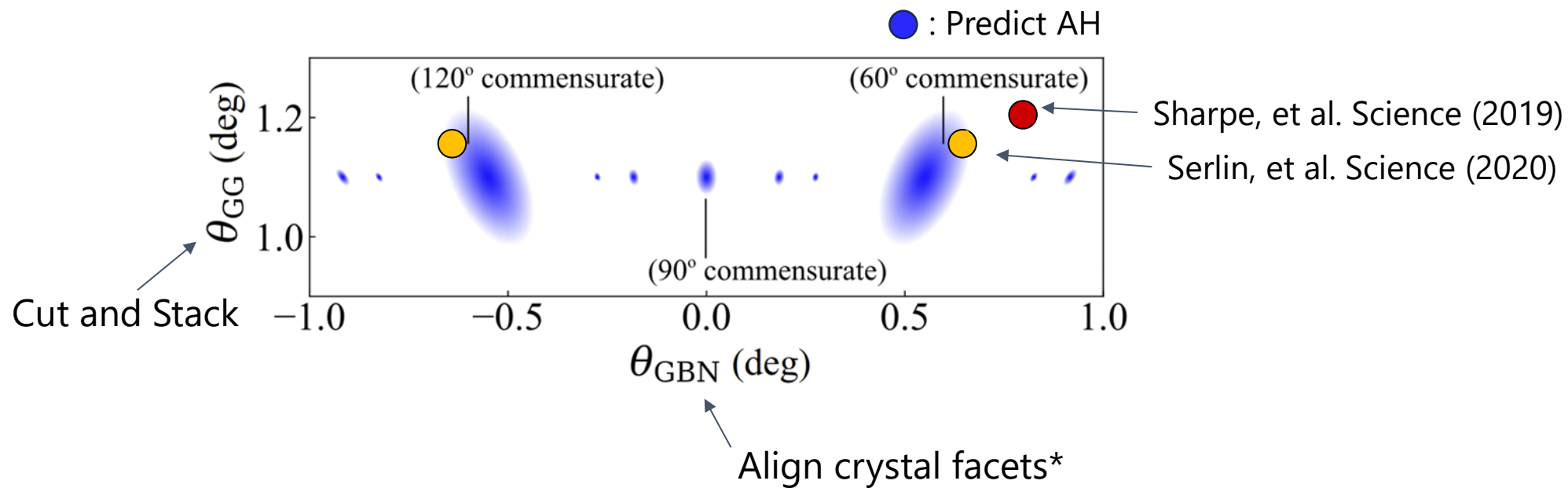
TBG/hBN multimoiré



TBG/hBN multimoiré

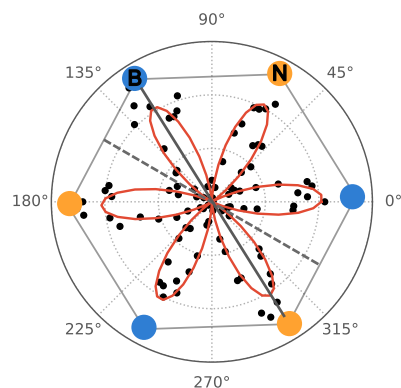
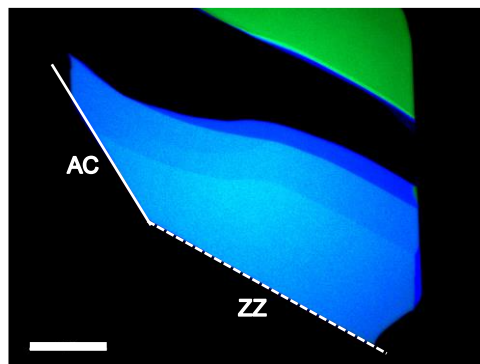


TBG/hBN multimoiré



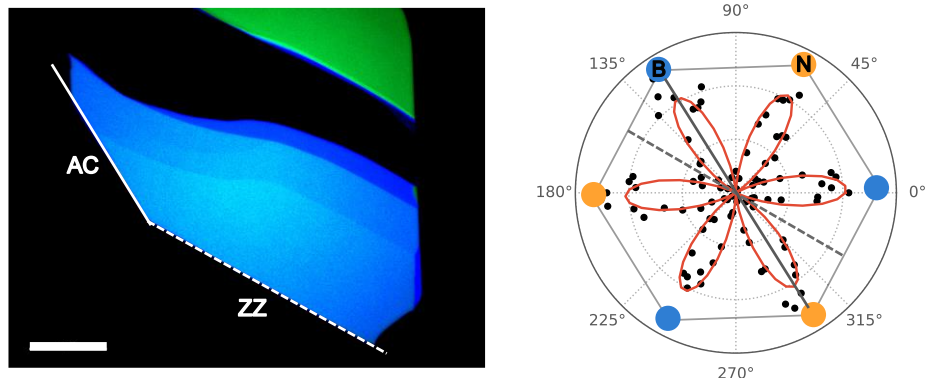
Deterministic fab with rapid feedback

Second harmonic generation for hBN

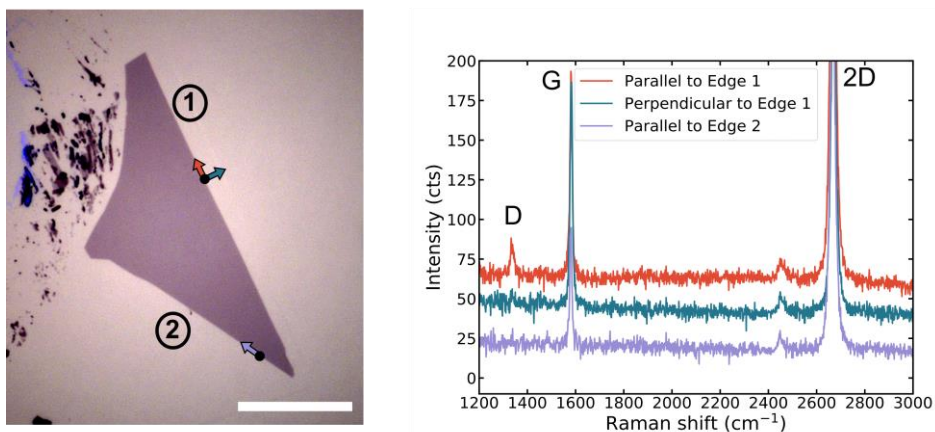


Deterministic fab with rapid feedback

Second harmonic generation for hBN

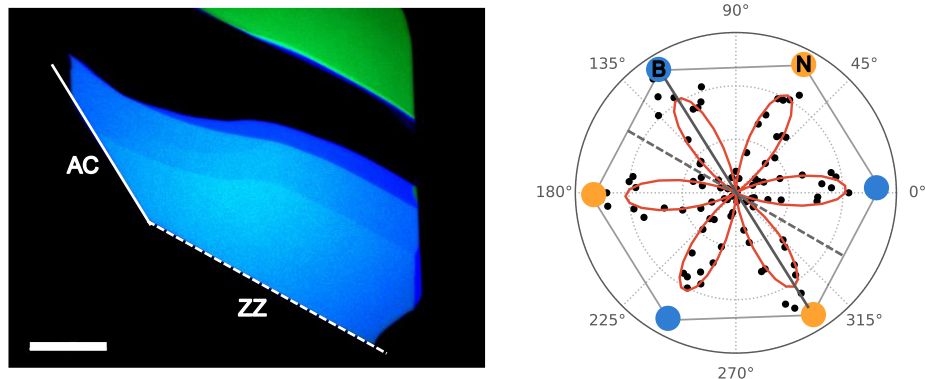


Polarized Raman for graphene

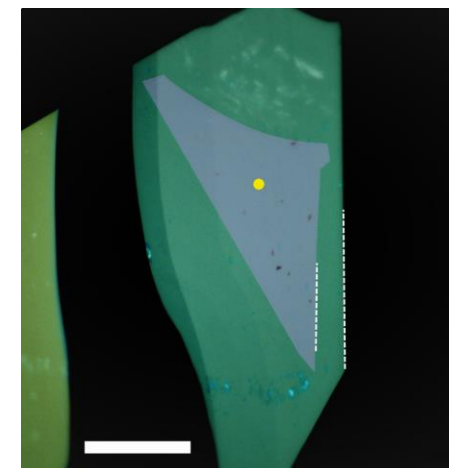


Deterministic fab with rapid feedback

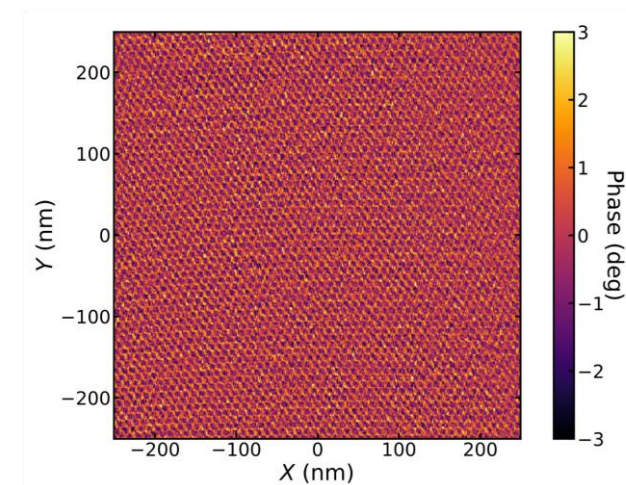
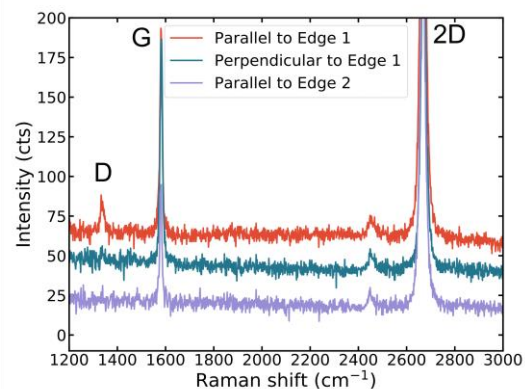
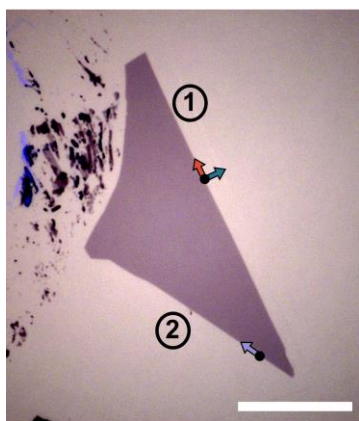
Second harmonic generation for hBN



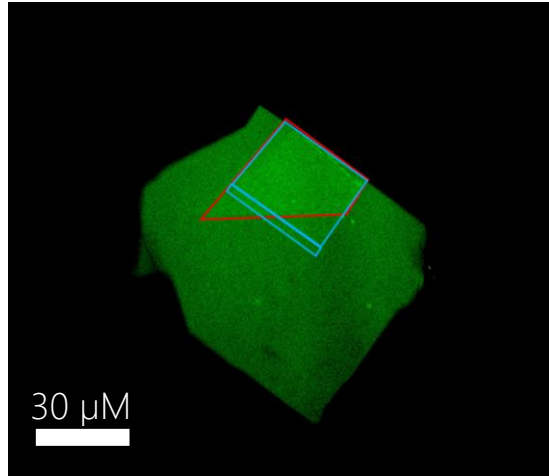
Torsional force microscopy for moirés



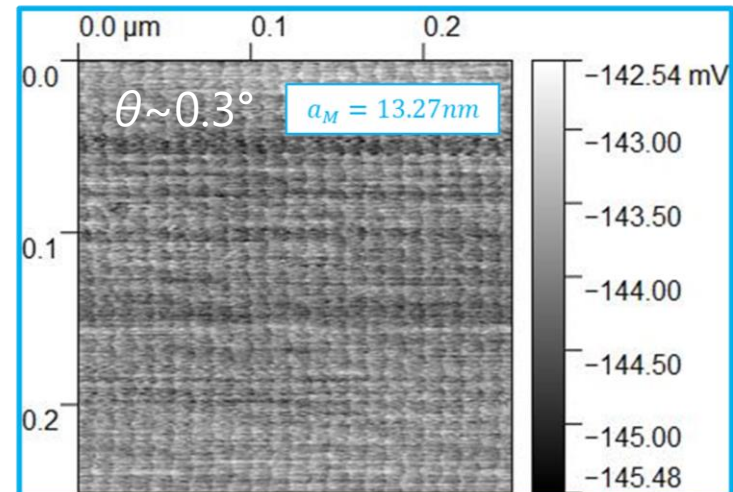
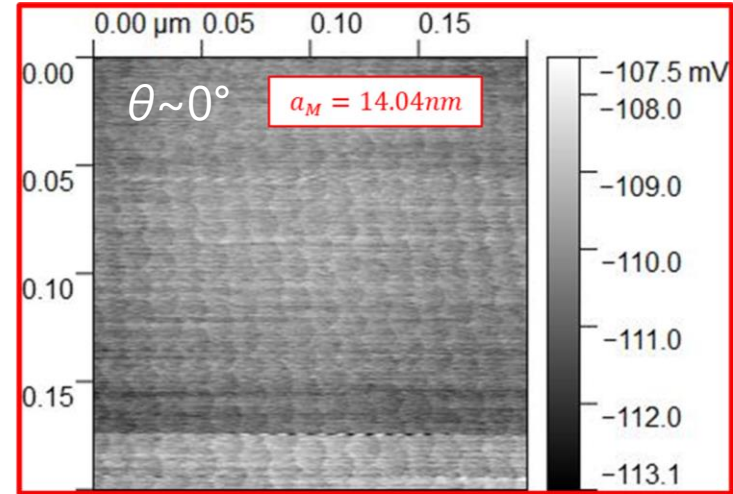
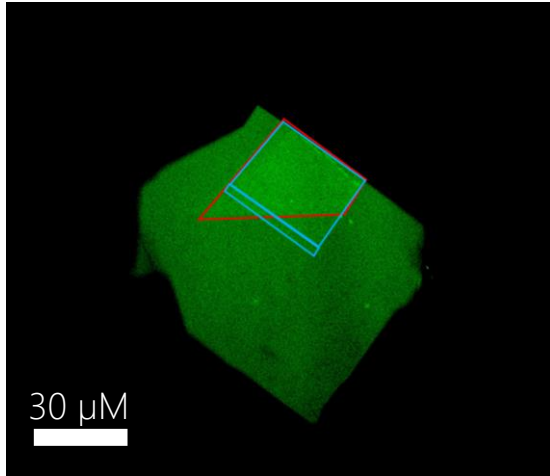
Polarized Raman for graphene



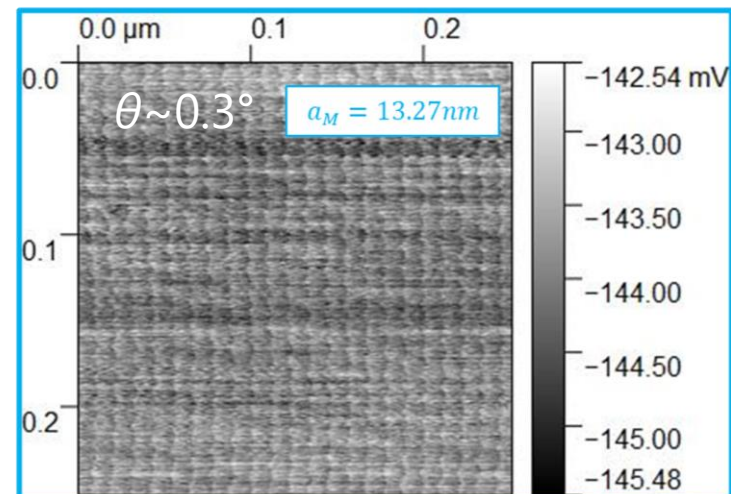
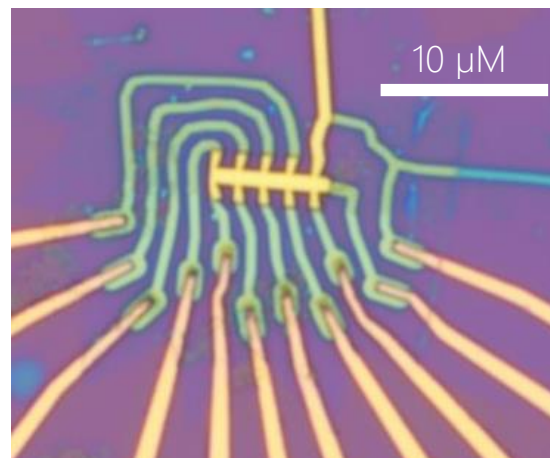
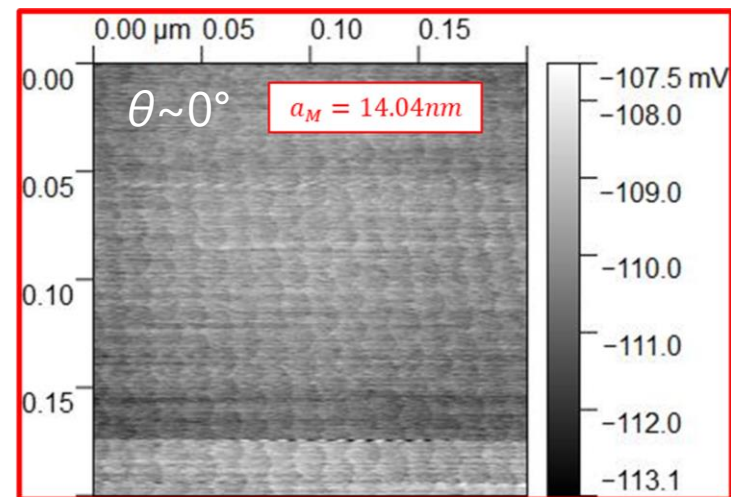
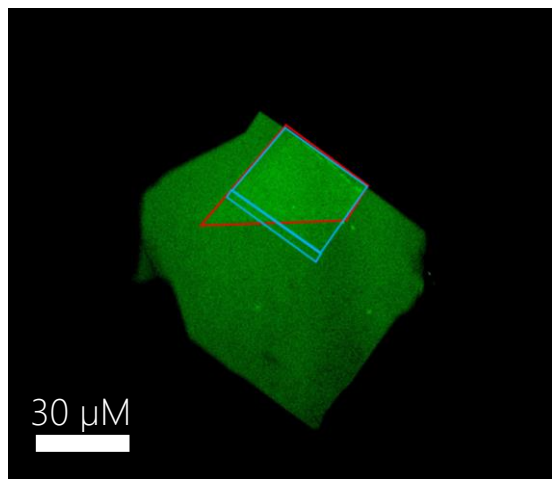
Deterministic fab with rapid feedback



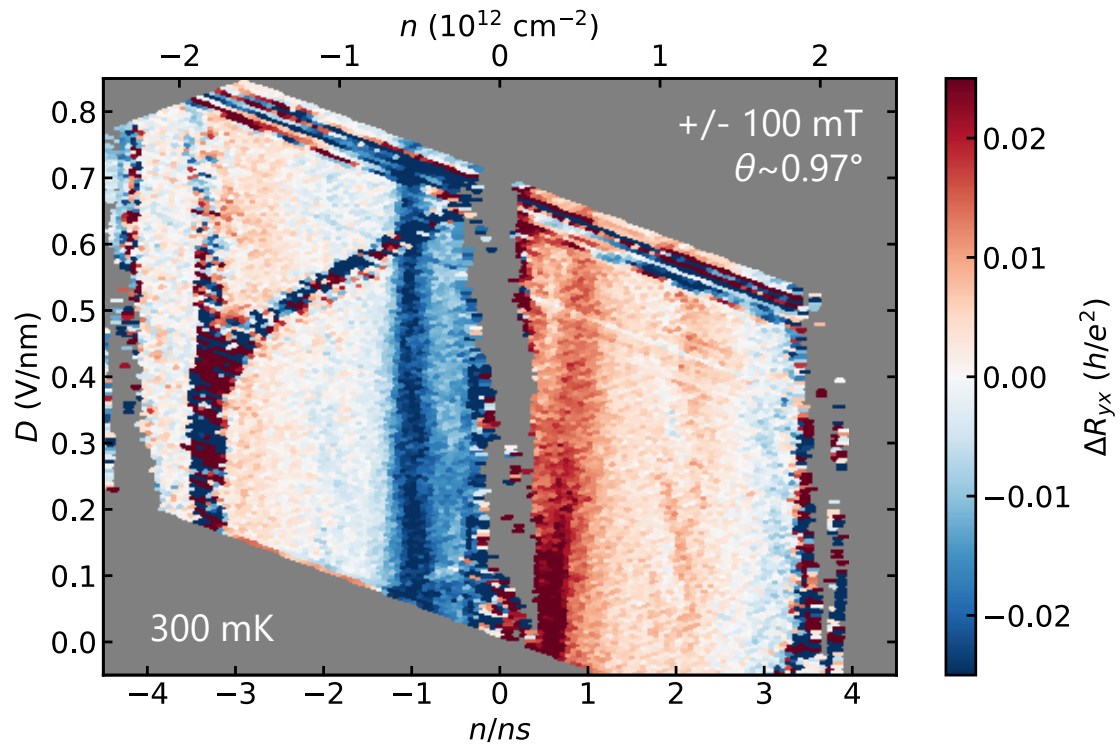
Deterministic fab with rapid feedback



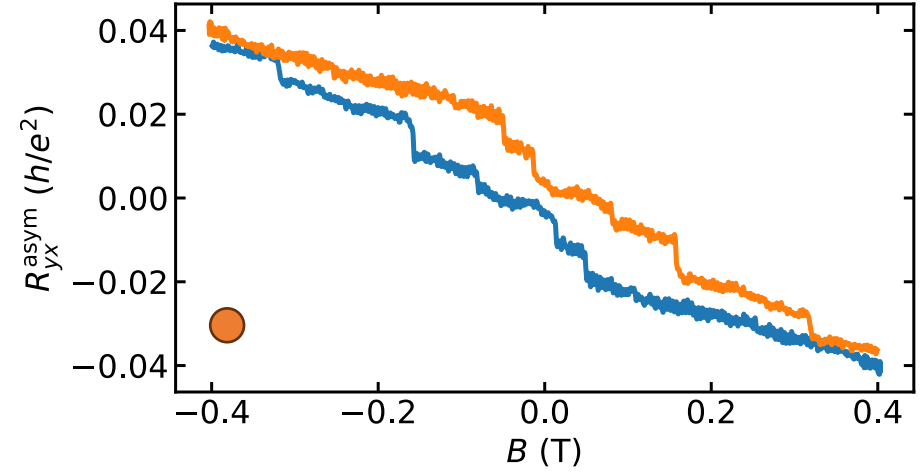
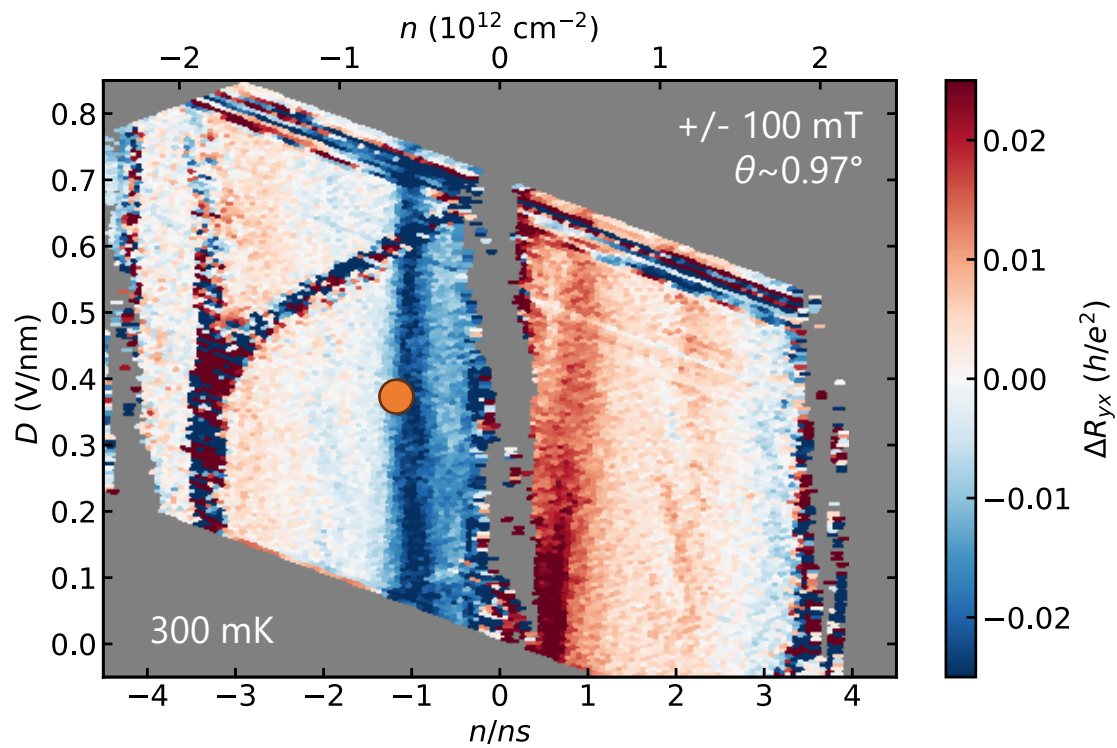
Deterministic fab with rapid feedback



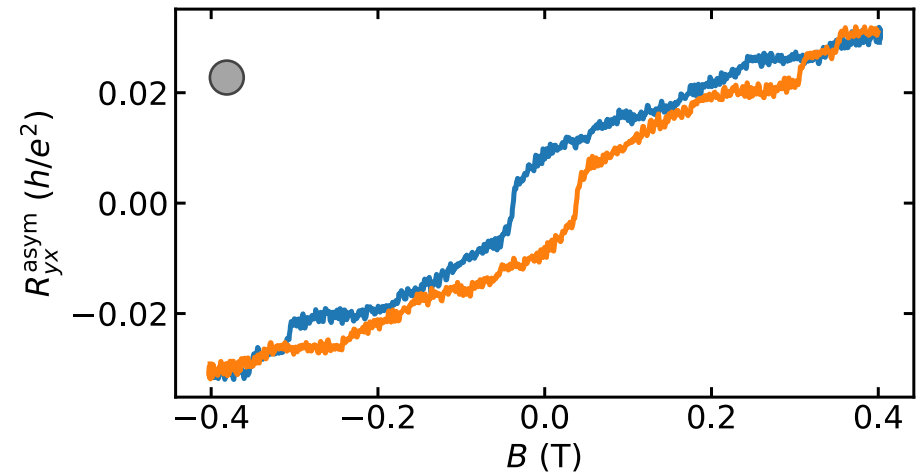
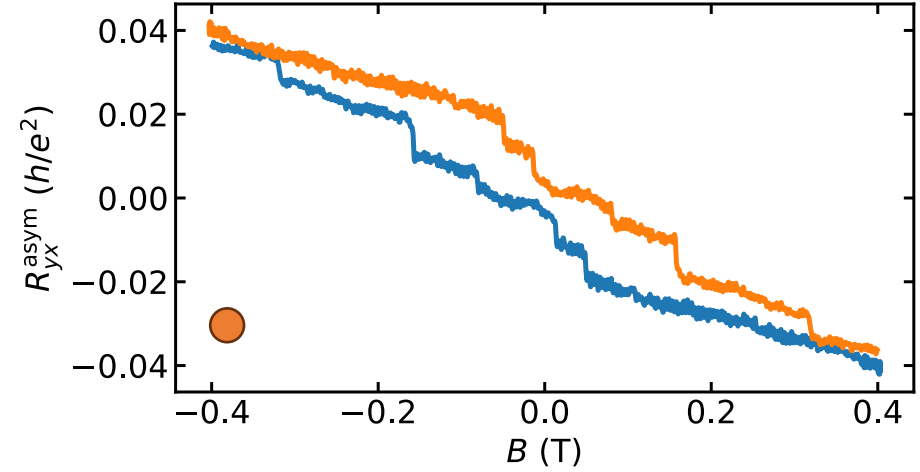
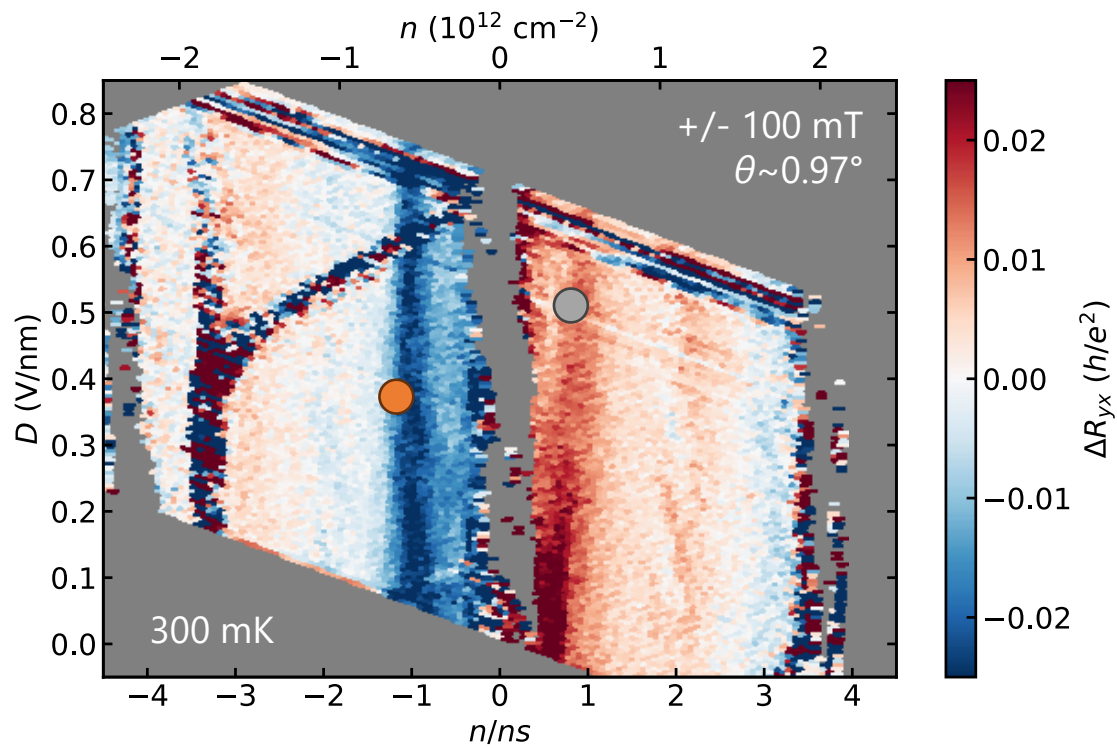
Anomalous Hall!



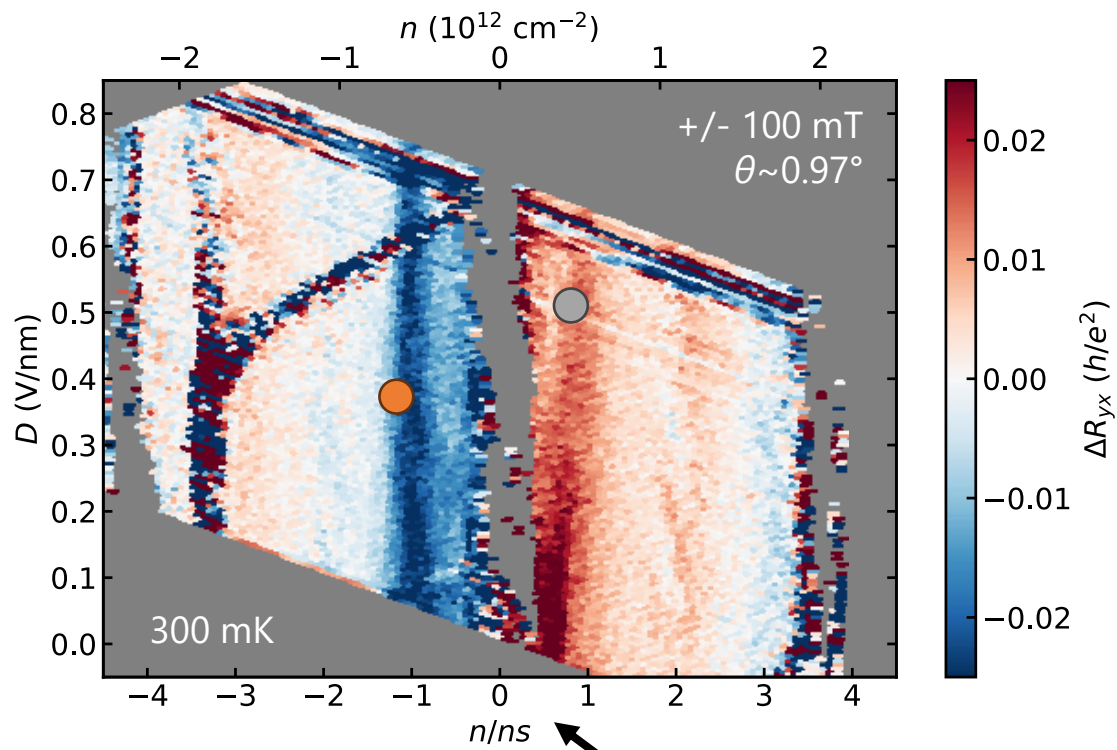
Anomalous Hall!



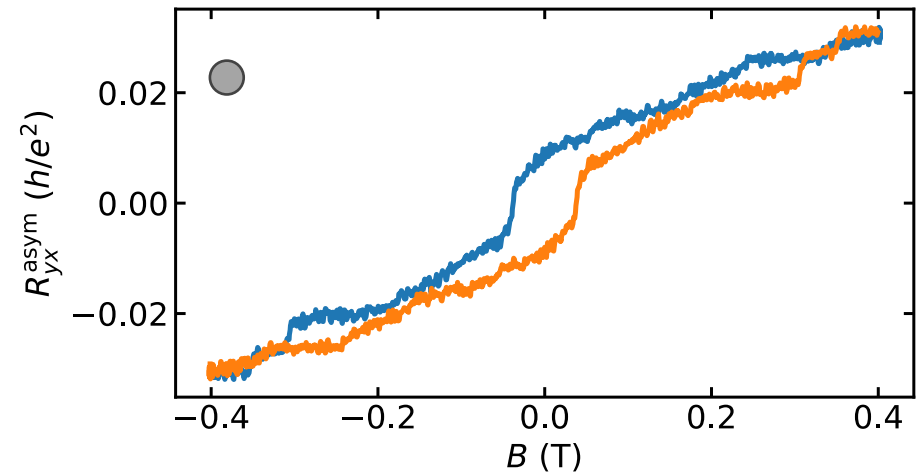
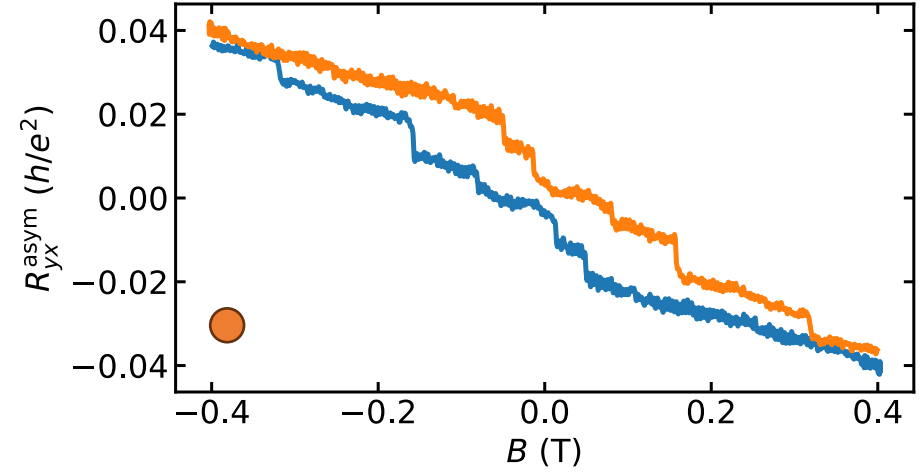
Anomalous Hall!



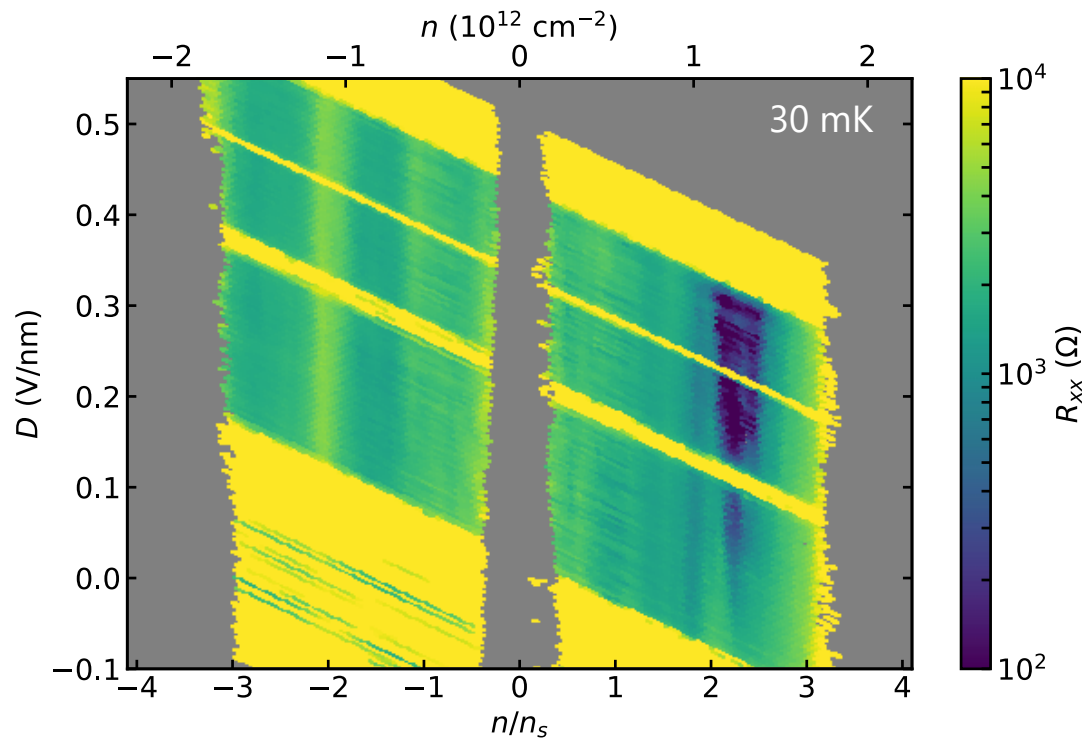
Anomalous Hall!



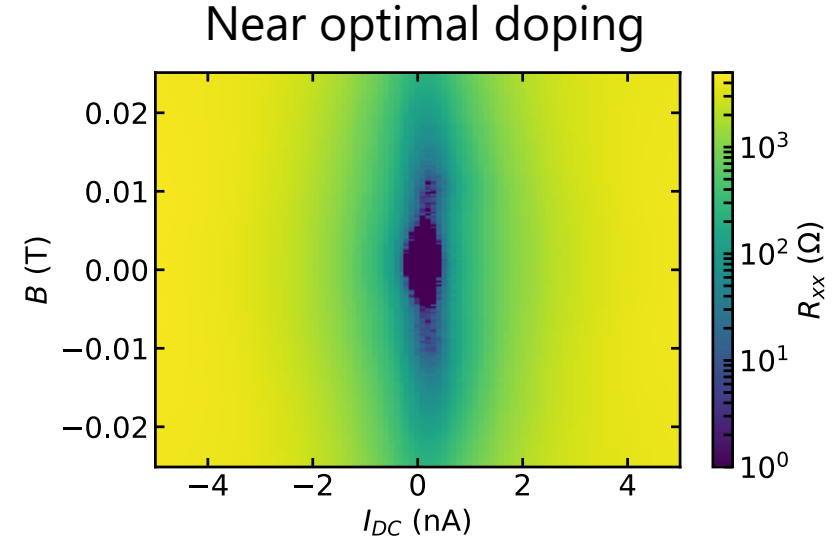
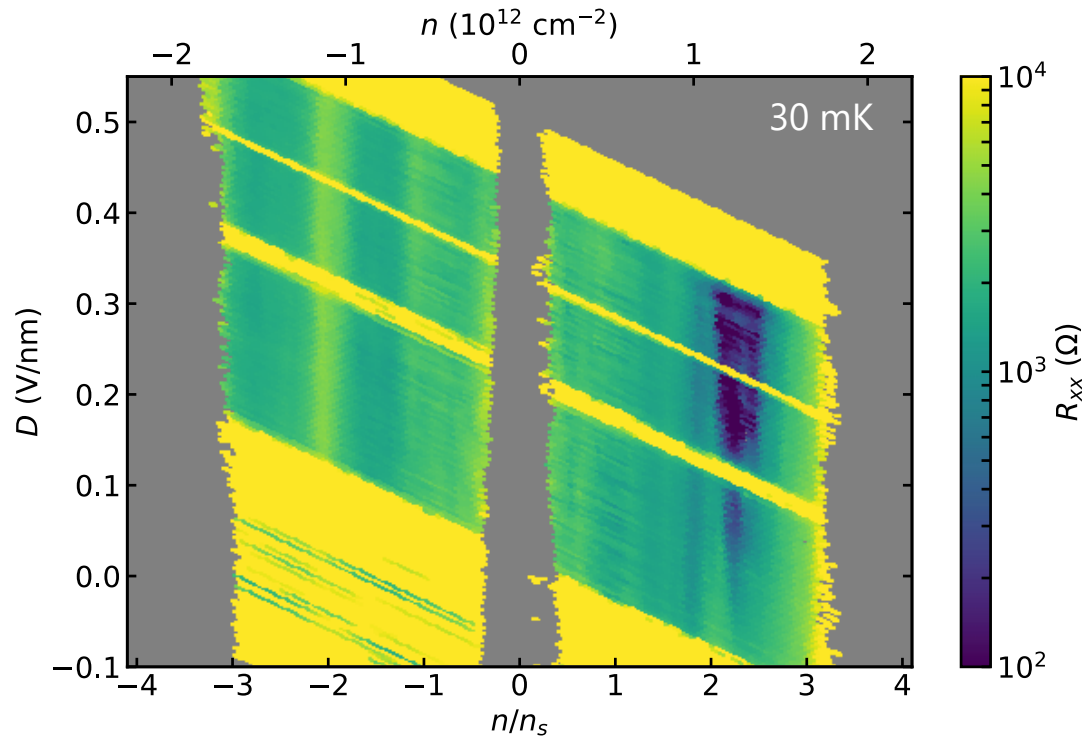
Large gap at CNP



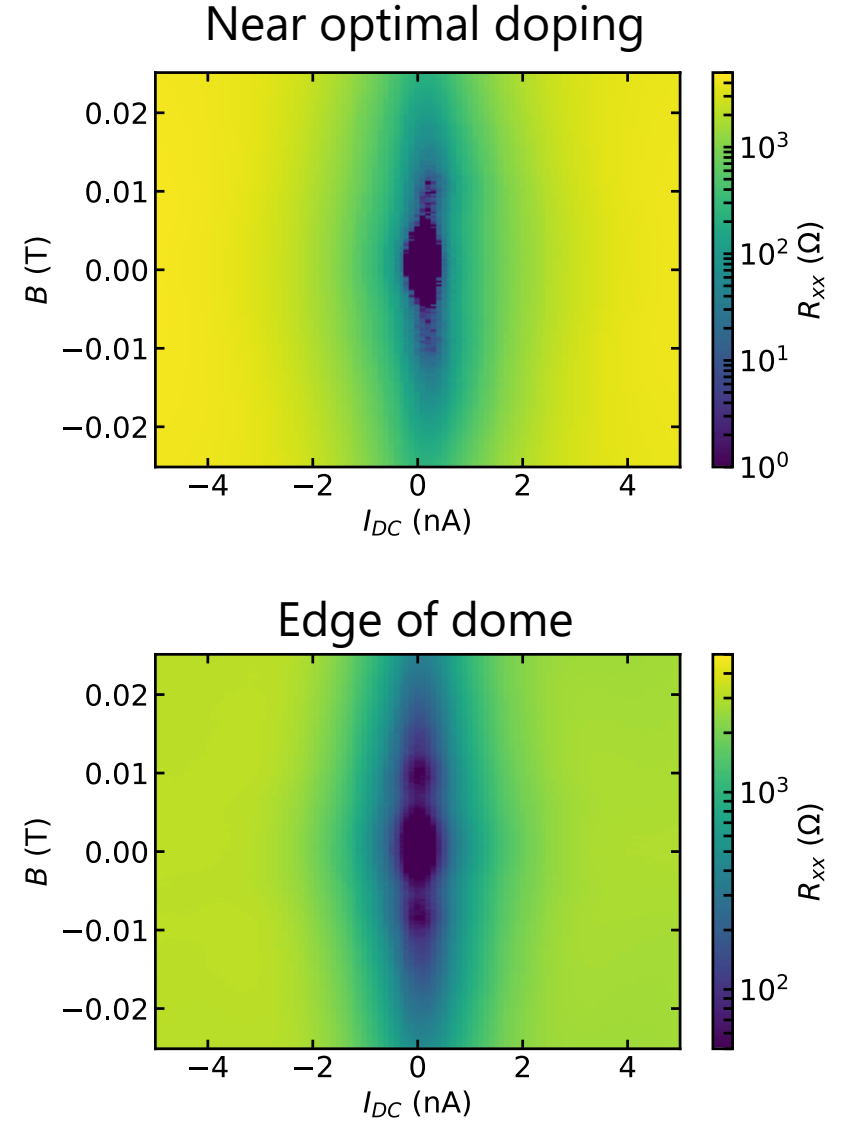
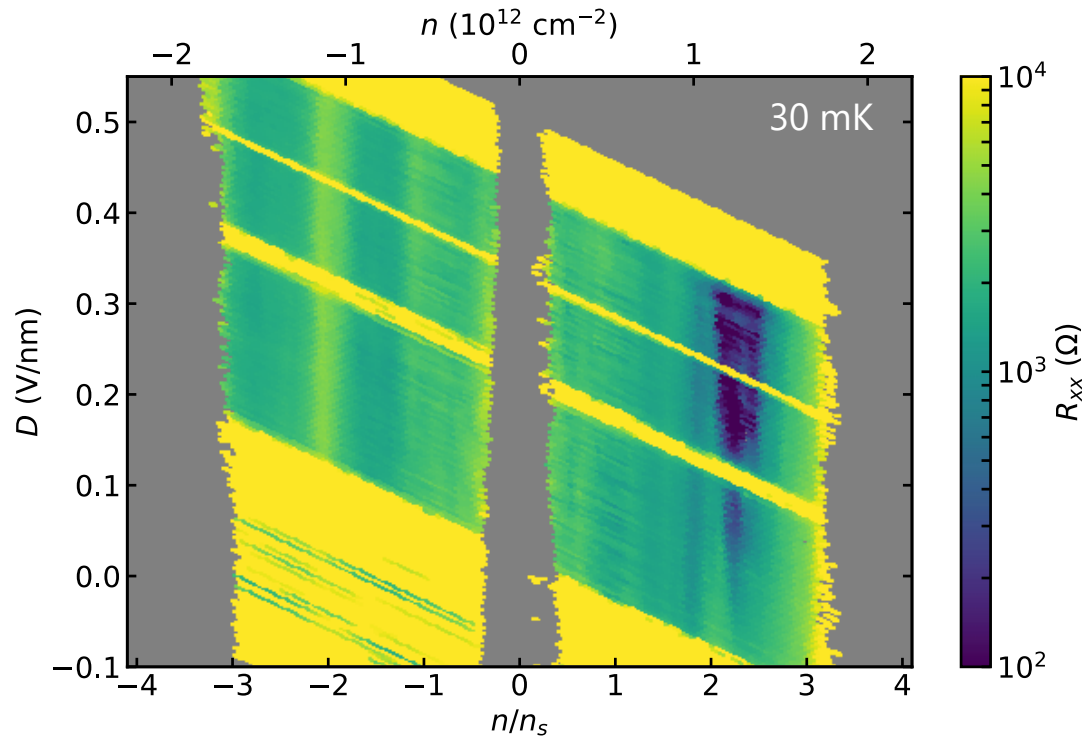
Cooling to 30 mK, superconductivity!?



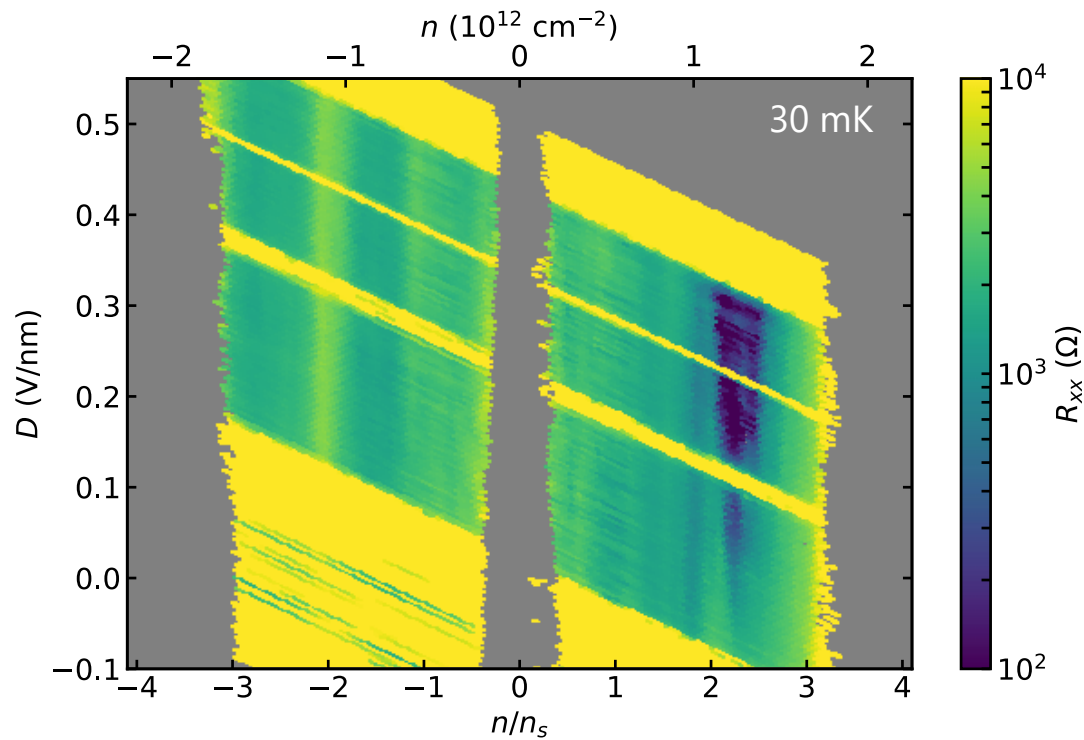
Cooling to 30 mK, superconductivity!?



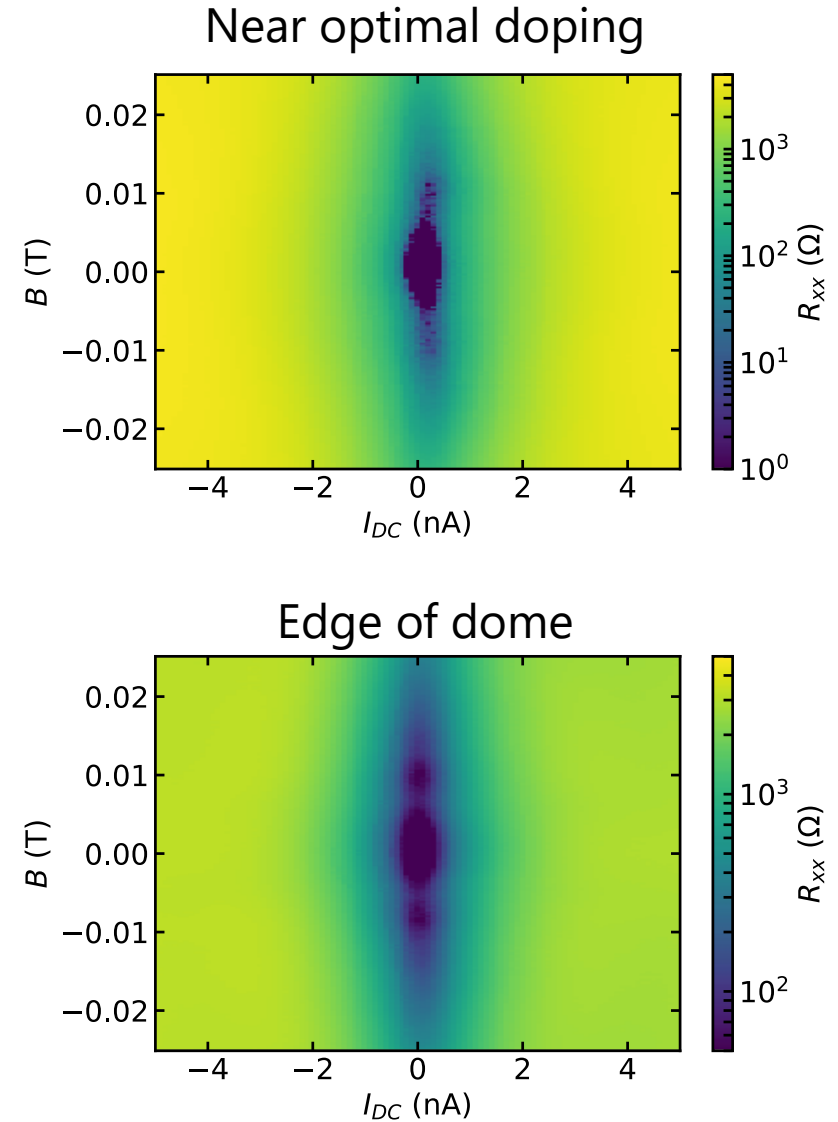
Cooling to 30 mK, superconductivity!?



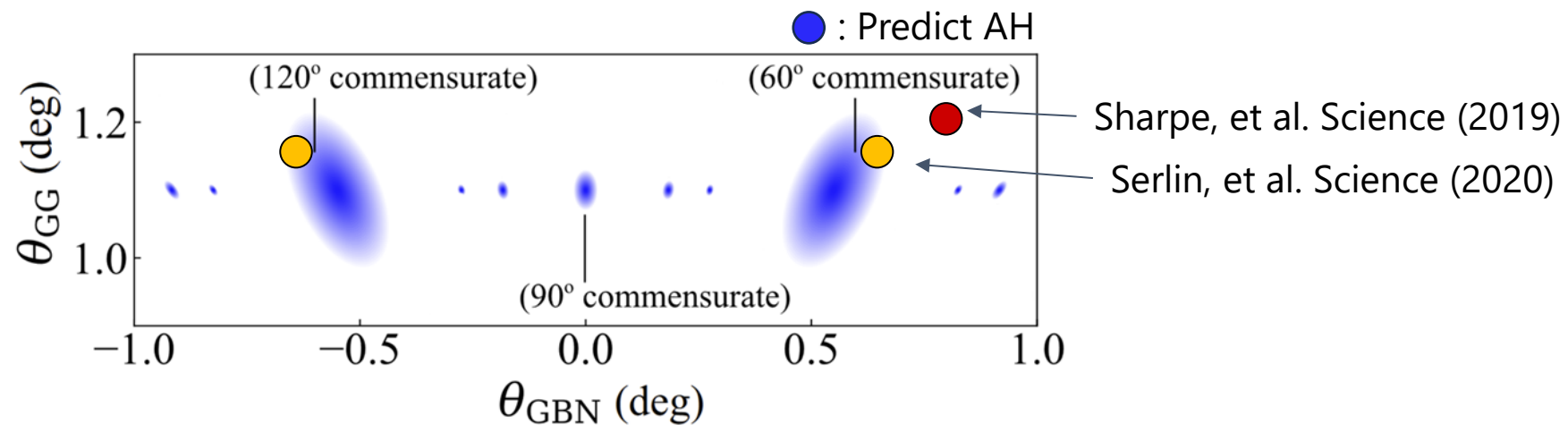
Cooling to 30 mK, superconductivity!?



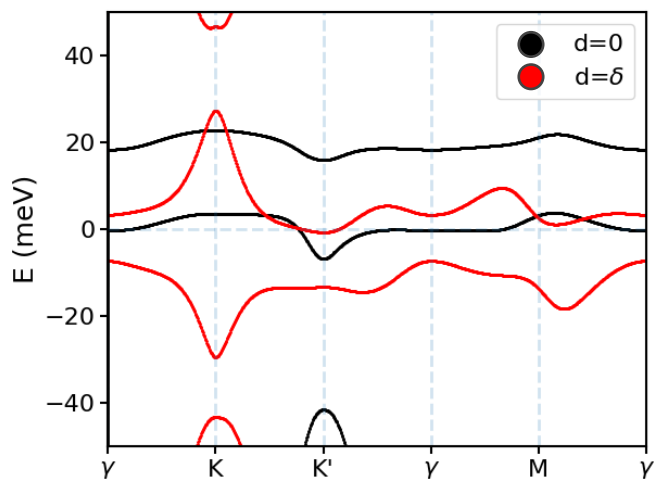
This device exhibits both magnetism and superconductivity!



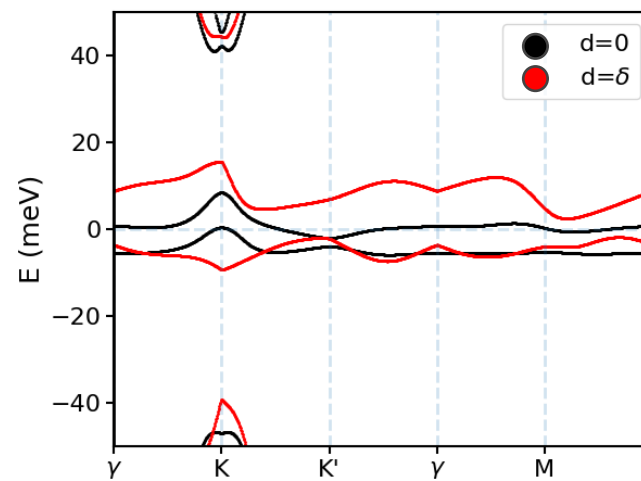
What is θ_{GBN} ?



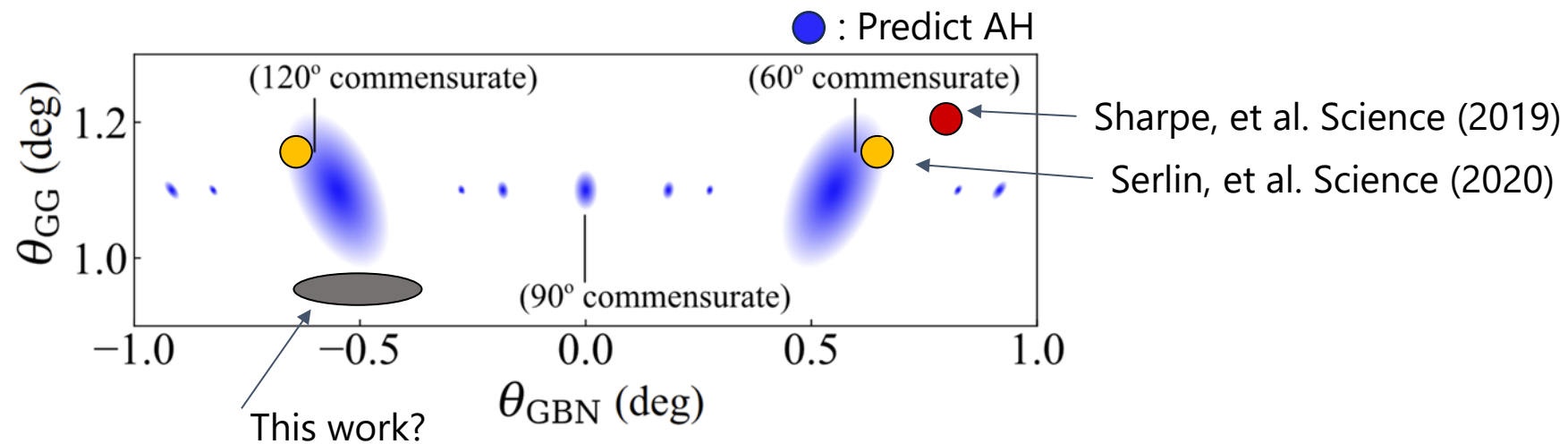
120 commensurate



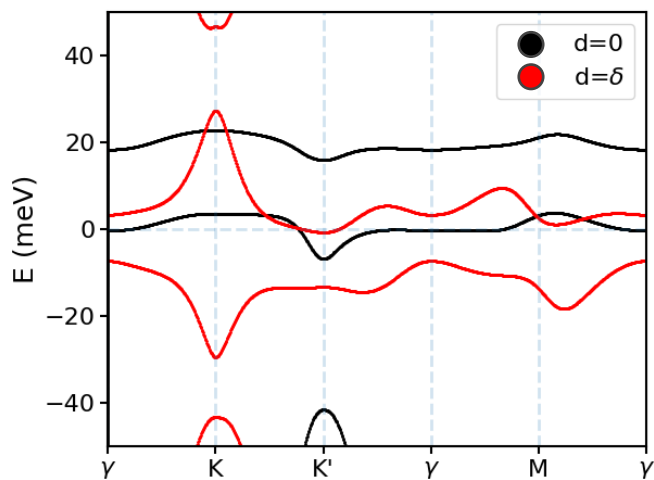
60 commensurate



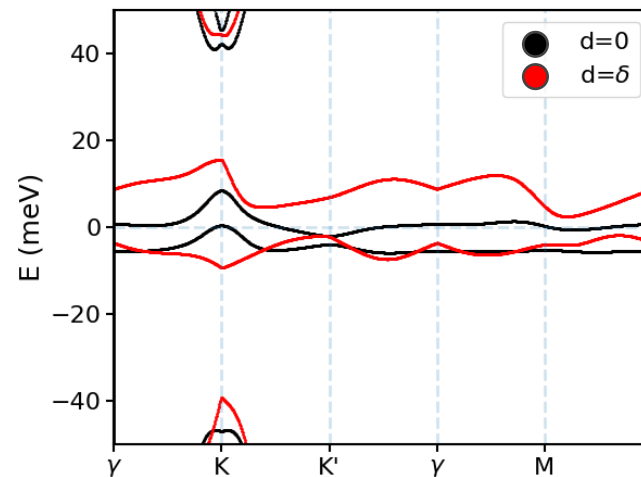
What is θ_{GBN} ?



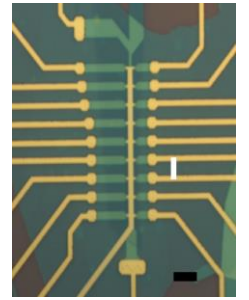
120 commensurate



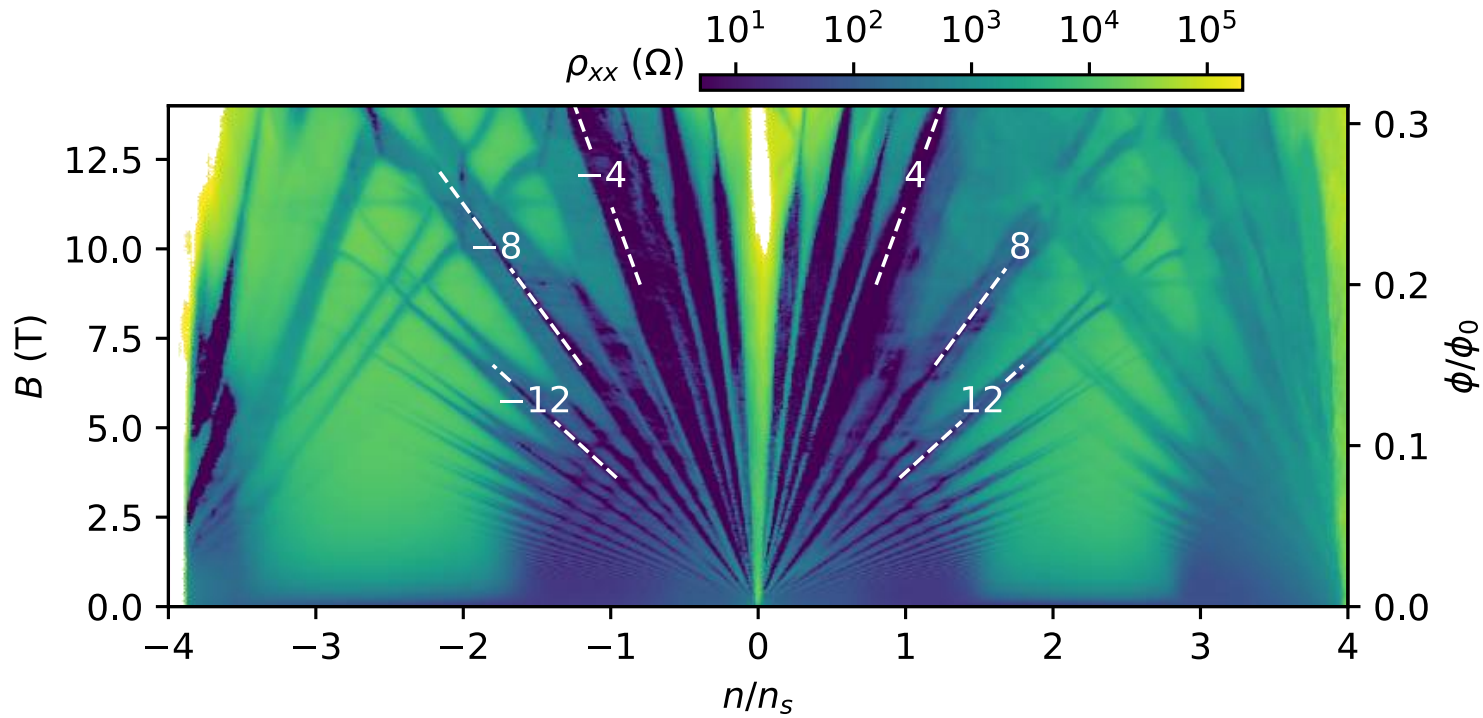
60 commensurate



TBG is still hiding secrets

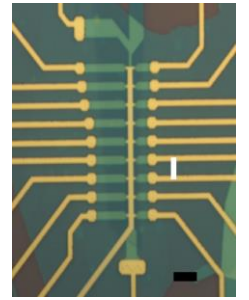
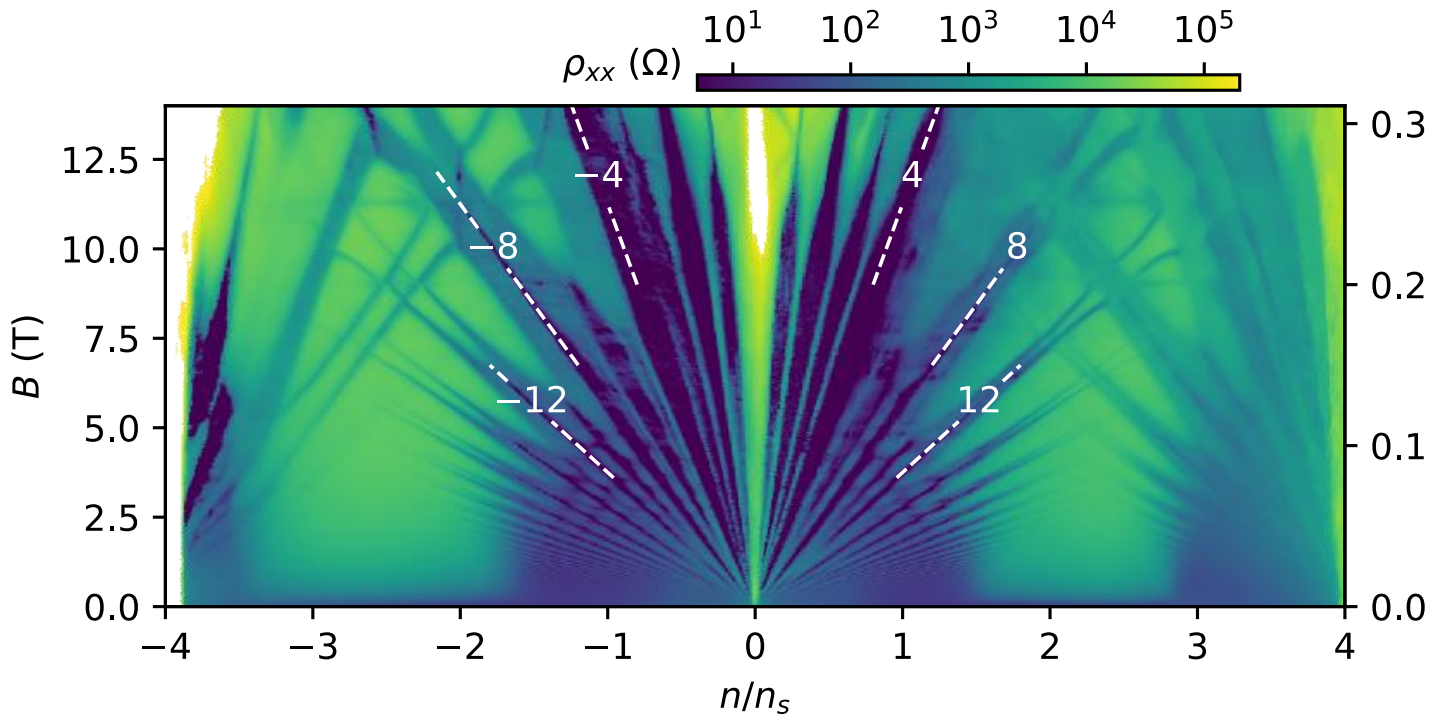


1.38° TBG

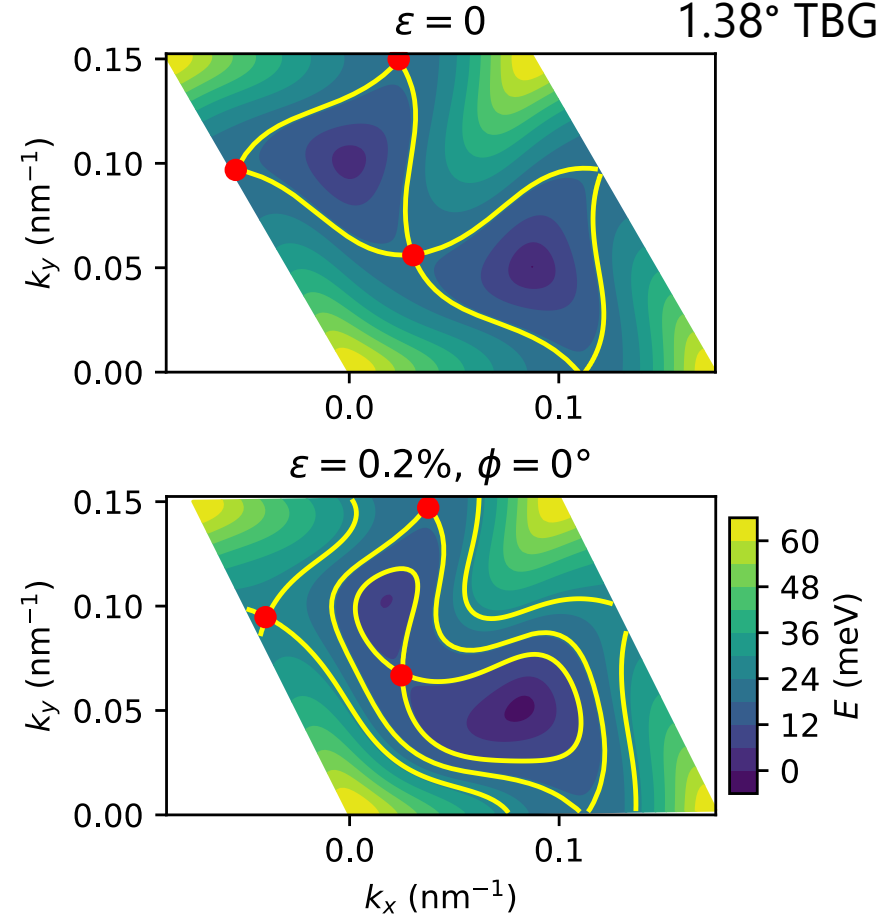


Wang, Finney, Sharpe, et al. PNAS (2023)
Finney, Sharpe, et al. PNAS (2022)

TBG is still hiding secrets

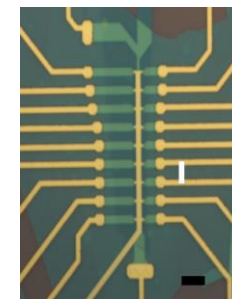
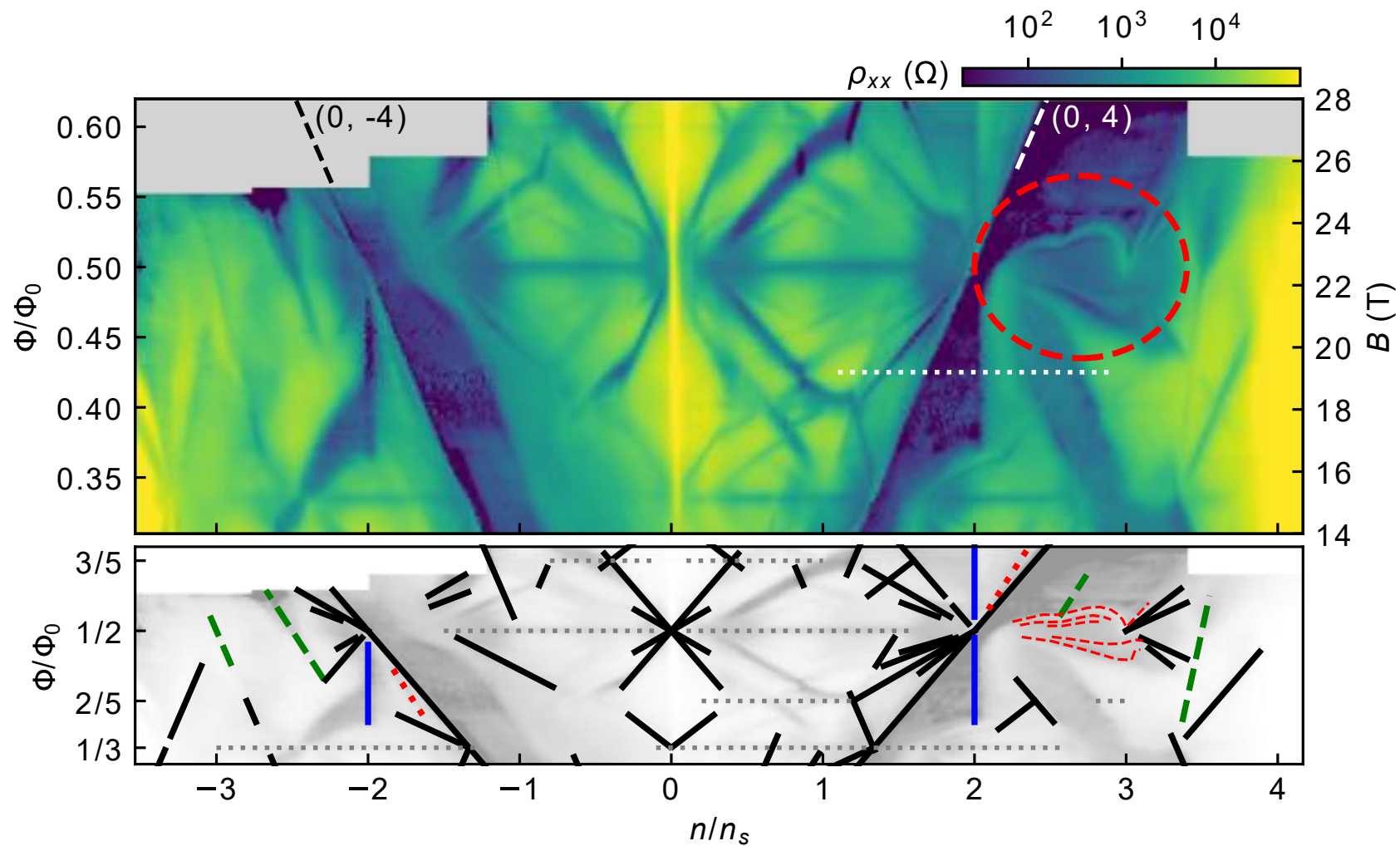


1.38° TBG



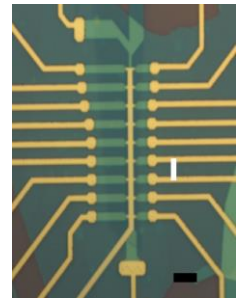
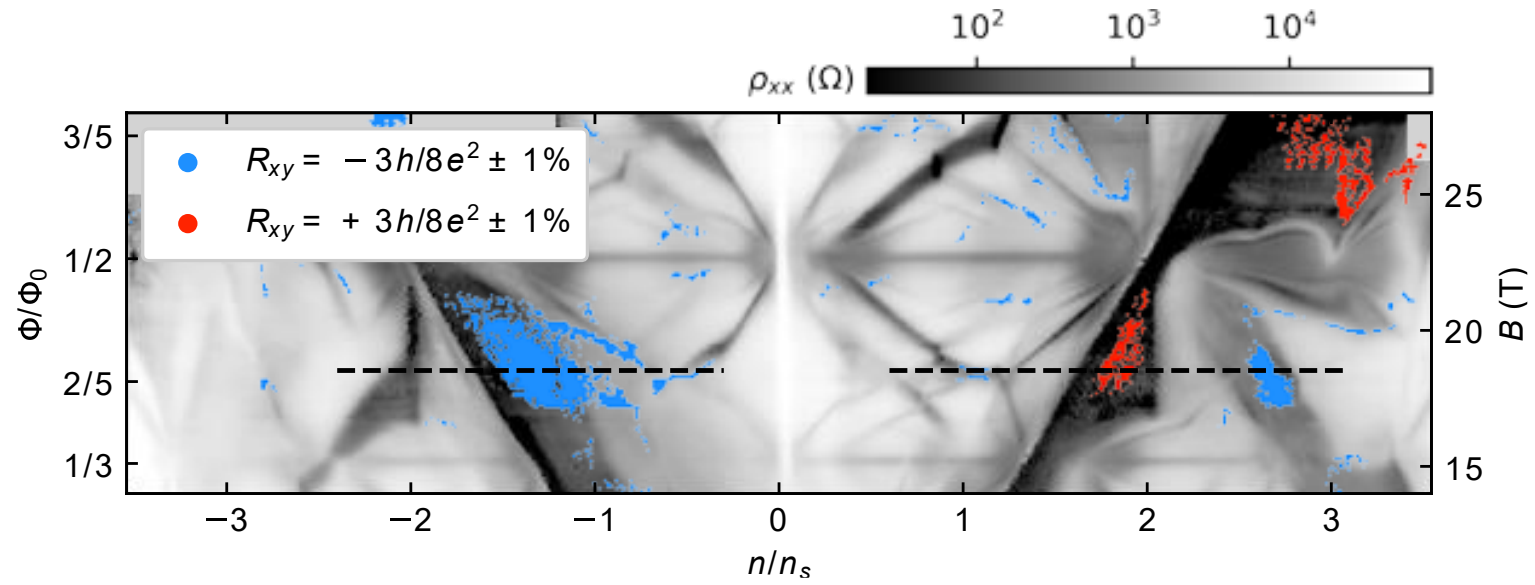
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TBG is still hiding secrets



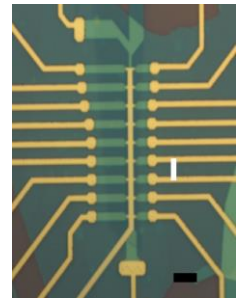
1.38° TBG

TBG is still hiding secrets

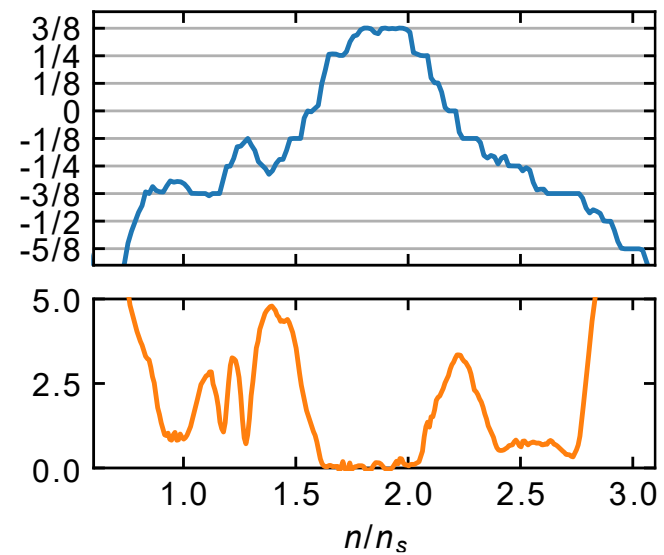
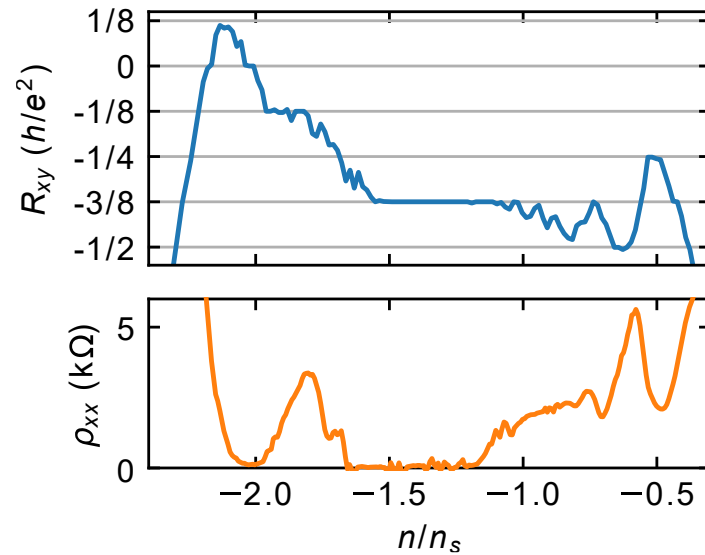
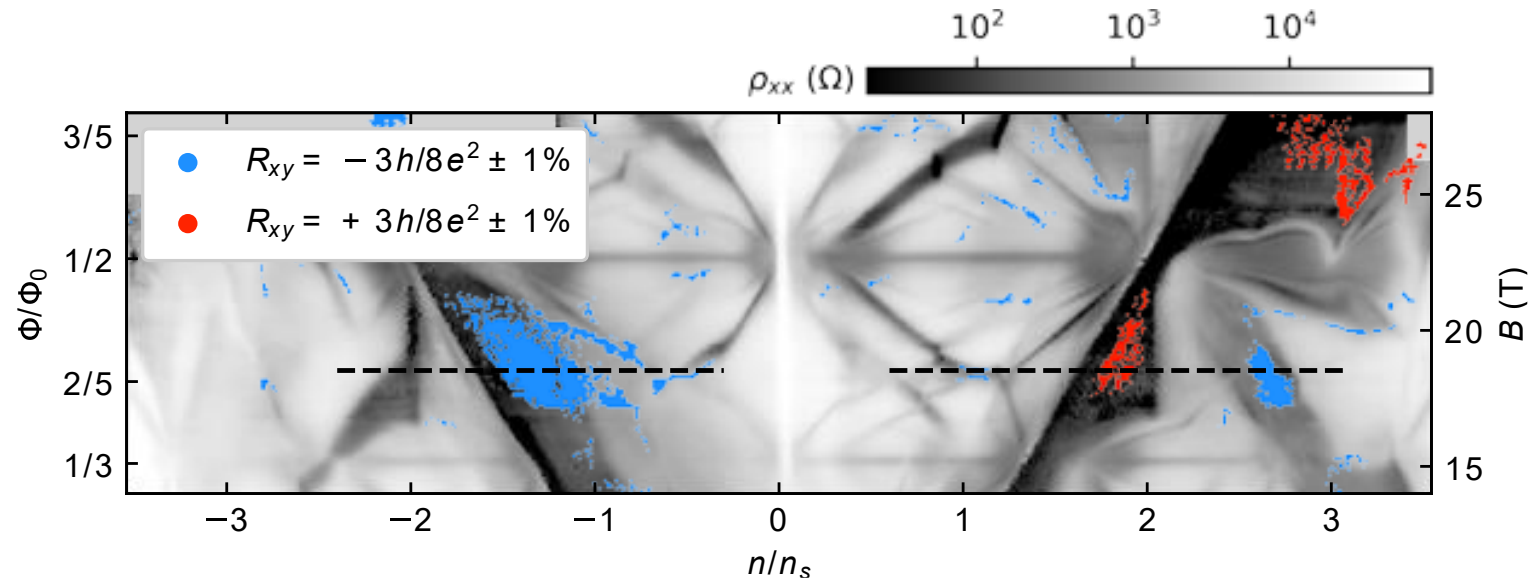


1.38° TBG

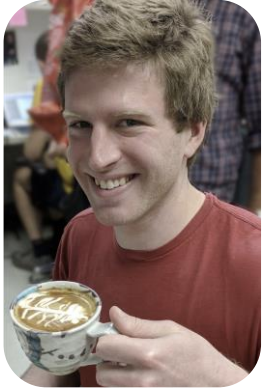
TBG is still hiding secrets



1.38° TBG



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Guorui Chen, Ya-Hui Zhang, Zuocheng Zhang, Feng Wang
Steve Kivelson, Tomohiro Soejima, Ben Feldman, Wei Pan,
Sayak Bhattacharjee, Jonah Herzog-Arbeitman

Summary

By controlling twist angle, graphene multilayers can become strongly correlated!

TBG is a Chern insulator at filling factor 3!

Magnetism is orbital in character
hBN alignment may be crucial

Why is this orbital magnet so hard to reproduce in TBG?

(Q)AH appears to be quite ubiquitous in moirés
hBN's effect is shift dependent!

Expect AH near commensurate structures?

Using intermediate characterization during fab we:

Verified hBN alignment, AH, and superconductivity
in a single sample

We still have much to learn about TBG. Explore:

G-G and G-hBN twist phase space
FCI states at high field

